# Examination in Compilers, EDAN65 

Department of Computer Science, Lund University
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## SOLUTIONS

Max points: 60
For grade 3: Min 30
For grade 4: Min 40
For grade 5: Min 50

## 1 Lexical analysis

a)

A regular expression for INT can be written, for example

$$
\text { INT }=[0-9]([-] *[0-9]+) *
$$

or

$$
\operatorname{INT}=[0-9]([0-9-] *[0-9]) ?
$$

or

$$
\text { INT }=[0-9]+\left(\left[\_\right]+[0-9]+\right) *
$$

b)

A DFA for INT

c)

A DFA for FLOAT

d)

The combined DFA

e)

An INT token for the lexeme "375_97" will be output. The scanner will need to read two more characters to decide this: "_."

## 2 Grammars

a)

For example, the sentence EOF can be derived in the following two ways:

b)

The FOLLOW set for stmt is

$$
\{\text { "\{", "\}", ID, EOF \} }
$$

To prove that each of these terminals are in the FOLLOW set, we construct derivations from the start symbol that show that each of them can follow directly after a stmt symbol. We can, for example, construct the following derivation:

```
start }=>\mathrm{ stmt EOF }=>\mathrm{ " "{" stmt "}" EOF
```

Here we see that a stmt symbol can be followed by EOF and by "\}".
To see that also " $\{$ " and ID can follow a stmt symbol, we can construct, for example, the following derivations:

```
start }=>\mathrm{ stmt EOF }=>\mathrm{ stmt stmt EOF }=>\mathrm{ s stmt ID "=" NUM ";" EOF
```

and

$$
\text { start } \Rightarrow \text { stmt EOF } \Rightarrow \text { stmt stmt EOF } \Rightarrow \text { stmt "\{" stmt "\}" EOF }
$$

c)

An equivalent grammar on EBNF form, with as few nonterminals and production alternatives as possible:

```
start -> stmt* EOF
stmt -> "{" stmt* "}" | ID "=" NUM ";"
```

d)

Equivalent LL(1) grammar:

```
po: start }->\mathrm{ stmtlist EOF
p}: : stmtlist -> stmt stmtlis
p2: stmtlist }->
p3: stmt -> "{" stmtlist "}"
p4: stmt -> ID "=" NUM ";"
```

We can check that this grammar is $\operatorname{LL}(1)$ by constructing the $\operatorname{LL}(1)$ table:

|  | " $\{$ " | "\}" | ID | "=" | "; | NUM | EOF |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| start | p0 |  | p0 |  |  |  | po |
| stmtlist | p1 | p2 | p1 |  |  |  | p2 |
| stmt | p3 |  | p4 |  |  |  |  |

Since there is no conflict, the grammar is LL(1).

## 3 Abstract grammars and analysis

a)

Abstract grammar

```
Program ::= FuncDecl*;
abstract Stmt;
abstract Expr;
FuncDecl ::= <ID> Param* FuncDecl* Stmt*;
Param ::= <ID>;
Assignment:Stmt ::= IdUse Expr;
Returnstmt:Stmt ::= Expr;
CallStmt:Stmt ::= Call;
Call : Expr ::= IdUse Expr*;
IdUse : Expr ::= <ID>;
```

b)

Attribute grammar computing FuncCall.levelsOut():

```
inh int FuncDecl.level();
inh int FuncCall.level();
eq Program.getChild().level() = 0;
eq FuncDecl.getChild().level() = level()+1;
syn int FuncCall.levelsOut() {
    if (decl() != null) {
        return level() - decl().level();
    }
    return -1;
}
```

c)

Attribute grammar computing FuncCall.decl):

```
syn FuncDecl FuncCall.decl() = lookup(getIdUse().getID());
inh FuncDecl FuncCall.lookup(String s);
eq Program.getChild().lookup(String s) {
    for (FuncDecl d : getFuncDecls())
        if (d.getID().equals(s)) return d;
    return null;
}
inh FuncDecl FuncDecl.lookup(String s);
eq FuncDecl.getChild().lookup(String s){
    for (FuncDecl d : getFuncDecls())
        if (d.getID().equals(s)) return d;
    return lookup(s);
}
```


## 4 Runtime systems

a)

Stack:

> stack of activations

b)

The frame pointer points to the start of the baz frame. Using the frame pointer, the static link for baz can be accessed ( 2 words down) and followed to the start of the foo frame. From this point, the static link for foo can be accessed ( 2 words down), and followed to the start of the main frame. From there, the local variable x is found 1 word up.

