

Tessellation

Vertex array
Index array
Exercise 2-1
Parametric surfaces
Circle ring
Sphere
Torus

Interpolation

Linear
Cubic
Exercise 2-2

Assignment 2

Tessellation
Interpolation
Demo

Tessellation & Interpolation

EDAF80: Computer Graphics

Rikard Olajos



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Circle ring
Sphere
Torus

Interpolation

Linear
Cubic
Exercise 2-2

Assignment 2

Tessellation
Interpolation
Demo

1 Tessellation

2 Interpolation

3 Assignment 2

Tessellation

- Vertex array
- Index array
- Exercise 2-1
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- Circle ring
- Sphere
- Torus

Interpolation

- Linear
- Cubic
- Exercise 2-2

Assignment 2

- Tessellation
- Interpolation
- Demo

Tessellation

TESSELLATION

Tessellation

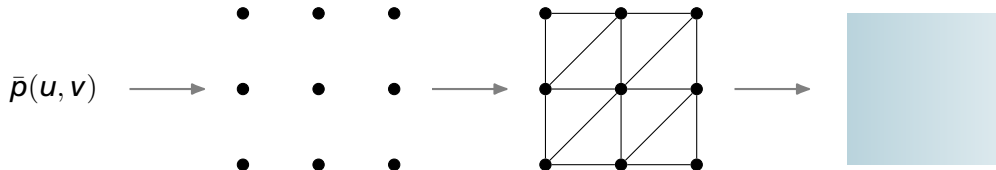
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Index array
Exercise 2-1
Parametric surfaces
Circle ring
Sphere
Torus

Interpolation

Linear
Cubic
Exercise 2-2

Assignment 2

Tessellation
Interpolation
Demo



- 1 Setup *vertex array*
- 2 Setup *index array* (triangulate)

CREATE VERTEX ARRAY

Tessellation

Vertex array
Index array
Exercise 2-1
Parametric surfaces
Circle ring
Sphere
Torus

Interpolation

Linear
Cubic
Exercise 2-2

Assignment 2

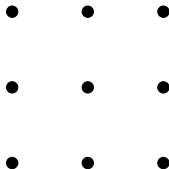
Tessellation
Interpolation
Demo

- Create vertex array (e.g. 3×3 vertices)

```
auto vertices = std::vector<glm::vec3>(9);
```

- Assign vertex

```
vertices[index] = glm::vec3(x, y, z);
```



VERTEX ARRAY LAYOUT

Tessellation

Vertex array

Index array

Exercise 2-1

Parametric surfaces

Circle ring

Sphere

Torus

Interpolation

Linear

Cubic

Exercise 2-2

Assignment 2

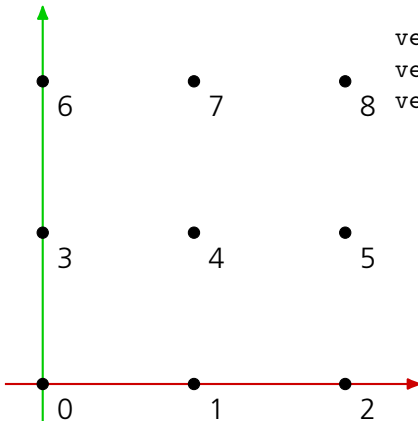
Tessellation

Interpolation

Demo

```
vertices[3].x = 0.0;  
vertices[3].y = 0.5;  
vertices[3].z = 0.0;
```

```
vertices[8].x = 1.0;  
vertices[8].y = 1.0;  
vertices[8].z = 0.0;
```



TRIANGULATION

Tessellation

Vertex array

Index array

Exercise 2-1

Parametric surfaces

Circle ring

Sphere

Torus

Interpolation

Linear

Cubic

Exercise 2-2

Assignment 2

Tessellation

Interpolation

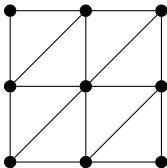
Demo

- Create index array ($2 \times (3 - 1)(3 - 1)$ triangles)

```
auto indices = std::vector<glm::uvec3>(8);
```

- Define triangle (indices for the three vertices)

```
indices[index] = glm::uvec3(v0, v1, v2);
```



Tessellation

Vertex array

Index array

Exercise 2-1

Parametric surfaces

Circle ring

Sphere

Torus

Interpolation

Linear

Cubic

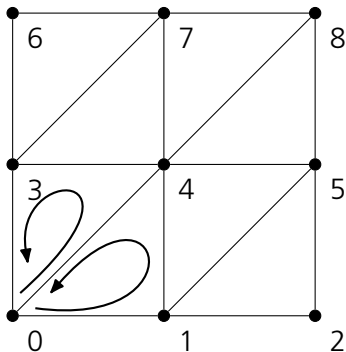
Exercise 2-2

Assignment 2

Tessellation

Interpolation

Demo



INDEX ARRAY LAYOUT

- Indices in counter-clockwise order (CCW)
- Backface culling is off by default, turn it on to improve performance!

```
indices[0].x = 0;  
indices[0].y = 1;  
indices[0].z = 4;
```

```
indices[1].x = 0;  
indices[1].y = 4;  
indices[1].z = 3;
```

```
glEnable(GL_CULL_FACE);  
glCullFace(GL_BACK); // GL_BACK (default), GL_FRONT, GL_FRONT_AND_BACK  
glFrontFace(GL_CCW); // GL_CCW (default), GL_CW
```


Tessellation

Vertex array

Index array

Exercise 2-1

Parametric surfaces

Circle ring

Sphere

Torus

Interpolation

Linear

Cubic

Exercise 2-2

Assignment 2

Tessellation

Interpolation

Demo

Seminar Exercise 2-1: Indexed Draw and Vertex Attributes

- 1 Change the index list to draw a triangle between vertices 3, 4 and 5.
- 2 Keep the green triangle and add back the original red triangle.
- 3 Try changing the color of the vertices by changing the vertex attributes.

FOLLOW-UP QUESTIONS

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Vertex array

Index array

Exercise 2-1

Parametric surfaces

Circle ring

Sphere

Torus

Interpolation

Linear

Cubic

Exercise 2-2

Assignment 2

Tessellation

Interpolation

Demo

- 1 Can you control which triangle that ends up on top?
- 2 What happens when attributes within a triangle have different values?

PARAMETRIC SURFACES

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Vertex array

Index array

Exercise 2-1

Parametric surfaces

Circle ring

Sphere

Torus

Interpolation

Linear

Cubic

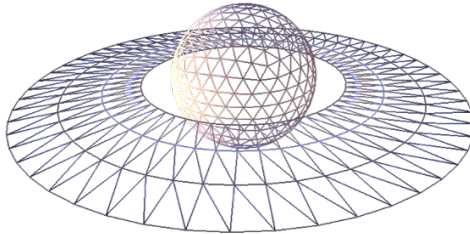
Exercise 2-2

Assignment 2

Tessellation

Interpolation

Demo



PARAMETRIC SURFACE & TANGENT SPACE

Tessellation

Vertex array

Index array

Exercise 2-1

Parametric surfaces

Circle ring

Sphere

Torus

Interpolation

Linear

Cubic

Exercise 2-2

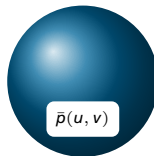
Assignment 2

Tessellation

Interpolation

Demo

- Map surface from 2D:
 $\bar{p}(x, y, z) = \bar{p}(u, v)$
- $\mathbb{R}^2 \mapsto \mathbb{R}^3$



PARAMETRIC SURFACE & TANGENT SPACE

Tessellation

Vertex array

Index array

Exercise 2-1

Parametric surfaces

Circle ring

Sphere

Torus

Interpolation

Linear

Cubic

Exercise 2-2

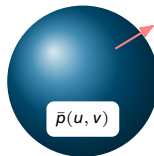
Assignment 2

Tessellation

Interpolation

Demo

- Map surface from 2D:
 $\bar{p}(x, y, z) = \bar{p}(u, v)$
- $\mathbb{R}^2 \mapsto \mathbb{R}^3$
 - Tangent $\mathbf{t} = \frac{\partial \bar{p}}{\partial u}$



PARAMETRIC SURFACE & TANGENT SPACE

Tessellation

Vertex array

Index array

Exercise 2-1

Parametric surfaces

Circle ring

Sphere

Torus

Interpolation

Linear

Cubic

Exercise 2-2

Assignment 2

Tessellation

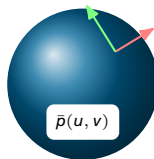
Interpolation

Demo

- Map surface from 2D:

$$\bar{p}(x, y, z) = \bar{p}(u, v)$$

- $\mathbb{R}^2 \mapsto \mathbb{R}^3$
 - Tangent $\mathbf{t} = \frac{\partial \bar{p}}{\partial u}$
 - Binormal $\mathbf{b} = \frac{\partial \bar{p}}{\partial v}$



PARAMETRIC SURFACE & TANGENT SPACE

Tessellation

Vertex array

Index array

Exercise 2-1

Parametric surfaces

Circle ring

Sphere

Torus

Interpolation

Linear

Cubic

Exercise 2-2

Assignment 2

Tessellation

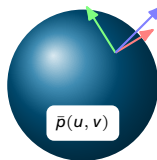
Interpolation

Demo

- Map surface from 2D:

$$\bar{p}(x, y, z) = \bar{p}(u, v)$$

- $\mathbb{R}^2 \mapsto \mathbb{R}^3$
 - Tangent $\mathbf{t} = \frac{\partial \bar{p}}{\partial u}$
 - Binormal $\mathbf{b} = \frac{\partial \bar{p}}{\partial v}$
 - Normal $\mathbf{n} = \frac{\partial \bar{p}}{\partial u} \times \frac{\partial \bar{p}}{\partial v}$



CIRCLE RING

Tessellation

Vertex array
Index array
Exercise 2-1
Parametric surfaces
Circle ring
Sphere
Torus

$$\bar{\mathbf{p}}(r, \theta) = \begin{Bmatrix} r \cos(\theta) \\ r \sin(\theta) \\ 0 \end{Bmatrix} \text{ for } \begin{matrix} r_1 \leq r \leq r_2 \\ 0 \leq \theta < 2\pi \end{matrix}$$

Interpolation

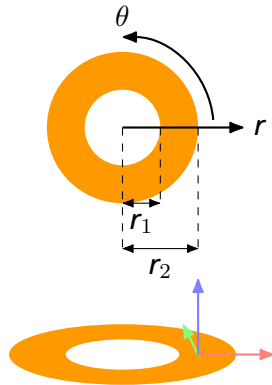
Linear
Cubic
Exercise 2-2

$$\mathbf{t} = \frac{\partial \bar{\mathbf{p}}}{\partial r} = \begin{Bmatrix} \cos(\theta) \\ \sin(\theta) \\ 0 \end{Bmatrix}$$

Assignment 2

Tessellation
Interpolation
Demo

$$\mathbf{b} = \frac{\partial \bar{\mathbf{p}}}{\partial \theta} = \begin{Bmatrix} -r \sin(\theta) \\ r \cos(\theta) \\ 0 \end{Bmatrix}$$



SPHERE

Tessellation

Vertex array
Index array
Exercise 2-1
Parametric surfaces
Circle ring
Sphere
Torus

$$\bar{\mathbf{p}}(\theta, \varphi) = \begin{cases} r \sin(\theta) \sin(\varphi) \\ -r \cos(\varphi) \\ r \cos(\theta) \sin(\varphi) \end{cases} \text{ for } \begin{cases} 0 \leq \theta \leq 2\pi \\ 0 \leq \varphi \leq \pi \end{cases}$$

Interpolation

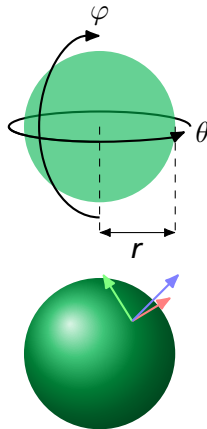
Linear
Cubic
Exercise 2-2

Assignment 2

Tessellation
Interpolation
Demo

$$\mathbf{t} = \frac{\partial \bar{\mathbf{p}}}{\partial \theta} = \begin{cases} r \cos(\theta) \sin(\varphi) \\ 0 \\ -r \sin(\theta) \sin(\varphi) \end{cases}$$

$$\mathbf{b} = \frac{\partial \bar{\mathbf{p}}}{\partial \varphi} = \begin{cases} r \sin(\theta) \cos(\varphi) \\ r \sin(\varphi) \\ r \cos(\theta) \cos(\varphi) \end{cases}$$



SPHERE

Tessellation

Vertex array
Index array
Exercise 2-1
Parametric surfaces
Circle ring
Sphere
Torus

Interpolation

Linear
Cubic
Exercise 2-2

Assignment 2

Tessellation
Interpolation
Demo

$$\bar{\mathbf{p}}(\theta, \varphi) = \begin{Bmatrix} r \sin(\theta) \sin(\varphi) \\ -r \cos(\varphi) \\ r \cos(\theta) \sin(\varphi) \end{Bmatrix} \text{ for } \begin{matrix} 0 \leq \theta \leq 2\pi \\ 0 \leq \varphi \leq \pi \end{matrix}$$

$$\mathbf{t} = \frac{\partial \bar{\mathbf{p}}}{\partial \theta} = \begin{Bmatrix} r \cos(\theta) \sin(\varphi) \\ 0 \\ -r \sin(\theta) \sin(\varphi) \end{Bmatrix}$$

$$\mathbf{b} = \frac{\partial \bar{\mathbf{p}}}{\partial \varphi} = \begin{Bmatrix} r \sin(\theta) \cos(\varphi) \\ r \sin(\varphi) \\ r \cos(\theta) \cos(\varphi) \end{Bmatrix}$$

- \mathbf{t} and \mathbf{b} can be simplified since only direction is important
- \mathbf{t} *needs* to be simplified, or it will be undefined for $\varphi = 0$

Tessellation

Vertex array
Index array
Exercise 2-1
Parametric surfaces
Circle ring
Sphere
Torus

$$\bar{\mathbf{p}}(\theta, \varphi) = \begin{cases} (r_a + r_b \cos(\theta)) \cos(\varphi) \\ (r_a + r_b \cos(\theta)) \sin(\varphi) \\ -r_b \sin(\theta) \end{cases} \text{ for } \begin{cases} 0 \leq \theta \leq 2\pi \\ 0 \leq \varphi \leq 2\pi \end{cases}$$

Interpolation

Linear
Cubic
Exercise 2-2

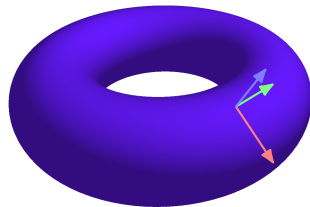
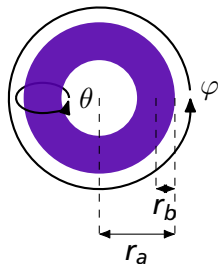
Assignment 2

Tessellation
Interpolation
Demo

$$\mathbf{t} = \frac{\partial \bar{\mathbf{p}}}{\partial \theta} = \begin{cases} -r_b \sin(\theta) \cos(\varphi) \\ -r_b \sin(\theta) \sin(\varphi) \\ -r_b \cos(\theta) \end{cases}$$

$$\mathbf{b} = \frac{\partial \bar{\mathbf{p}}}{\partial \varphi} = \begin{cases} -(r_a + r_b \cos(\theta)) \sin(\varphi) \\ (r_a + r_b \cos(\theta)) \cos(\varphi) \\ 0 \end{cases}$$

TORUS



Tessellation

- Vertex array
- Index array
- Exercise 2-1
- Parametric surfaces
- Circle ring
- Sphere
- Torus

Interpolation

- Linear
- Cubic
- Exercise 2-2

Assignment 2

- Tessellation
- Interpolation
- Demo

Interpolation

LINEAR INTERPOLATION (LERP)

Tessellation

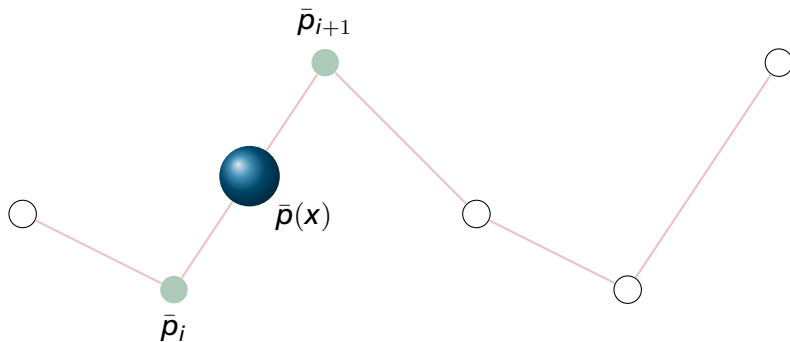
Vertex array
Index array
Exercise 2-1
Parametric surfaces
Circle ring
Sphere
Torus

Interpolation

Linear
Cubic
Exercise 2-2

Assignment 2

Tessellation
Interpolation
Demo



$$\bar{p}(x) = \begin{bmatrix} 1 & x \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} \bar{p}_i \\ \bar{p}_{i+1} \end{bmatrix} \text{ for } x \in [0, 1]$$

LINEAR INTERPOLATION (LERP)

Tessellation

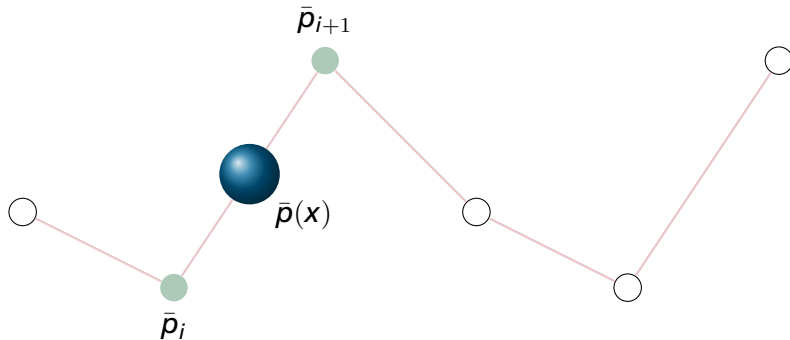
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Index array
Exercise 2-1
Parametric surfaces
Circle ring
Sphere
Torus

Interpolation

Linear
Cubic
Exercise 2-2

Assignment 2

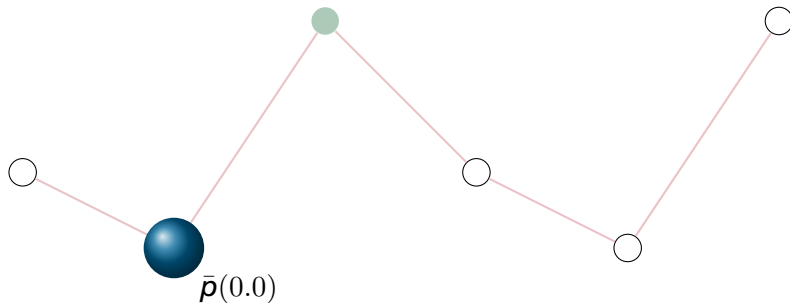
Tessellation
Interpolation
Demo



$$\bar{p}(x) = \begin{bmatrix} 1 & x \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} \bar{p}_i \\ \bar{p}_{i+1} \end{bmatrix} \text{ for } x \in [0, 1]$$

$$\bar{p}(x) = (1 - x)\bar{p}_i + x\bar{p}_{i+1}$$

LINEAR INTERPOLATION (LERP)



$$\bar{p}(x) = \begin{bmatrix} 1 & x \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} \bar{p}_i \\ \bar{p}_{i+1} \end{bmatrix} \text{ for } x \in [0, 1]$$

$$\bar{p}(x) = (1 - x)\bar{p}_i + x\bar{p}_{i+1}$$

Tessellation

Vertex array
Index array
Exercise 2-1
Parametric surfaces
Circle ring
Sphere
Torus

Interpolation

Linear
Cubic
Exercise 2-2

Assignment 2

Tessellation
Interpolation
Demo

LINEAR INTERPOLATION (LERP)

Tessellation

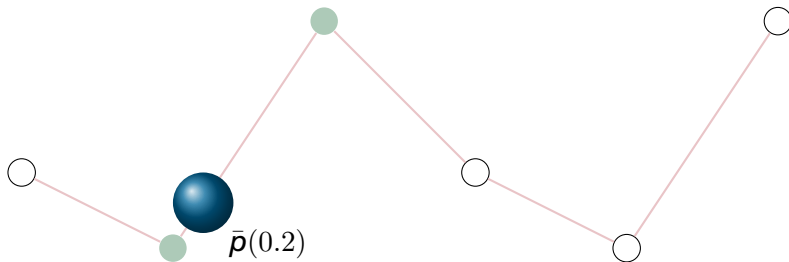
Vertex array
Index array
Exercise 2-1
Parametric surfaces
Circle ring
Sphere
Torus

Interpolation

Linear
Cubic
Exercise 2-2

Assignment 2

Tessellation
Interpolation
Demo



$$\bar{p}(x) = \begin{bmatrix} 1 & x \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} \bar{p}_i \\ \bar{p}_{i+1} \end{bmatrix} \text{ for } x \in [0, 1]$$

$$\bar{p}(x) = (1 - x)\bar{p}_i + x\bar{p}_{i+1}$$

LINEAR INTERPOLATION (LERP)

Tessellation

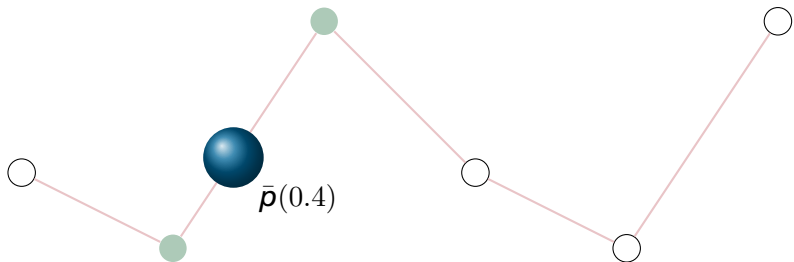
Vertex array
Index array
Exercise 2-1
Parametric surfaces
Circle ring
Sphere
Torus

Interpolation

Linear
Cubic
Exercise 2-2

Assignment 2

Tessellation
Interpolation
Demo



$$\bar{p}(x) = \begin{bmatrix} 1 & x \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} \bar{p}_i \\ \bar{p}_{i+1} \end{bmatrix} \text{ for } x \in [0, 1]$$

$$\bar{p}(x) = (1 - x)\bar{p}_i + x\bar{p}_{i+1}$$

LINEAR INTERPOLATION (LERP)

Tessellation

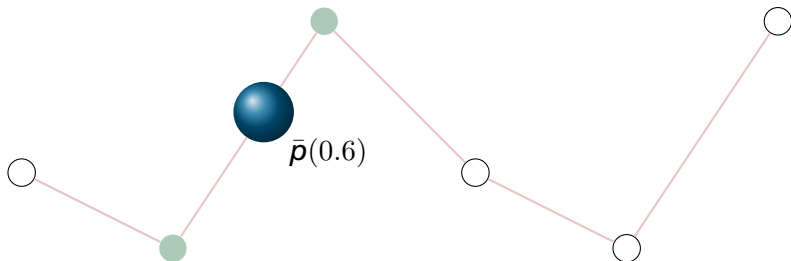
Vertex array
Index array
Exercise 2-1
Parametric surfaces
Circle ring
Sphere
Torus

Interpolation

Linear
Cubic
Exercise 2-2

Assignment 2

Tessellation
Interpolation
Demo



$$\bar{p}(x) = \begin{bmatrix} 1 & x \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} \bar{p}_i \\ \bar{p}_{i+1} \end{bmatrix} \text{ for } x \in [0, 1]$$

$$\bar{p}(x) = (1 - x)\bar{p}_i + x\bar{p}_{i+1}$$

LINEAR INTERPOLATION (LERP)

Tessellation

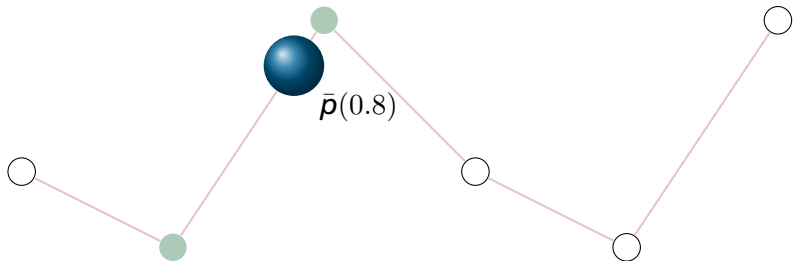
Vertex array
Index array
Exercise 2-1
Parametric surfaces
Circle ring
Sphere
Torus

Interpolation

Linear
Cubic
Exercise 2-2

Assignment 2

Tessellation
Interpolation
Demo



$$\bar{p}(x) = \begin{bmatrix} 1 & x \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} \bar{p}_i \\ \bar{p}_{i+1} \end{bmatrix} \text{ for } x \in [0, 1]$$

$$\bar{p}(x) = (1 - x)\bar{p}_i + x\bar{p}_{i+1}$$

LINEAR INTERPOLATION (LERP)

Tessellation

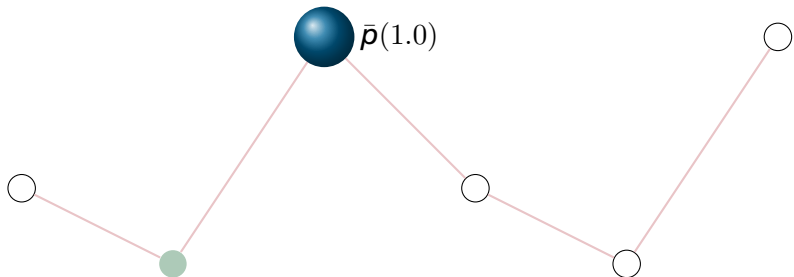
Vertex array
Index array
Exercise 2-1
Parametric surfaces
Circle ring
Sphere
Torus

Interpolation

Linear
Cubic
Exercise 2-2

Assignment 2

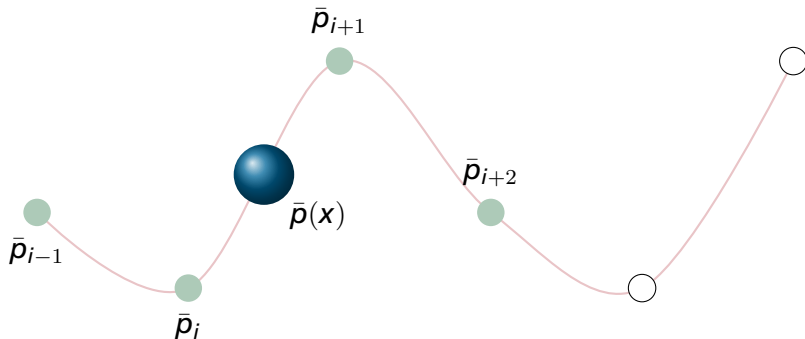
Tessellation
Interpolation
Demo



$$\bar{p}(x) = \begin{bmatrix} 1 & x \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} \bar{p}_i \\ \bar{p}_{i+1} \end{bmatrix} \text{ for } x \in [0, 1]$$

$$\bar{p}(x) = (1 - x)\bar{p}_i + x\bar{p}_{i+1}$$

CUBIC INTERPOLATION (CATMULL-ROM)



$$\bar{q}(x) = \begin{bmatrix} 1 & x & x^2 & x^3 \end{bmatrix} \begin{bmatrix} 0 & 1 & 0 & 0 \\ -\tau & 0 & \tau & 0 \\ 2\tau & \tau - 3 & 3 - 2\tau & -\tau \\ -\tau & 2 - \tau & \tau - 2 & \tau \end{bmatrix} \begin{bmatrix} \bar{p}_{i-1} \\ \bar{p}_i \\ \bar{p}_{i+1} \\ \bar{p}_{i+2} \end{bmatrix} \text{ for } x \in [0, 1]$$

Tessellation

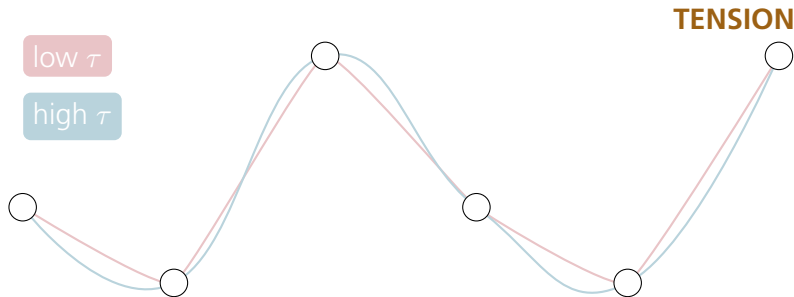
Vertex array
Index array
Exercise 2-1
Parametric surfaces
Circle ring
Sphere
Torus

Interpolation

Linear
Cubic
Exercise 2-2

Assignment 2

Tessellation
Interpolation
Demo



$$\bar{q}(x) = \begin{bmatrix} 1 & x & x^2 & x^3 \end{bmatrix} \begin{bmatrix} 0 & 1 & 0 & 0 \\ -\tau & 0 & \tau & 0 \\ 2\tau & \tau - 3 & 3 - 2\tau & -\tau \\ -\tau & 2 - \tau & \tau - 2 & \tau \end{bmatrix} \begin{bmatrix} \bar{p}_{i-1} \\ \bar{p}_i \\ \bar{p}_{i+1} \\ \bar{p}_{i+2} \end{bmatrix} \text{ for } x \in [0, 1]$$

Tessellation

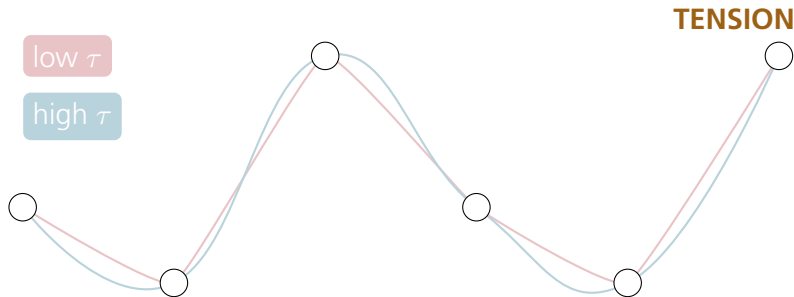
Vertex array
Index array
Exercise 2-1
Parametric surfaces
Circle ring
Sphere
Torus

Interpolation

Linear
Cubic
Exercise 2-2

Assignment 2

Tessellation
Interpolation
Demo



$$\bar{q}(x) = \begin{bmatrix} 1 & x & x^2 & x^3 \end{bmatrix} \begin{bmatrix} 0 & 1 & 0 & 0 \\ -\tau & 0 & \tau & 0 \\ 2\tau & \tau - 3 & 3 - 2\tau & -\tau \\ -\tau & 2 - \tau & \tau - 2 & \tau \end{bmatrix} \begin{bmatrix} \bar{p}_{i-1} \\ \bar{p}_i \\ \bar{p}_{i+1} \\ \bar{p}_{i+2} \end{bmatrix} \text{ for } x \in [0, 1]$$

- τ = tension, how “stiff” the curve is at the control points
- Keep within $[0, 1]$
- Good initial value: 0.5

Seminar Exercise 2-2: Interpolation

Tessellation

Vertex array
Index array
Exercise 2-1
Parametric surfaces
Circle ring
Sphere
Torus

Interpolation

Linear
Cubic
Exercise 2-2

Assignment 2

Tessellation
Interpolation
Demo

- 1 Make the top vertex of the triangle (`gl_VertexID 2`) move between point `p0` at $(-1.0, 1.0, 0.0)$ and `p1` at $(1.0, -0.3, 0.0)$.
 - Use `mix()` to do linear interpolation in GLSL.
 - Use the `time` uniform to animate, but remember to keep the `t` value of the interpolation between 0 and 1. Try using `mod()` or `sin()`.
- 2 Animate the color of the triangle by changing the color output in the fragment shader. Have it interpolate between two colors `c0` and `c1`.
- 3 Spend a few minutes and trying different combinations of animations: different vertex ID, other colors, maybe throw in an extra point to interpolate with and use nested mix functions.

Tessellation

- Vertex array
- Index array
- Exercise 2-1
- Parametric surfaces
- Circle ring
- Sphere
- Torus

Interpolation

- Linear
- Cubic
- Exercise 2-2

Assignment 2

- Tessellation
- Interpolation
- Demo

Assignment 2

Tessellation

Vertex array
Index array
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Assignment 2

Tessellation
Interpolation
Demo

- Tessellate objects from parametric equations
- Linear and cubic interpolation
- Files you have to modify
 - `src/EDAF80/assignment2.cpp`
 - `src/EDAF80/parametric_shapes.cpp`
 - `src/EDAF80/interpolation.cpp`

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Cubic
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Assignment 2

Tessellation
Interpolation
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- Implement function bodies in `src/EDAF80/parametric_shapes.cpp`

```
bonobo::mesh_data parametric_shapes::createQuad(...);  
bonobo::mesh_data parametric_shapes::createSphere(...);  
bonobo::mesh_data parametric_shapes::createTorus(...); // Optional
```

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Vertex array
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Sphere
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Linear
Cubic
Exercise 2-2

Assignment 2

Tessellation
Interpolation
Demo

- Implement function bodies in `src/EDAF80/parametric_shapes.cpp`

```
bonobo::mesh_data parametric_shapes::createQuad(...);  
bonobo::mesh_data parametric_shapes::createSphere(...);  
bonobo::mesh_data parametric_shapes::createTorus(...); // Optional
```

- Look at `createCircleRing(...)` in the same file for guidance
- Make sure parameter definitions and ranges are correct
 - Circle ring: $0 \leq \theta < 2\pi, r_1 \leq r \leq r_2$
 - Sphere: $0 \leq \theta \leq 2\pi, 0 \leq \varphi \leq \pi$

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Interpolation

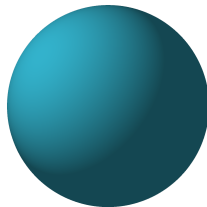
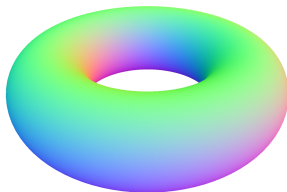
Linear
Cubic
Exercise 2-2

Assignment 2

Tessellation
Interpolation
Demo

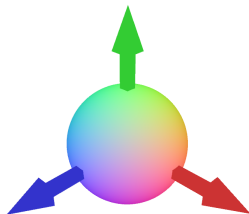
- Colourize, use the “Normals” shader to represent normals as RGB values
- Inspect illumination, is illumination consistent with the location of the light source?

DEBUGGING NORMALS



COLOURIZING NORMALS

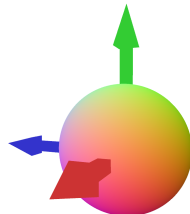
- Map from $[-1, 1]$ to $[0, 1]$
 - $(N \cdot 0.5) + 0.5$
- Example: Z axis $(0, 0, 1)$ becomes $(0.5, 0.5, 1)$
- Values are normalized: $(1, 1, 1) \mapsto (\frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}})$



$$(1, 1, 1) \mapsto (1, 1, 1)$$



$$(-1, -1, -1) \mapsto (0, 0, 0)$$



$$(1, 0, 0) \mapsto (1, 0.5, 0.5)$$

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Tessellation
Interpolation
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- Change cull mode: Disabled, Back faces, Front faces
- Change polygon mode: Fill, Line, Point
- Change shaders: Fallback, Diffuse, Normal, Tangent, Bitangent, Texture coords

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Linear
Cubic
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Assignment 2

Tessellation
Interpolation
Demo

- Implement linear and cubic interpolation
- Implement function bodies in `src/EDAF80/interpolation.cpp`

```
glm::vec3 interpolation::evalLERP(...);  
glm::vec3 interpolation::evalCatmullRom(...);
```

- Test with just 2 (LERP) or 4 (cubic) points first
- Animate an object along the path using both function and the predefined control points
- `use_linear` and `catmull_rom_tension` variables are bound to the GUI and should be used

IMPLEMENTATION SKETCH

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Tessellation
Interpolation
Demo

```
// Init:
```

```
std::array<glm::vec3, N> control_points = { ... };
```

```
float path_pos = 0.0f;
```

```
float velocity = ...
```

```
// Main loop:
```

```
    int i = floor(path_pos);
```

```
// Pick indices for interpolation: i-1, i, i+1, i+2
```

```
// Make sure indices wrap: 0, 1, ..., N-1, 0, 1, ...
```

```
// Call interpolation function with points from control_points
```

```
path_pos += velocity;
```

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Assignment 2

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- Demo**

