

TIME ASSUMPTIONS  
&  
TIME ABSTRACTIONS

# TIME ASSUMPTIONS

- Previously: *asynchronous systems*.
- No timing assumptions.
- No physical clock.
- No bounds on process or communication delays.
- First a parenthesis ...

# LOGICAL TIME

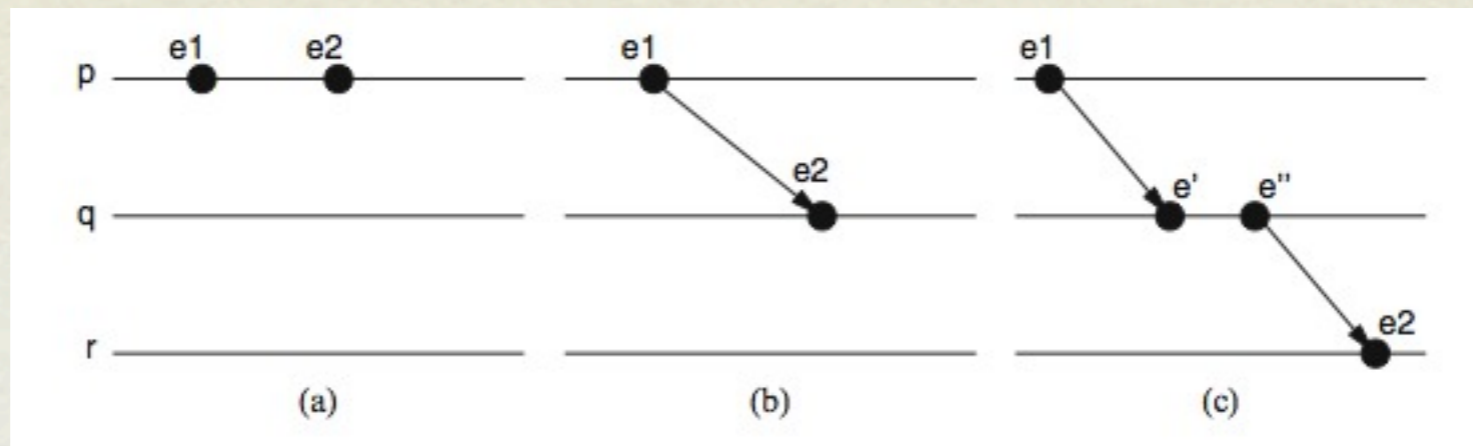
- Asynchronous systems.
- No physical clock!
- Time units: transmission and delivery of messages.

# LOGICAL TIME - ALGORITHM

Each process  $p$  keeps an integer called logical clock  $lp = 0$ .

1. Whenever an event occurs at process  $p$ , the logical clock  $lp$  is incremented by one unit.
2.  $p$  sends a message, adds timestamp  $t(e)$ .
3.  $p$  receives a message  $m$  with timestamp  $tm$ , sets  $lp := \max\{lp, tm\} + 1$ .

# LOGICAL TIME - CAUSALITY



Event  $e_1$  may have *potentially caused* event  $e_2$ ,  $e_1 \rightarrow e_2$  if:

(a)  $e_1$  and  $e_2$  occurred at the same process  $p$  and  $e_1$  occurred before  $e_2$ ;

(b)  $e_1$  corresponds to the transmission of a message  $m$  at a process  $p$  and  $e_2$  to the reception of  $m$  at some other process  $q$ ; or

(c) there exists some event  $e'$ , such that  $e_1 \rightarrow e'$  and  $e' \rightarrow e_2$ .

# SYNCHRONOUS SYSTEM

*Synchronous computation:* known upper bound on process delays.

AND

*Synchronous communication:* known upper bound on communication delays.

ALTERNATIVELY ONLY

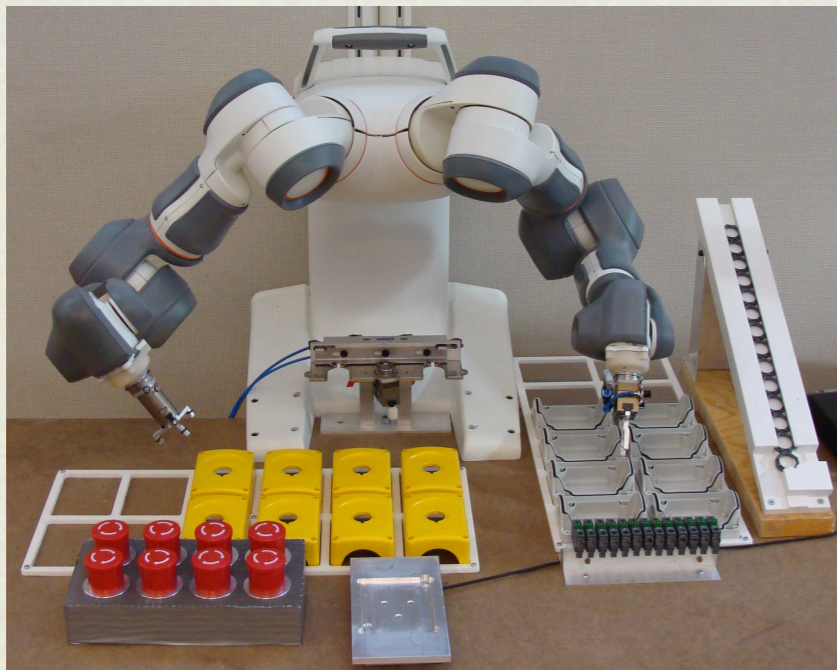
*Synchronous physical clocks:* local physical clocks + upper bound on deviation from global physical clock.

# SYNCHRONOUS SYSTEM - SERVICES

- Timed failure detection - heartbeats.
- Measure of transit delays.
- Coordination based on time. *Lease*.
- Worst-case performance.
- Synchronized clocks. Time stamp events + order (within sync precision).

# PROBLEMS

- *Coverage:* When the timing assumptions hold.



Controlled network load ...



reddit is under heavy load right now

Source: screenshot reddit.com

... worst case scenario.



# PARTIAL SYNCHRONY

- Periodically overloaded.
- No bound on the period that is asynchronous.
- After some time the timing assumptions hold “forever”.
- Eventually they will hold!

# ABSTRACTING TIME

- Add the timing assumptions to ...
- ... links and processes? Messy.
- Introduce: *failure detection!*
- Crash: heartbeats.

# PERFECT FAILURE DETECTION

- Timeouts:  $2 \times$  transmission time + worst-case process time.
- No response? Crash!
- Final judgement.

# PERFECT FAILURE DETECTION

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**Module 2.6:** Interface and properties of the perfect failure detector

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**Module:**

**Name:** PerfectFailureDetector, **instance**  $\mathcal{P}$ .

**Events:**

**Indication:**  $\langle \mathcal{P}, \text{Crash} \mid p \rangle$ : Detects that process  $p$  has crashed.

**Properties:**

**PFD1:** *Strong completeness:* Eventually, every process that crashes is permanently detected by every correct process.

**PFD2:** *Strong accuracy:* If a process  $p$  is detected by any process, then  $p$  has crashed.

to have crashed




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**Algorithm 2.5:** Exclude on Timeout

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**Implements:**PerfectFailureDetector, **instance**  $\mathcal{P}$ .**Uses:**PerfectPointToPointLinks, **instance**  $pl$ .**upon event**  $\langle \mathcal{P}, \text{Init} \rangle$  **do** $alive := \Pi$ ; $detected := \emptyset$ ; $starttimer(\Delta)$ ;

Large enough so that every process can send  
and deliver a heartbeat to all.

**upon event**  $\langle \text{Timeout} \rangle$  **do****forall**  $p \in \Pi$  **do****if**  $(p \notin alive) \wedge (p \notin detected)$  **then** $detected := detected \cup \{p\}$ ;**trigger**  $\langle \mathcal{P}, \text{Crash} \mid p \rangle$ ;**trigger**  $\langle pl, \text{Send} \mid p, [\text{HEARTBEATREQUEST}] \rangle$ ; $alive := \emptyset$ ; $starttimer(\Delta)$ ;

New heartbeats are triggered

**upon event**  $\langle pl, \text{Deliver} \mid q, [\text{HEARTBEATREQUEST}] \rangle$  **do****trigger**  $\langle pl, \text{Send} \mid q, [\text{HEARTBEATREPLY}] \rangle$ ;**upon event**  $\langle pl, \text{Deliver} \mid p, [\text{HEARTBEATREPLY}] \rangle$  **do** $alive := alive \cup \{p\}$ ;

# LEADER ELECTION

- Detect *living* process -> *Leader*.
- Leader that coordinates the others.
- Only for crash-stop!
- Useful for backup processes.

# LEADER ELECTION

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## Module 2.7: Interface and properties of leader election

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### Module:

**Name:** LeaderElection, **instance** *le*.

### Events:

**Indication:**  $\langle le, Leader \mid p \rangle$ : Indicates that process  $p$  is elected as leader.

### Properties:

**LE1: Eventual detection:** Either there is no correct process, or some correct process is eventually elected as the leader.

**LE2: Accuracy:** If a process is leader, then all previously elected leaders have crashed.

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## Algorithm 2.6: Monarchical Leader Election

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### Implements:

LeaderElection, **instance**  $le$ .

### Uses:

PerfectFailureDetector, **instance**  $\mathcal{P}$ .

**upon event**  $\langle le, Init \rangle$  **do**

$suspected := \emptyset$ ;

$leader := \perp$ ;

**upon event**  $\langle \mathcal{P}, Crash \mid p \rangle$  **do**

$suspected := suspected \cup \{p\}$ ;

**upon**  $leader \neq \text{maxrank}(\Pi \setminus suspected)$  **do**

$leader := \text{maxrank}(\Pi \setminus suspected)$ ;

**trigger**  $\langle le, Leader \mid leader \rangle$ ;

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#1



Source: [http://en.wikipedia.org/wiki/File:King\\_Carl\\_XVI\\_Gustaf\\_at\\_National\\_Day\\_2009\\_Cropped.png](http://en.wikipedia.org/wiki/File:King_Carl_XVI_Gustaf_at_National_Day_2009_Cropped.png)

#2



Source: [http://en.wikipedia.org/wiki/File:Crown\\_Princess\\_Victoria.jpg](http://en.wikipedia.org/wiki/File:Crown_Princess_Victoria.jpg)



# EVENTUAL FAILURE DETECTION

- Partial synchronous systems.
- False suspicions.
- Change judgement.
- Small timeouts -> increased.
- After increased timeouts -> system synchronous.



Source: <http://en.wikipedia.org/wiki/File:Noel-coypel-the-resurrection-of-christ-1700.jpg>

# EVENTUAL FAILURE DETECTION

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**Module 2.8:** Interface and properties of the eventually perfect failure detector

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**Module:**

**Name:** EventuallyPerfectFailureDetector, **instance**  $\diamond\mathcal{P}$ .

**Events:**

**Indication:**  $\langle \diamond\mathcal{P}, Suspect \mid p \rangle$ : Notifies that process  $p$  is suspected to have crashed.

**Indication:**  $\langle \diamond\mathcal{P}, Restore \mid p \rangle$ : Notifies that process  $p$  is not suspected anymore.

**Properties:**

**EPFD1:** *Strong completeness:* Eventually, every process that crashes is permanently suspected by every correct process.

**EPFD2:** *Eventual strong accuracy:* Eventually, no correct process is suspected by any correct process.

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**Algorithm 2.7: Increasing Timeout**

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**Implements:**

EventuallyPerfectFailureDetector, instance  $\diamond\mathcal{P}$ .

**Uses:**

PerfectPointToPointLinks, instance  $pl$ .

**upon event**  $\langle \diamond\mathcal{P}, \text{Init} \rangle$  **do**

*alive* :=  $\Pi$ ;  
*suspected* :=  $\emptyset$ ;  
*delay* :=  $\Delta$ ;  
starttimer(*delay*);

**upon event**  $\langle \text{Timeout} \rangle$  **do**

**if**  $alive \cap suspected \neq \emptyset$  **then**

*delay* := *delay* +  $\Delta$ ;

**forall**  $p \in \Pi$  **do**

**if**  $(p \notin alive) \wedge (p \notin suspected)$  **then**

*suspected* := *suspected*  $\cup$   $\{p\}$ ;

**trigger**  $\langle \diamond\mathcal{P}, \text{Suspect} \mid p \rangle$ ;

**else if**  $(p \in alive) \wedge (p \in suspected)$  **then**

*suspected* := *suspected*  $\setminus$   $\{p\}$ ;

**trigger**  $\langle \diamond\mathcal{P}, \text{Restore} \mid p \rangle$ ;

**trigger**  $\langle pl, \text{Send} \mid p, [\text{HEARTBEATREQUEST}] \rangle$ ;

*alive* :=  $\emptyset$ ;

starttimer(*delay*);

**upon event**  $\langle pl, \text{Deliver} \mid q, [\text{HEARTBEATREQUEST}] \rangle$  **do**

**trigger**  $\langle pl, \text{Send} \mid q, [\text{HEARTBEATREPLY}] \rangle$ ;

**upon event**  $\langle pl, \text{Deliver} \mid p, [\text{HEARTBEATREPLY}] \rangle$  **do**

*alive* := *alive*  $\cup$   $\{p\}$ ;

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← Performance goes down.

# EVENTUAL LEADER ELECTION

- Living dead!
- Eventually correct processes elect the same leader.
- Crash-recovery.
- Two algorithms.

# EVENTUAL LEADER ELECTION

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**Module 2.9:** Interface and properties of the eventual leader detector

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**Module:**

**Name:** EventualLeaderDetector, **instance**  $\Omega$ .

**Events:**

**Indication:**  $\langle \Omega, Trust \mid p \rangle$ : Indicates that process  $p$  is trusted to be leader.

**Properties:**

**ELD1:** *Eventual accuracy:* There is a time after which every correct process trusts some correct process.

**ELD2:** *Eventual agreement:* There is a time after which no two correct processes trust different correct processes.

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## Algorithm 2.8: Monarchical Eventual Leader Detection

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### Implements:

EventualLeaderDetector, **instance**  $\Omega$ .

### Uses:

EventuallyPerfectFailureDetector, **instance**  $\diamond\mathcal{P}$ .

**upon event**  $\langle \Omega, \text{Init} \rangle$  **do**

*suspected* :=  $\emptyset$ ;

*leader* :=  $\perp$ ;

**upon event**  $\langle \diamond\mathcal{P}, \text{Suspect} \mid p \rangle$  **do**

*suspected* := *suspected*  $\cup$   $\{p\}$ ;

**upon event**  $\langle \diamond\mathcal{P}, \text{Restore} \mid p \rangle$  **do**

*suspected* := *suspected*  $\setminus$   $\{p\}$ ; ← New

**upon** *leader*  $\neq$   $\text{maxrank}(\Pi \setminus \text{suspected})$  **do**

*leader* :=  $\text{maxrank}(\Pi \setminus \text{suspected})$ ;

**trigger**  $\langle \Omega, \text{Trust} \mid \text{leader} \rangle$ ;

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**Algorithm 2.9:** Elect Lower Epoch

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**Implements:**EventualLeaderDetector, instance  $\Omega$ .**Uses:**FairLossPointToPointLinks, instance  $fl$ .**upon event**  $\langle \Omega, Init \rangle$  **do**

```
epoch := 0;
store(epoch);
candidates :=  $\emptyset$ ;
trigger  $\langle \Omega, Recovery \rangle$ ; // recovery procedure completes the initialization
```

**upon event**  $\langle \Omega, Recovery \rangle$  **do**

```
leader := maxrank( $\Pi$ );
trigger  $\langle \Omega, Trust \mid leader \rangle$ ;
delay :=  $\Delta$ ;
retrieve(epoch);
epoch := epoch + 1;
store(epoch);
forall  $p \in \Pi$  do
    trigger  $\langle fl, Send \mid p, [HEARTBEAT, epoch] \rangle$ ;
candidates :=  $\emptyset$ ;
starttimer(delay);
```


**upon event**  $\langle Timeout \rangle$  **do**

```
newleader := select(candidates);
if newleader  $\neq$  leader then
    delay := delay +  $\Delta$ ;
    leader := newleader;
    trigger  $\langle \Omega, Trust \mid leader \rangle$ ;
forall  $p \in \Pi$  do
    trigger  $\langle fl, Send \mid p, [HEARTBEAT, epoch] \rangle$ ;
candidates :=  $\emptyset$ ;
starttimer(delay);
```

**upon event**  $\langle fl, Deliver \mid q, [HEARTBEAT, ep] \rangle$  **do**

```
if exists  $(s, e) \in candidates$  such that  $s = q \wedge e < ep$  then
    candidates := candidates  $\setminus$   $\{(q, e)\}$ ;
candidates := candidates  $\cup$   $(q, ep)$ ;
```

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Note!

Select the one with highest rank,  
among those with lowest epoch.



Longer time

# BYZANTINE LEADER ELECTION

- Trust, but verify!
- Complain if wrong actions or too slow.
- Progressively more time to prove yourself.



# BYZANTINE LEADER ELECTION

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**Module 2.10:** Interface and properties of the Byzantine eventual leader detector

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**Module:**

**Name:** ByzantineLeaderDetector, **instance** *bld*.

**Events:**

**Indication:**  $\langle bld, Trust \mid p \rangle$ : Indicates that process *p* is trusted to be leader.

Can be byzantine!



**Request:**  $\langle bld, Complain \mid p \rangle$ : Receives a complaint about process *p*.

**Properties:**

Triggered by higher level algorithm

**BLD1: Eventual succession:** If more than *f* correct processes that trust some process *p* complain about *p*, then every correct process eventually trusts a different process than *p*.

**BLD2: Putsch resistance:** A correct process does not trust a new leader unless at least one correct process has complained against the previous leader.

**BLD3: Eventual agreement:** There is a time after which no two correct processes trust different processes.

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# BYZANTINE LEADER ELECTION

- Max  $f$  Byzantine processes.
- $N > 3f$ .
- $leader(r) = p$  when  $rank(p) = r \bmod N$ ,  $r \bmod N \neq 0$ .  
Otherwise  $q$ , such that  $rank(q) = N$ .
- More than  $2f$  complaints needed!
- When more than  $f$  complaints for a round, processes that haven't complained, do it!

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**Algorithm 2.10: Rotating Byzantine Leader Detection**

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**Implements:**ByzantineLeaderDetector, **instance** *bld*.**Uses:**AuthPerfectPointToPointLinks, **instance** *al*.**upon event**  $\langle bld, Init \rangle$  **do***round* := 1;*complainlist* :=  $[\perp]^N$ ;*complained* := FALSE;**trigger**  $\langle bld, Trust \mid leader(round) \rangle$ ;**upon event**  $\langle bld, Complain \mid p \rangle$  **such that**  $p = leader(round)$  **and**  
*complained* = FALSE **do***complained* := TRUE;**forall**  $q \in \Pi$  **do****trigger**  $\langle al, Send \mid q, [COMPLAINT, round] \rangle$ ;**upon event**  $\langle al, Deliver \mid p, [COMPLAINT, r] \rangle$  **such that**  $r = round$  **and**  
*complainlist*[*p*] =  $\perp$  **do***complainlist*[*p*] := COMPLAINT;**if**  $\#(complainlist) > f \wedge complained = FALSE$  **then***complained* := TRUE;**forall**  $q \in \Pi$  **do****trigger**  $\langle al, Send \mid q, [COMPLAINT, round] \rangle$ ;**else if**  $\#(complainlist) > 2f$  **then***round* := *round* + 1;*complainlist* :=  $[\perp]^N$ ;*complained* := FALSE;**trigger**  $\langle bld, Trust \mid leader(round) \rangle$ ;