

In the last lecture...

- ► Procedure Summaries
- ► IFDS algorithm
- ► IDE algorithm
- Path Sensitivity

Our Memory Modelling Until Now

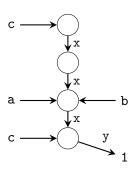
- Our analyses so far have considered:
 - ► Static Variables
 - ► Local (stack-dynamic) Variables
 - ► (Stack-dynamic) parameters

Missing: heap variables!

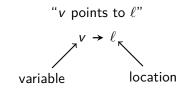
Example Program

Example

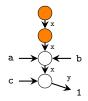
```
a = new();  // \( \)
a.x = null;  // \( \)
b = a;  // \( \)
b.x = new();  // \( \)
a.x.y = 1;  // \( \)
c = new();  // \( \)
c.x = new();  // \( \)
c.x.x = a;  // \( \)
c = a.x;  // \( \)
// A
```



Concrete Heap Graph



- ► Heap graph connects memory locations
- Represents all heap-allocated objects and their points-to relationships
- ► Edges labelled with field names
- ► Some objects not reachable from variables



Aliasing

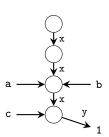
Example

```
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b.x = new();
a.x.y = 1;
c = new();
c.x = new();
c.x.x = a;
c = a.x;
// A
```

Aliases at // A:

▶ a and b represent the same object⇒ a and b are aliased

$$\mathtt{a} \stackrel{\mathit{alias}}{=\!\!\!=\!\!\!=} \mathtt{b}$$



Pointer Analysis



- ► Points-To Analysis:
 - ► Analyse *heap usage*
 - Which variables may/must point to which heap locations?

$$a \rightarrow \ell_0$$

- Alias Analysis:
 - ► Analyse address sharing
 - Which pair/set of variables may/must point to the same address?

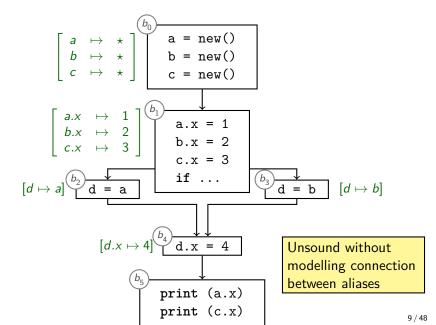
$$a \stackrel{alias}{==} b$$

Summary: Pointer Analysis

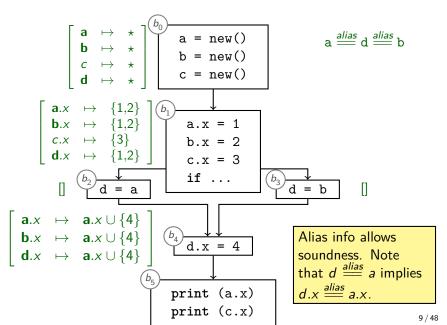
- Class of analyses to model dynamic heap allocation
- ▶ Points-To Analysis: computes mapping
 - ► From *variables*
 - ► To *pointees* (other variables)
 - ▶ More general than Alias Analysis
- ► Alias Analysis: computes
 - ▶ Sharing information between variables
 - ▶ Implicitly produced by points-to analysis

$$a \stackrel{alias}{=} b \iff a \rightarrow \ell \leftarrow b$$

Dataflow with Alias Information



Dataflow with Alias Information



Dataflow + Aliases

Aliasing affects shared fields:

$$a \stackrel{alias}{=} b \implies a.x \stackrel{alias}{=} b.x \text{ for all } x$$

- ► Exploiting aliasing knowledge:
 - ► Multiply *updates* for each alias:

$$\begin{bmatrix} \mathbf{a}.x & \mapsto & \mathbf{a}.x \cup \{4\} \\ \mathbf{b}.x & \mapsto & \mathbf{a}.x \cup \{4\} \\ \mathbf{d}.x & \mapsto & \mathbf{a}.x \cup \{4\} \end{bmatrix}$$

Multiply reads for each alias

$$\left[\begin{array}{ccc} \mathbf{a}.x & \mapsto & \mathbf{a}.x \cup \mathbf{b}.x \cup \mathbf{c}.x \cup \{4\} \end{array}\right]$$

- ▶ Replace aliased paths by single representative
 - Most efficient

Compute Aliases during Dataflow?

- Previoulsy: Dataflow analysis as analysis client of Alias analysis:
- ► Can use Dataflow Analysis to compute pointer analyses
- ► Caveat:
 - y.field = z
 - ► Transfer function updates y.field by z
 - ▶ Must extract both y, z from in_b to compute update
 - ► Non-distributive in practice

Summary

- ► Analysis client: user of analysis, often another analysis
 - ▶ E.g., *Type analysis* is client of *name analysis*
- ► Alias analysis helps make dataflow analysis more precise
 - ► Fields inherit aliasing:

$$a \stackrel{alias}{=} b \implies a.x \stackrel{alias}{=} b.x \text{ for all } x$$

- So if $a.x \stackrel{alias}{=} b.y$, then:
 - \triangleright a.x.z $\stackrel{alias}{=}$ b.y.z
 - \triangleright a.x.z.z $\stackrel{alias}{=}$ b.y.z.z
 - $ightharpoonup a.x.z.z.z \stackrel{alias}{==} b.y.z.z.z$ etc.
- Dataflow analysis can compute pointer analyses
 - ▶ Requires non-distributive framework for realistic languages

Concrete Heap Graphs (1/2)

Capturing the heap as a graph:

$$G_{\mathsf{CHG}} = \langle \mathit{MemLoc}, \rightarrow, \stackrel{-}{\rightarrow} \rangle$$

- ► G_{CHG} describes the *actual* heap contents
- ► MemLoc represents addressable memory locations
 - Named variables (a)
 - ► Unnamed variables (○)
- ► Heap size typically 'unbounded for all practical purposes'
- ▶ (→): Points-to relation from named variables

$$a \rightarrow \ell_0$$

ightharpoonup: Points-to relation from objects/arrays

$$\ell_1 \stackrel{f}{\rightarrow} \ell_1$$

$$\downarrow 0 \qquad \qquad \downarrow \ell_0 \qquad \qquad \downarrow \ell_1$$

Concrete Heap Graphs (2/2)

Direct points-to references:

$$(\rightarrow): Var \rightarrow MemLoc$$

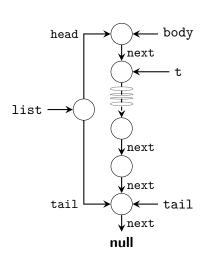
- ► Language difference:
 - ▶ Java: Var is set of global / local variables and pameters
 - ► Disjoint from MemLoc
 - ► C/C++: Var = MemLoc
 - ► Address-of operator (&) allows translating variable into *MemLoc*
- ▶ Points-to references via fields:

$$(\stackrel{-}{\rightarrow}): MemLoc \times Field \rightarrow MemLoc$$

- ► Field labels Field:
 - ► E.g., x in 'a.x' (Java) / 'a->x' (C/C++)
 - lacktriangle Array indices for 'a[10]' (i.e., $\mathbb{N}\subseteq \mathit{Field}$)

Example

```
proc makeList(len) {
  tail = new() //\Leftarrow
 tail.next = null //=
 body = tail //⇐
  while len > 0 {
   t = body //←
    body = new() //\Leftarrow
    body.next = t //←
   len = len - 1
  list = new()
                  //⇐
 list.head = body //⇐
  list.tail = tail //⇐
  return list
```



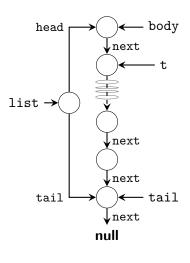
Managing Heap Graphs

- Size of Concrete Heap Graphs is unbounded
- ▶ Need summarisation technique to model heap
- Store-less heap models:
 - ▶ Do away with heap locations
 - ► Model heap exclusively via access paths

list.head.next.next

- Store-based heap models:
 - Keep heap locations explicit
 - Introduce Summary nodes that can describe multiple CHG nodes

Store-less Model



- Access path-based equivalences:
 - ▶ Must: list.tail = tail
 - ► **Must**: list.head ^{alias} body

 - ► May: body.next* = tail
- Use regular expressions to denote repetition
- ▶ body.next* = tail means:

body $\stackrel{alias}{=}$ tail body.next $\stackrel{alias}{=}$ tail body.next.next $\stackrel{alias}{=}$ tail

. . .

► For **May** or **Must** information

Store-based Model

► Concrete Heap Graph (CHG): graph of the program's reality

$$G_{\mathsf{CHG}} = \langle \mathit{MemLoc}, \rightarrow, \stackrel{-}{\rightarrow} \rangle$$

 Abstract Heap Graph (AHG): approximation of the program's reality

$$G_{\mathsf{AHG}} = \langle \mathcal{P}(\mathsf{MemLoc}),
ightharpoonup, \stackrel{-}{
ightharpoonup}
angle \ (
ightharpoonup) \; : \; \mathcal{P}(\mathsf{Var})
ightharpoonup \mathcal{P}(\mathsf{MemLoc}) \ (\stackrel{-}{
ightharpoonup}) \; : \; \mathcal{P}(\mathsf{MemLoc}) imes \mathcal{P}(\mathsf{Field})
ightharpoonup \mathcal{P}(\mathsf{MemLoc})$$

- ▶ Key idea: AHG is finite graph that summarises CHG
- ► Soundness via:

► Technique: *Summary nodes*

Summary Nodes and Edges

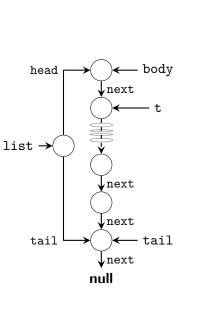
Notation:

- ▶ Abstract node *N* ⊂ *MemLoc*:
 - ► |N| = 1: precise: |N| > 1: summary: \bigcirc
- ▶ Consider edge $V \rightarrow L$:
 - ▶ |*V*| = 1: *precise*:
 - $V \longrightarrow L$
 - |V| > 1: summary: V --- ► 1

▶ Analogous for $(\stackrel{t}{\rightarrow})$ **Example:**

null head body list tail tail

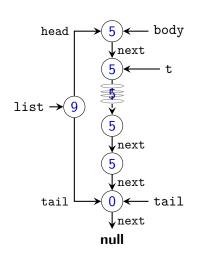
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Summaries from Allocation Sites

Example

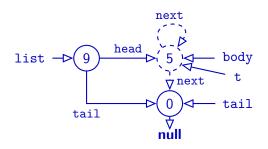
```
proc makeList(len) {
[0] tail = new()
[1] tail.next = null
[2] body = tail
[3] while len > 0 {
[4] t = body
[5] body = new()
[6] body.next = t
[7] len = len - 1
[8]
[9] list = new()
[10] list.head = body
[11] list.tail = tail
[12] return list
```



Summaries from Allocation Sites

Example

```
proc makeList(len) {
[0]
    tail = new()
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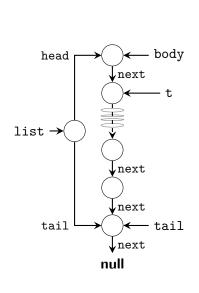
► Summarise *MemLoc* allocated at same program location

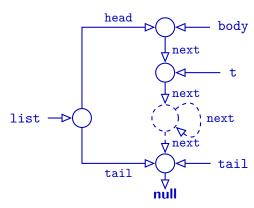
Summaries via k-Limiting

. . .

▶ *k*-Limiting: bound size Examples: Limiting. . . Access path length Example (k=3): list.head.next list.head.next list.head.next.next ⇒ list.head.next* list.head.next.next.next ⇒ list.head.next* list.head.next.next.val ⇒ list.head.(val|next)* \blacktriangleright # of (\rightarrow) hops after named variable → # of nodes transitively reachable via (→) after named variable ▶ # of nodes in a loop / function body

Variable-Based Summaries





- ► Summarise *MemLoc* when not referenced by variables
- For May analyses: summarise nodes potentially pointed to by same set of variables

Other Summary Techniques

- ▶ General idea: Map $\mathcal{P}(MemLoc)$ to finite (manageable!) set
- ► Can combine different techniques for increased precision
- ▶ Other techniques: distinguish heap nodes by:
 - ▶ How many edges point to the node?
 - ▶ Is the node in a cycle?
 - ► What is the type of the node? (ArrayList, StringTokenizer, File, ...)

Design Considerations

- ▶ First goal remains: make output finite
- Useful for analysis clients
- Efficient to compute / represent
- ▶ When considering flow-sensitive models:
 - ▶ Different program locations will have different AHGs
 - ► Exploit sharing across program locations

Summary of Heap Summaries

- Heap size is unbounded, must summarise
- Store-less Models:
 - ▶ Use access paths to describe memory locations
 - ► Common in alias analysis
- Store-based Models:
 - Use Abstract Heap Graph for summarisation
 - Common for finding memory bugs
- Summarisation techniques:
 - Allocation-Site Based: summarise nodes allocated at same program point
 - ▶ k-Limiting: Set bound on some property P: no more than k
 Ps allowed
 - Variable-Based: summarise data not pointed to by variables or pointed to by the same variables (May analysis)
 - Many combinations / extensions conceivable

Pointer Operations in C and Java

Referencing

Create location:

Dereferencing

Access location:

Aliasing

Copy pointer:

\mathbf{C}

my_t *p = &var; p = malloc(8);

\mathbf{C}

- read int x = *ptr;
x = ptr2->fld;
- write -

\mathbf{C}

my_t *pa;
pa = pb;

Java

A = new A()

Java

*ptr = x; ptr2->fld = x;

- read int x = a.f;
- write a.f = x;

Java

A a = b;

Pointer Operations

- ► Three principal pointer operations:
 - ► Referencing:
 - $\triangleright v := address-of(...)$
 - ► Create location ℓ
 - ▶ Introduce $v \rightarrow \ell$
 - ► Dereferencing:
 - $\triangleright x := v.f$
 - ightharpoonup Access existing location ℓ
 - Aliasing:
 - ▶ Pointer/reference variables v_1 , v_2
 - $V_2 := v_1$
 - $ightharpoonup v_1
 ightharpoonup \ell \iff v_2
 ightharpoonup \ell$

Summary

▶ Points-to anaysis: approximate 'v points to location ℓ '

$$V \rightarrow \ell$$

- Analysis must consider:
 - ▶ **Referencing**: taking location
 - ▶ **Dereferencing**: accessing object at location
 - ▶ Aliasing: copying location
- ▶ Locations ℓ may model different parts of memory:
 - Static variables: uniquely defined
 - ► Stack-dynamic variables: zero or more copies (recursion!)
 - Heap-dynamic variables:zero or more copies without variable names attached

Steensgaard's Points-To Analysis¹

- ► Fast: $O(n\alpha(n,n))$ over variables in program
- ▶ Developed to deal with large code bases at AT&T
- Sacrifices Precision
- ► Equality-based
- Intuition:
 Whenever two variables could point to the same memory location, treat them as globally equal

Steensgard: Pointer Operations

- ▶ Recall C pointer semantics:
 - ▶ &a: Address of a
 - ▶ *a: Object pointed to by a
 - ► Converse operators: *(&a) = a

Steensgard's analysis considers four cases:

	С	Java
Referencing	a = &b	a = new A()
Aliasing	a = b	a = b
Dereferencing read	a = *b	a = b.f
Dereferencing write	*a = b	a.f = b

Constraint Collection

- 'Points-to-set': pts(v) approximates $\{\ell|v \rightarrow \ell\}$
 - ▶ Corresponds to $\{\ell|v \rightarrow \ell\}$
- ▶ For each statement in program:
 - ▶ If **Referencing** (a = &b):

$$\ell_b \in \textit{pts}(a)$$

▶ If Aliasing (a = b):

$$pts(a) = pts(b)$$

▶ If Dereferencing read (a = *b):

for each
$$\ell \in \mathit{pts}(b) \implies \mathit{pts}(a) = \mathit{pts}(\ell)$$

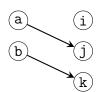
▶ If Dereferencing write (*a = b):

for each
$$\ell \in \mathit{pts}(\mathtt{a}) \implies \mathit{pts}(\mathtt{b}) = \mathit{pts}(\ell)$$

```
\begin{array}{lll} \mathbf{x} = \&\mathbf{y} & \ell_{\mathbf{y}} \in \mathit{pts}(\mathbf{x}) \\ \mathbf{x} = \mathbf{y} & \mathit{pts}(\mathbf{x}) = \mathit{pts}(\mathbf{y}) \\ \mathbf{x} = *\mathbf{y} & \text{for each } \ell \in \mathit{pts}(\mathbf{y}) \\ & \Longrightarrow \mathit{pts}(\mathbf{x}) = \mathit{pts}(\ell) \\ *\mathbf{x} = \mathbf{y} & \text{for each } \ell \in \mathit{pts}(\mathbf{x}) \\ & \Longrightarrow \mathit{pts}(\mathbf{y}) = \mathit{pts}(\ell) \end{array}
```

```
int i, j, k;
int* a = &i;
int* b = &k;
a = &j; //
int** p = &a;
int** q = &b;
p = q;
int* c = *q;
```

Actual:



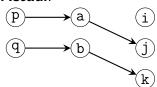
► Steensgaard:



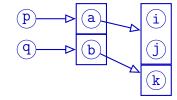
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► Actual:



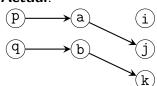
► Steensgaard:



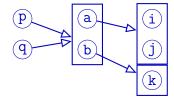
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int i, j, k; int* a = &i; int* b = &k; a = &j; int** p = &a; int** q = &b; p = q; // int* c = *q;

► Actual:



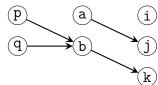
► Steensgaard:



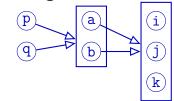
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► Actual:



► Steensgaard:

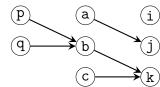


When merging: 'collapse' children (merge recursively)

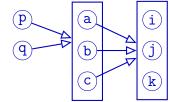
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```

int i, j, k; int* a = &i; int* b = &k; a = &j; int** p = &a; int** q = &b; p = q; int* c = *q; //

Actual:



► Steensgaard:



When merging: 'collapse' children (merge recursively)

Constraint Representation & Solving

- $\hat{v} \in \mathcal{P}(\textit{MemLoc})$: set of possible locations of variable v
- ▶ Represent with UNION-FIND data structure (efficient union)
- ► Collapse child nodes when merging
- ► Implementing Referencing (a = &b)
 - ightharpoonup pts(\widehat{a}).union(\widehat{b})
- ► Implementing Aliasing (a = b)
 - $ightharpoonup pts(\widehat{a}).union(pts(\widehat{b}))$
- Implementing Dereferencing (*a = b)
 - ▶ $pts(pts(\widehat{a})).union(pts(\widehat{b}))$

Result is immediate: no further analysis needed

Summary

- Points-to sets pts(v) serve as abstraction over addresses that v can point to
- Steensgaard's points-to analysis:
 - ▶ Insensitive to flow, context, fields, ...
- Steensgaard's analysis in practice:
 - ► Highly efficient
 - Imprecise

Andersen's Points-To Analysis²

- Asymptotic performance is $O(n^3)$
- ▶ More precise than Steensgaard's analysis
- ► Subset-based (a.k.a. inclusion-based)
- ▶ Popular as basis for current points-to analyses

Collecting Constraints

- Collect constraints, resolve as needed
- ▶ For each statement in program, we record:
 - ▶ If **Referencing** (a = &b):

$$pts(a)\supseteq\{\ell_b\}$$

▶ If Aliasing (a = b):

$$pts(a) \supseteq pts(b)$$

▶ If Dereferencing read (a = *b):

$$pts(a) \supseteq pts(*b)$$

▶ If Dereferencing write (*a = b):

$$pts(*a) \supseteq pts(b)$$

Solving Constraints

- We have collected constraints:
 - 1 $pts(a) \subseteq pts(b)$
 - $pts(*a)\subseteq pts(b)$
 - $\exists pts(a) \subseteq pts(*b)$
- ▶ Also, we have initial points-to set elements: $\ell \in pts(a)$
- ▶ Build directed *inclusion graph* $G_I = \langle MemLoc, E \rangle$
- ▶ Edges $a \rightarrow b \in E$ iff one of:
 - $ightharpoonup pts(a) \subseteq pts(b)$
 - ▶ $a \in pts(v)$ and $pts(*v) \subseteq pts(b)$
 - ▶ $pts(a) \subseteq pts(*v)$ and $b \in pts(v)$
- While keeping in mind the following:
 - $lackbox{($\ell \in pts(a)$)}$ and $(a \rightarrow b \in E) \implies (\ell \in pts(b))$
 - ▶ Propagate ℓ along E

```
int i, j, k;
int* a = &i;
int* b = &k;
a = &j;
int** p = &a;
int** q = &b;
p = q;
int* c = *q;
```

Actual:

```
int i, j, k; //
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int* b = &k;
a = &j;
int** p = &a;
int** q = &b;
p = q;
int* c = *q;
```

Actual:

- (i)
- (j)
- (k)

- (i)
- (j
- (k)

int i, j, k; int* a = &i; // int* b = &k; a = &j; int** p = &a; int** q = &b; p = q; int* c = *q;

Actual:









int i, j, k; int* a = &i; int* b = &k; // a = &j; int** p = &a; int** q = &b; p = q; int* c = *q;

► Actual:





\mathbf{C}

```
int i, j, k;
int* a = &i;
int* b = &k;
a = &j; //
int** p = &a;
int** q = &b;
p = q;
int* c = *q;
```

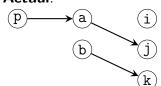
Actual:

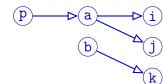




int i, j, k; int* a = &i; int* b = &k; a = &j; int** p = &a; // int** q = &b; p = q; int* c = *q;

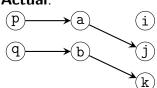
► Actual:

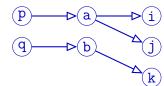




C int i, j, k; int* a = &i; int* b = &k; a = &j; int** p = &a; int** q = &b; // p = q; int* c = *q;

► Actual:

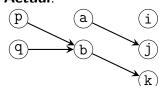


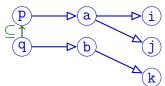


\mathbf{C}

```
int i, j, k;
int* a = &i;
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a = &j;
int** p = &a;
int** q = &b;
p = q; //
int* c = *q;
```

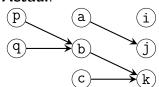
► Actual:

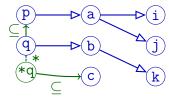




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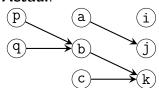
► Actual:

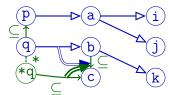




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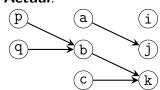
► Actual:



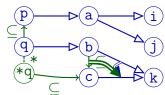


int i, j, k; int* a = &i; int* b = &k; a = &j; int** p = &a; int** q = &b; p = q; int* c = *q;

Actual:



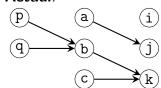
► Andersen:



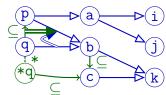
Andersen's algorithm must propagate along inclusion graph

```
int i, j, k;
int* a = &i;
int* b = &k;
a = &j;
int** p = &a;
int** q = &b;
p = q;
int* c = *q;
```

► Actual:



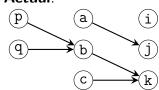
► Andersen:



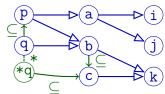
Andersen's algorithm must propagate along inclusion graph

int i, j, k; int* a = &i; int* b = &k; a = &j; int** p = &a; int** q = &b; p = q; int* c = *q;

Actual:



► Andersen:



Andersen's algorithm must propagate along inclusion graph

Complexity

- ▶ Complexity of graph closure: $O(n^3)$
- ► Traditional assumption about Andersen's analysis
- ▶ Recent work observes³: Close to $O(n^2)$ if:
 - 1 Few statements dereference each variable
 - 2 Control flow graphs not too complex
 - ▶ Both conditions are common in practical programs

Summary

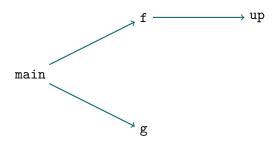
- Andersen's analysis:
 - Subset-based
 - Builds inclusion graph for propagating memory locations along subset constraints
 - $\triangleright O(n^3)$ worst-case behaviour
 - ▶ Closer to $O(n^2)$ in practice
 - ▶ More precise than Steensgaard's analysis
 - ▶ Less scalable than Steensgaard's analysis

The Call Graph

```
void f(char *s) {
                                for (char *p = s; *p; p++) {
                                    *p = (up)(*p);
                                puts(s);
int main(int argc,
         char *argv)
                            char up(char c) {
    if (argc > 1) {
                                if (c >= 'a' && c <= 'z') {
       (f(argv[0]);
                                    return c - ('a' - 'A'):
                                return c;
    return 0
                            void g(void) {
                                puts("Hello, World!");
```

The Call Graph

- $G_{call} = \langle P, E_{call} \rangle$
- ► Connects procedures from *P* via call edges from *E*_{call}
- ▶ 'Which procedure can call which other procedure?'
- ► Often refined to:
 'Which *call site* can call which procedure?'
- Used by program analysis to find procedure call targets



Finding Calls and Targets

```
class Main {
  public void
  main(String[] args) {
    A[] as = { new A() new B() };
    for (A a : as) {
        A a2 = a.f();
        print(a.g());
        print(a2.g());
    }
}
```

```
class A {
  public A
  f() { return new C(); }

public String
  g() { return "A"; }
}
```

```
class D extends A {
    @Override
    public String
    g() { return "D"; }
}
```

```
class C extends A {
   @Override
   public String
   g() { return "A"; }
```

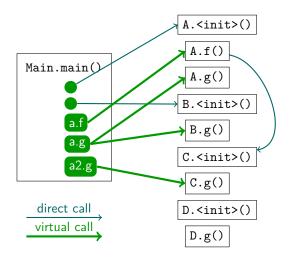
```
class B extends A {
   @Override
   public String
   g() { return "B"; }
}
```

Finding Calls and Targets

```
class Main {
  public void
 main(String[] args) {
                                              class A {
    A[] as \longrightarrow new A(), new B() };
                                                public A
    for (A = a.f as) {
                                               \rightarrowf() { return new C(); }
      A a2 = (a.f())
      ra.g(a.g())
                                                public String
                                               →g() { return "A"; }
      print(a2.g());
          a2.g
class D extends A {
                        class C extends A
                                                     class B extends A {
  Onverride
                           @Override
                                                       Onverride
                          public String
                                                       public String
 public String
 g() { return "D"; }
                          g() { return "A"; }
```

Dynamic Dispatch: Call Graph

Challenge: Computing the precise call graph:



Summary

- Call Graphs capture which procedure calls which other procedure
- ▶ For program analysis, further specialised to map:

Callsite \rightarrow Procedure

- ▶ Direct calls: straightforward
- ▶ Virtual calls (dynamic dispatch):
 - ▶ Multiple targets possible for call
 - Not straightforward

Callgraphs with Points-to Data

```
class A {
  public A
  f() {
    return new C();
  }
}
```

```
class B extends A {
  public A
  f() {
    return new A();
  }
}
```

```
class C extends A {
  public A
  f() {
   return new B();
  }
}
```

```
A a = new A();
a = a.f();
a = a.f();
```

- Precision of call graph affects quality of all interprocedural analyses
 - ▶ IFDS, IDE
 - ▶ Points-to analyses
- Idea: Use points-to analysis to determine dynamic type of objects
 - ▶ More precise virtual call resolution!
- Problem: Mutual dependency between call-graph and points-to analysis!

Review

- Pointer Analysis
 - ▶ Points-To Analysis
 - ► Alias Analysis
- ► Concrete Heap Graphs
- Abstract Heap Graphs
- Access Paths
- ► Heap Summarisation
 - ► Call-site
 - Variable-based
 - ► *k*-Limiting
- Steensgard's Analysis
- Andersen's Analysis
- Call graphs

To be continued...

Next week:

▶ Program Analysis with Datalog