# EDAF40 examination 2.5 hp

28th May 2018

14:00 - 19:00

WRITE ONLY ON ONE SIDE OF THE PAPER - the exams will be scanned in and only the front/ odd pages will be read.

**DO NOT WRITE WITH OTHER COLOUR THAN BLACK** - coloured text may disappear during scanning

**PUT YOUR ID AND PAGE NUMBER ON EACH PAGE YOU SUBMIT** - make sure that the amount of pages is equal to the amount you note on the front information page

WRITE CLEARLY - if we cannot read you we cannot grade you.

**PRELIMINARY AMOUNT OF POINTS: 6** (1+0.5+1+0.5+1+2)

{-A list of selected functions from the Haskell modules: Prelude Data.List Data.Mavbe Data.Char -} -- standard type classes class Show a where show :: a -> String class Eq a where (==), (/=) :: a -> a -> Bool class (Eq a) => Ord a where (<), (<=), (>=), (>) :: a -> a -> Bool max. min :: a -> a -> a class (Eq a, Show a) => Num a where (+), (-), (\*) :: a -> a -> a :: a -> a negate :: a -> a abs, signum fromInteger :: Integer -> a class (Num a. Ord a) => Real a where toRational :: a -> Rational class (Real a, Enum a) = Integral a where quot, rem :: a -> a -> a div, mod :: a -> a -> a toInteger :: a -> Integer class (Num a) => Fractional a where (/):: a -> a -> a fromRational :: Rational -> a class (Fractional a) => Floating a where exp, log, sgrt :: a -> a sin, cos, tan :: a -> a class (Real a. Fractional a) => RealFrac a where truncate, round :: (Integral b) => a -> b ceiling, floor :: (Integral b) => a -> b -- numerical functions even, odd :: (Integral a) => a -> Bool = n`rem` 2 == 0 even n = not . even odd -- monadic functions

sequence :: Monad m => [m a] -> m [a] sequence = foldr mcons (return [])

sequence\_ :: Monad m => [m a] -> m () sequence\_ xs = do sequence xs; return () -- functions on functions :: a -> a id x = x const :: a -> b -> a const x \_ = x (.) :: (b -> c) -> (a -> b) -> a -> c  $= \langle x - \rangle f(q x)$ f.g flip :: (a -> b -> c) -> b -> a -> c flip f x y = f y x(\$) :: (a -> b) -> a -> b f\$x = f x \_\_\_\_\_ -- functions on Bools data Bool = False | True (&&), (||) :: Bool -> Bool -> Bool True && x = xFalse && \_ = False True || \_ = True False || x = x not :: Bool -> Bool not True = False not False = True -- functions on Maybe data Maybe a = Nothing | Just a isJust :: Maybe a -> Bool isJust (Just a) = True isJust Nothing = False :: Maybe a -> Bool isNothing isNothing = not . isJust fromJust :: Maybe a -> a

maybeToList :: Maybe a -> [a] maybeToList Nothing = [] maybeToList (Just a) = [a]

= a

fromJust (Just a)

id

```
listToMaybe :: [a] -> Maybe a
listToMaybe [] = Nothing
listToMaybe (a:_) = Just a
```

-- a hidden goodie

instance Monad [] where return x = [x]xs >>= f = concat (map f xs) -- functions on pairs fst :: (a, b) -> a fst(x, y) = xsnd :: (a, b) -> b snd(x, y) = ycurry :: ((a, b) -> c) -> a -> b -> c curry f x y = f(x, y)uncurry :: (a -> b -> c) -> (a, b) -> c uncurry f p = f (fst p) (snd p)-- functions on lists map ::  $(a \rightarrow b) \rightarrow [a] \rightarrow [b]$ map f xs = [f x | x < -xs](++) :: [a] -> [a] -> [a] = foldr (:) ys xs xs ++ ys :: (a -> Bool) -> [a] -> [a] filter = [x | x < -xs, px]filter p xs :: [[a]] -> [a] concat = foldr (++) [] xss concat xss concatMap :: (a -> [b]) -> [a] -> [b] concatMap f = concat . map f head, last :: [a] -> a head (x: ) = x last [x] = x last (\_:xs) = last xs tail. init :: [a] -> [a] tail (\_:xs) = xs init [x] = [] init (x:xs) = x : init xs

:: [a] -> Bool null null [] = True null ( : ) = False length :: [a] -> Int length [] = 0 length ( :1) = 1 + length l:: [a] -> Int -> a (!!)(x:\_) !! 0 = x (:xs) !! n = xs !! (n-1)foldr ::  $(a \rightarrow b \rightarrow b) \rightarrow b \rightarrow [a] \rightarrow b$ foldr f z [] = 7 foldr f z (x:xs) = f x (foldr f z xs) foldl :: (a -> b -> a) -> a -> [b] -> a foldl f z [] = z foldl f z (x:xs) = foldl f (f z x) xs iterate :: (a -> a) -> a -> [a] iterate f x = x : iterate f (f x) repeat :: a -> [a] repeat x = xs where xs = x:xs :: Int -> a -> [a] replicate replicate n x = take n (repeat x) cycle :: [a] -> [a] cycle [] = error "Prelude.cycle: empty list" cycle xs = xs' where xs' = xs++xs' take, drop :: Int -> [a] -> [a] take n \_ | n <= 0 take \_ [] = [] = [] take n (x:xs) = x : take (n-1) xsdrop n xs | n <= 0 = xs drop [] = [] drop n (:xs) = drop (n-1) xs splitAt :: Int -> [a] -> ([a],[a]) = (take n xs, drop n xs) splitAt n xs takeWhile, dropWhile :: (a -> Bool) -> [a] -> [a] takeWhile p [] = [] takeWhile p (x:xs) = x : takeWhile p xs| p x l otherwise = [] dropWhile p [] = [] dropWhile p xs@(x:xs') = dropWhile p xs' l p x otherwise = xs

```
lines. words
                     :: String -> [String]
-- lines "apa\nbepa\ncepa\n" == ["apa","bepa","cepa"]
-- words "apa bepa\n cepa" == ["apa","bepa","cepa"]
unlines. unwords
                    :: [String] -> String
-- unlines ["apa","bepa","cepa"] == "apa\nbepa\ncepa"
-- unwords ["apa","bepa","cepa"] == "apa bepa cepa"
and, or
                     :: [Bool] -> Bool
and
                     = foldr (&&) True
or
                     = foldr (||) False
                     :: (a -> Bool) -> [a] -> Bool
any, all
                 = or . map p
any p
alĺ́p
                 = and map p
elem. notElem
                 :: (Eq a) => a -> [a] -> Bool
elemx
                 = any (== x)
                 = all (/= x)
notElem x
lookup
                 :: (Eq a) => a -> [(a,b)] -> Maybe b
lookup key [] = Nothing
lookup key ((x,y):xys)
     key == x = Just y
     otherwise = lookup key xys
                 :: (Num a) => [a] -> a
sum. product
                 = foldl (+) 0
sum
                 = foldl (*) 1
product
maximum, minimum :: (Ord a) => [a] -> a
maximum []
                 = error "Prelude.maximum: empty list"
                 = foldl1 max xs
maximum xs
                 = error "Prelude.minimum: empty list"
minimum []
minimum xs
                 = foldl1 min xs
                 :: [a] -> [b] -> [(a,b)]
zip
zip
                 = zipWith (.)
zipWith
                 :: (a->b->c) -> [a]->[b]->[c]
zipWith z (a:as) (b:bs)
                 = z a b : zipWith z as bs
zipWith _ _ _
                 = []
                 :: [(a,b)] -> ([a],[b])
unzip
unzip
                 = foldr (\(a,b) ~(as,bs) -> (a:as,b:bs)) ([],[])
nub
                 :: (Eq a) => [a] -> [a]
nub []
                 = []
nub (x:xs)
                 = x : nub [y | y < -xs, x / = y]
delete
                 :: Eq a => a -> [a] -> [a]
delete y []
                 = []
```

```
delete y (x:xs) = if x == y then xs else x : delete y xs
())
                 :: Eq a => [a] -> [a]-> [a]
                 = foldl (flip delete)
())
                 :: Eq a => [a] -> [a] -> [a]
union
                 = xs ++ (ys \setminus xs)
union xs ys
                         :: Eq a => [a] -> [a]-> [a]
intersect
intersect xs ys
                         = [ x | x <- xs, x `elem` ys ]
intersperse
                         :: a -> [a] -> [a]
-- intersperse 0 [1,2,3,4] == [1,0,2,0,3,0,4]
transpose
                         :: [[a]] -> [[a]]
-- transpose [[1,2,3],[4,5,6]] == [[1,4],[2,5],[3,6]]
partition
                          :: (a -> Bool) -> [a] -> ([a],[a])
partition p xs
                         = (filter p xs, filter (not . p) xs)
aroup
                          :: Eq a => [a] -> [[a]]
-- group "aapaabbbeee"
                         == ["aa","p","aa","bbb","eee"]
isPrefixOf, isSuffixOf
                         :: Eq a => [a] -> [a] -> Bool
isPrefixOf []
isPrefixOf _ []
                         = True
                         = False
isPrefixOf(x:xs)(y:ys) = x == y \& isPrefixOf xs ys
isSuffixOf x y
                         = reverse x `isPrefixOf` reverse y
sort
                          :: (Ord a) => [a] -> [a]
sort
                         = foldr insert []
                         :: (0rd a) \Rightarrow a \Rightarrow [a] \Rightarrow [a]
insert
insert x []
                         = [x]
insert x (y:xs)
                         = if x <= y then x:y:xs else y:insert x xs
-- functions on Char
type String = [Char]
toUpper, toLower :: Char -> Char
-- toUpper 'a' == 'A'
-- toLower 'Z'
                  == 'z'
digitToInt
                  :: Char -> Int
-- digitToInt '8' == 8
intToDigit
                  :: Int -> Char
```

-- intToDigit 3 == '3'

:: Char -> Int

:: Int -> Char

ord

chr

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## Exam

### 1. Point-free notation (1p)

Rewrite the following two definitions into a point-free form (i.e.,  $f = \ldots$ ,  $g = \ldots$ ), using neither lambda-expressions nor list comprehensions nor enumeration nor where clause nor let clause:

f x y = (3 - y) / x g x y = [x z | z <- [1,3..y]]

### 2. Type derivation (0.5p)

Which type has the function g defined as

g xs = [f x | x <- xs, x > 3]

where f n = replicate n '+' ?

3. Type declarations (1p)

Explain the difference between type, newtype and data type declarations in Haskell.

4. **Programming** (0.5p)

Give an example of a function with type

(a -> b , [a]) -> [b]

5. List comprehension (1p)

A Pythagorean triad is a triple of integers (a,b,c) such that

 $a^2 + b^2 == c^2$ 

Define a function of **n** that will find all Pythagorean triads with  $a \le b \le c \le n$ . Express it using list comprehension.

### 6. **Programming** (2p)

A proposition is a boolean formula of one of the following forms:

- a variable name (a string)
- $p \wedge q$  (and)
- $p \lor q$  (or)
- $\neg p \pmod{1}$

where p and q are propositions (note recursiveness). For example,  $p \vee \neg p$  is a proposition.

- (a) Design a data type Proposition to represent propositions.
- (b) Define a function

vars :: Proposition -> [String]

which returns a list of the variables in a proposition. Make sure each variable appears only once in the list you return. E.g., for (your representation of)  $p \lor \neg p$  it should return p.

(c) Suppose you are given a list of variable names, and their values of type Bool, for example, [("p",True),("q",False)]. Define a function

truthValue :: Proposition -> [(String,Bool)] -> Bool

which determines whether the proposition is true when the variables have the values given as second argument. E.g., for (your representation of)  $p \vee \neg p$  and [("p", True)] it should return True.

(d) Define a function

tautology :: Proposition -> Bool

which returns true if the proposition holds for all values of the variables appearing in it. E.g., for (your representation of)  $p \vee \neg p$  it should return **True**.

# Good Luck!