



# Photon Mapping



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# Outline

- Photon Mapping (ch. 14 in textbook)
  - Progressive
  - Stochastic

# How to make light sampling faster?

- Path tracing converges slowly
- Shot rays from the light
  - Bidirectional path tracing
  - Metropolis Light Transport
    - Find a path to the light
    - ... then reuse a modified version
- Photon Mapping

# Photon mapping

## State-of-the-art in GI

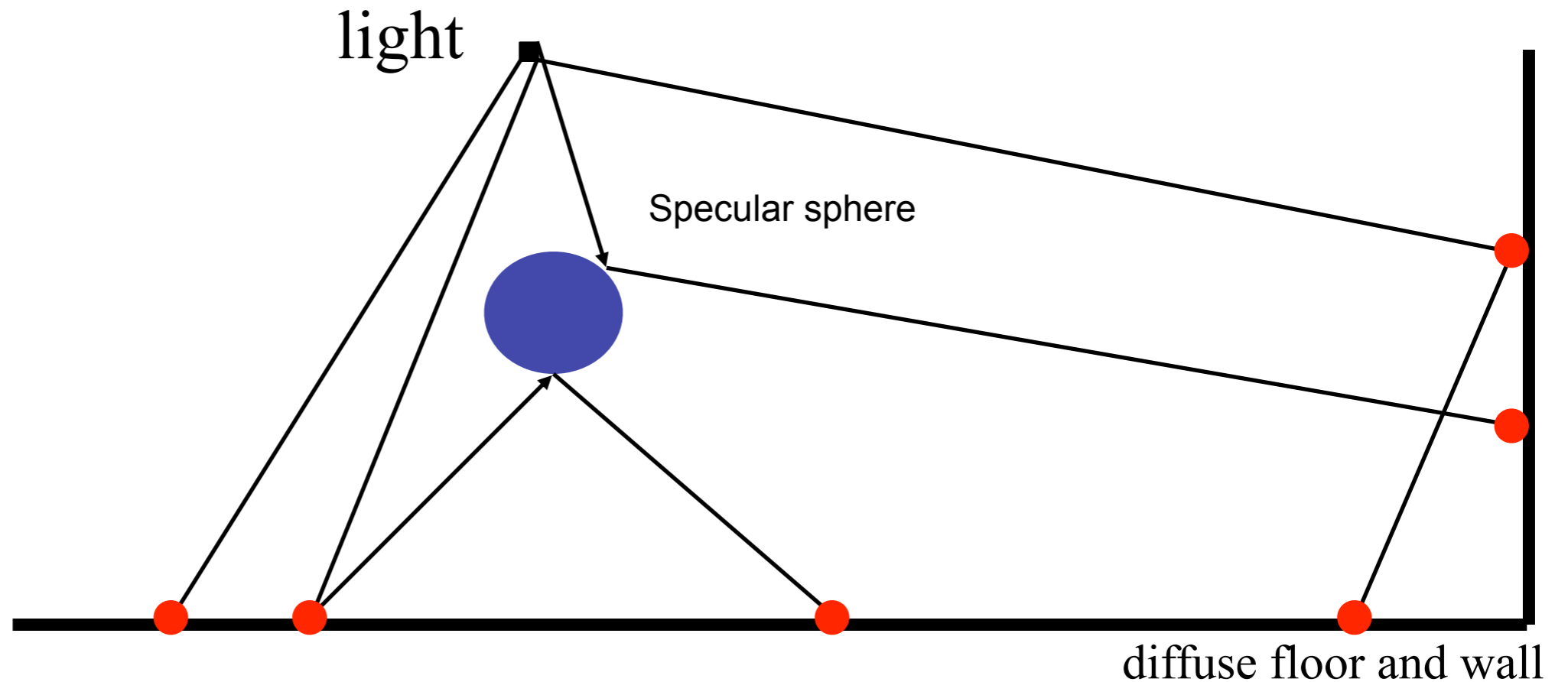
- Developed by Henrik Wann Jensen (started 1993)
- A clever two-pass algorithm:
  - 1: Shoot photons from light sources, and let them bounce around in the scene, and store them where they land
  - 2: "Ray tracing"-like pass from the eye, but gather the photons from the previous pass
- Advantages:
  - Fast
  - Handles arbitrary geometry (as does path tracing)
  - All global illumination effects can be seen
  - Little noise

# The first pass: Photon tracing

- Store illumination as points (photons) in a "photon map" data structure
- In the first pass: **photon tracing**
  - Emit photons from light sources
  - Trace them through scene
  - Store them in photon map data structure
- More details:
  - Then use Russian roulette to find out whether the photon is absorbed or reflected
  - If a photon is absorbed, by a surface (that has a diffuse component), store the photon in photon map
  - If reflected, then shoot photon in new random direction

# Photon tracing

● This type of marker is a stored photon



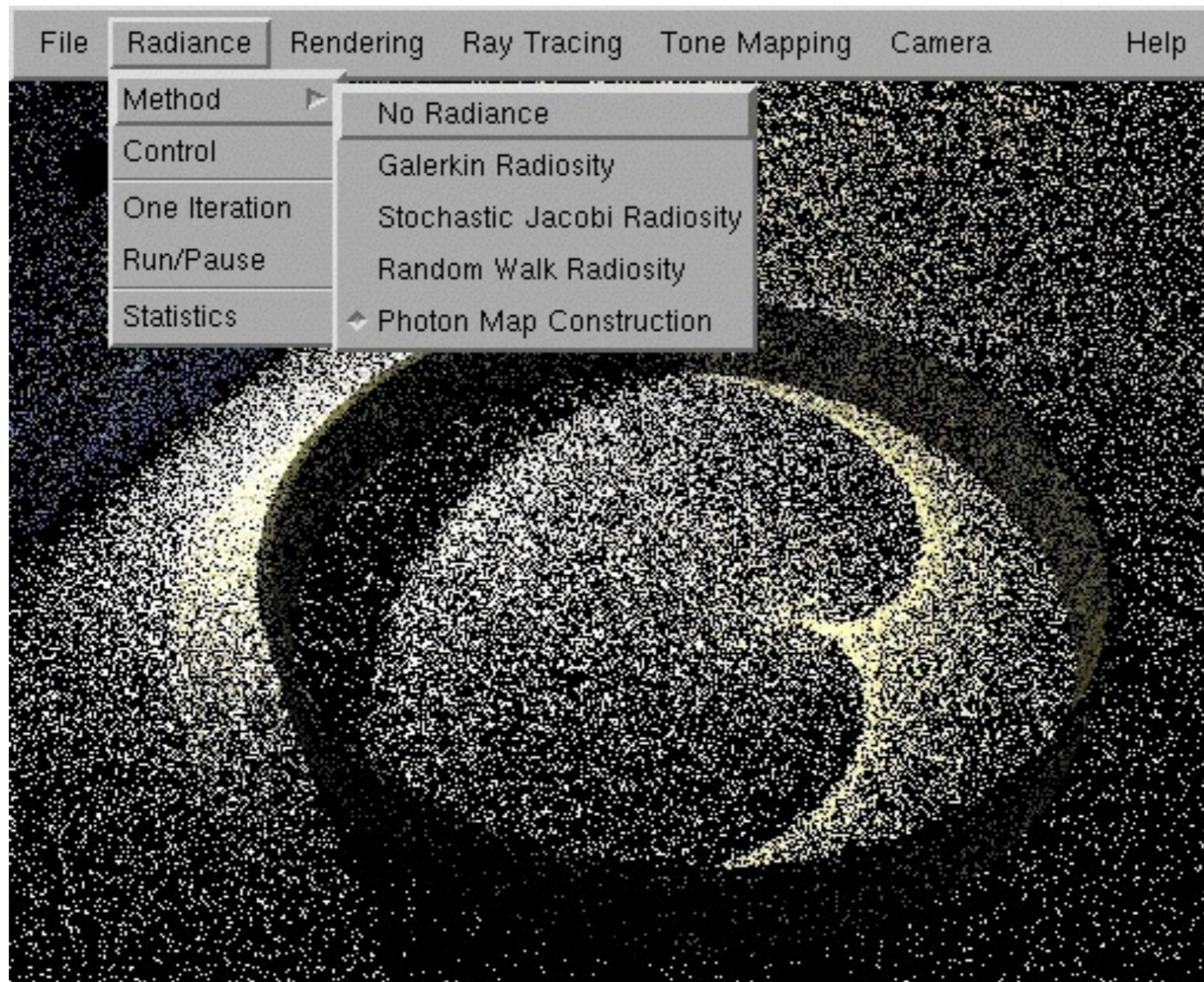
- Should not store photon at specular surfaces, because these effects are view dependent
  - only diffuse effect is view independent
- Some diffuse photons are absorbed, some are scattered further
- A photon = the incoming illumination at a point

# The photon map data structure

- Keep them in a separate (from geometry) structure
- Store all photons in kD-tree
  - Essentially an axis-aligned BSP tree, but we must alter splitting axis:  $x, y, z, x, y, z, x, y, z$ , etc.
  - Each node stores a photon
  - Needed because the algorithm needs to locate the  $n$  closest photons to a point
- A photon:
  - float  $x, y, z$ ;
  - char  $power[4]$ ; // RGBE, with more accuracy using shared Exponent
  - char  $phi, theta$ ; // compact representation of incoming direction
  - short  $flag$ ; // used by KD-tree (stores which plane to split)
- Create balanced KD-tree – simple, done once.
- Photons are stored linearly in memory:
  - Parent node at index:  $p$ , left child at:  $2p$ , right child:  $2p+1$

# What does it look like?

- Stored photons displayed:





# Density estimation

- The density of the photons indicate how much light that point receives
- Radiance is the term for what we display at a pixel
- Rather complex derivation skipped (see Jensen's book)...
- Reflected radiance at point  $\mathbf{x}$ :

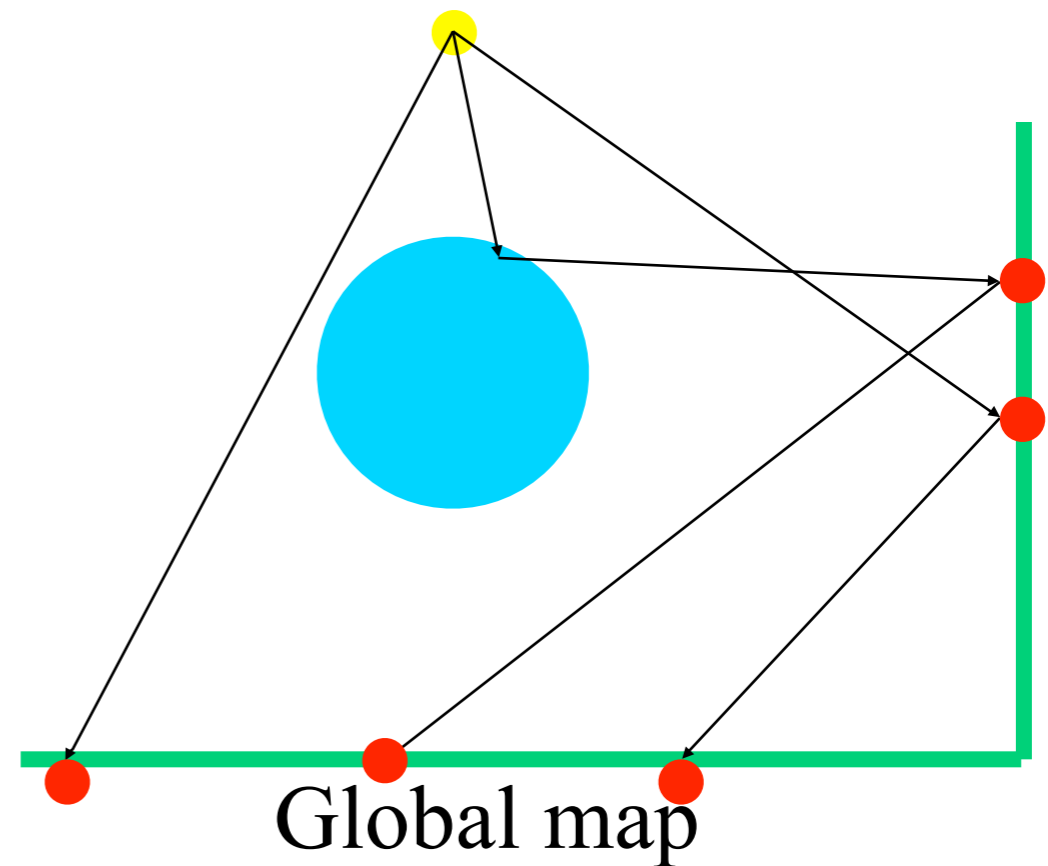
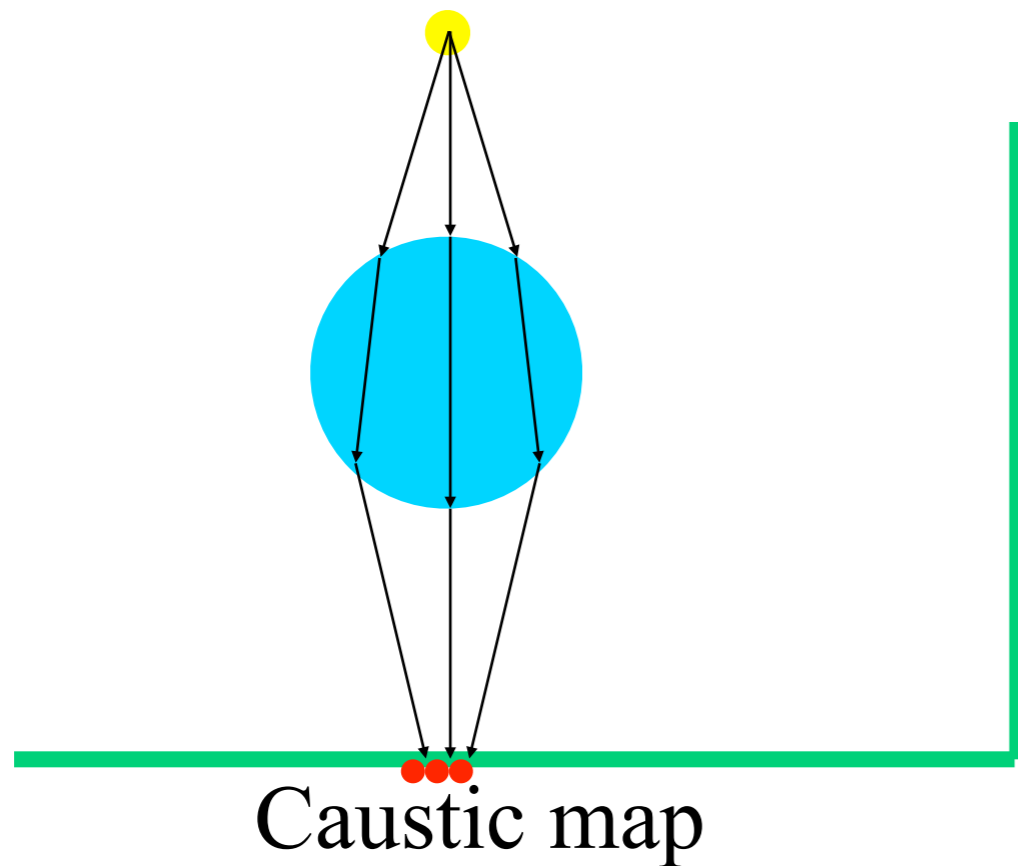
$$L(\mathbf{x}, \omega) \approx \frac{1}{\pi r^2} \sum_1^n f_r(\mathbf{x}, \omega_p \leftrightarrow \omega) \Phi_p(\mathbf{x}, \omega_p)$$

- $L$  is radiance at  $\mathbf{x}$  in the direction of  $\omega$
- $r$  is radius of expanded sphere
- $\omega_p$  is the direction of the stored photon
- $\Phi_p$  is the stored power of the photon (flux)
- $f_r$  is the BRDF

# Two-pass algorithm

- Already said:
  - 1) Photon tracing, to build photon maps
  - 2) Rendering from the eye using photon maps
- Pass 1:
  - Use **two** photon maps
  - A **caustics photon map** (for caustics)
    - Reflected or refracted via a surface to a diffuse surface
    - Light transport notation: LS+D
  - A **global photon map** (for all illumination)
    - All photons that landed on diffuse surfaces
    - $L(S | D)^*D$

# Caustic map and global map

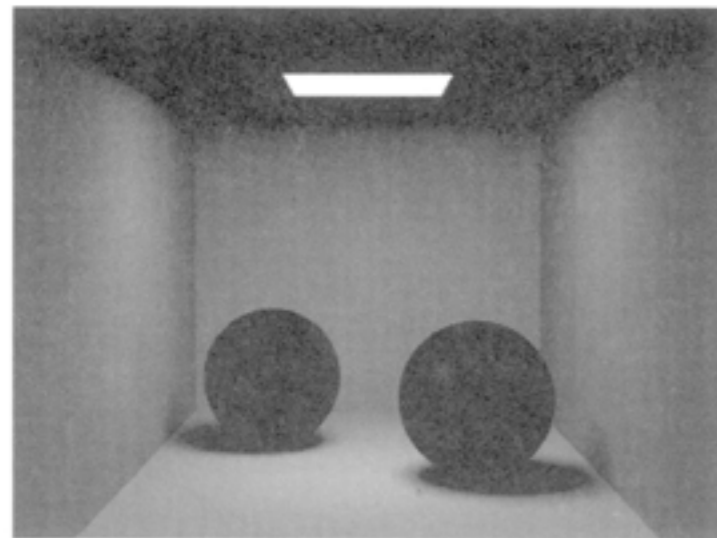


- Caustic map: send photons only towards reflective and refractive surfaces
  - Caustics is a high frequency component of illumination
  - Therefore, need many photons to represent accurately
- Global map - assumption: illumination varies more slowly

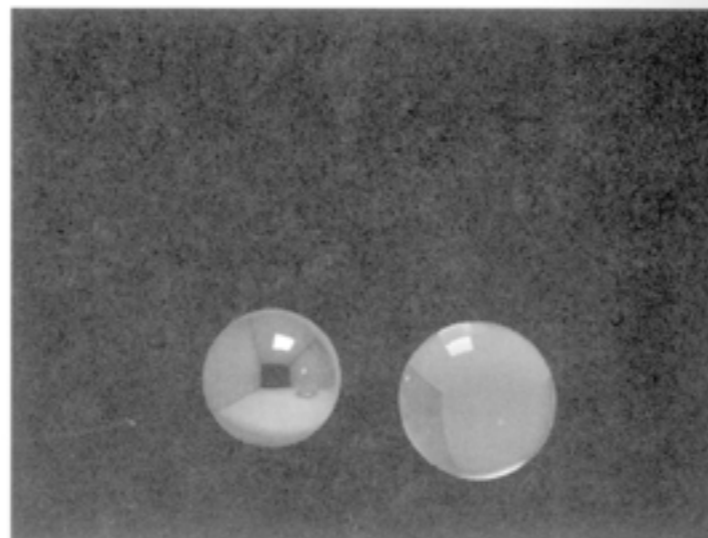
# Pass 2: Rendering using the photon map

- Render from the eye using a modified ray tracer
  - A number of rays are sent per pixel
  - Break up into fastest way to compute different terms
  - For each ray evaluate four terms
    - **Direct illumination** (light reaches a surface directly from light source)... may need to send many rays to area lights. Done using standard ray tracing.
    - **Specular reflection** (also evaluated using ray tracing, possibly, with many rays sent around the reflection direction)
    - **Caustics**: use caustics photon map
    - **Indirect illumination** (sample multiple diffuse reflections) (gives color bleeding): use the photon map for reflected rays.

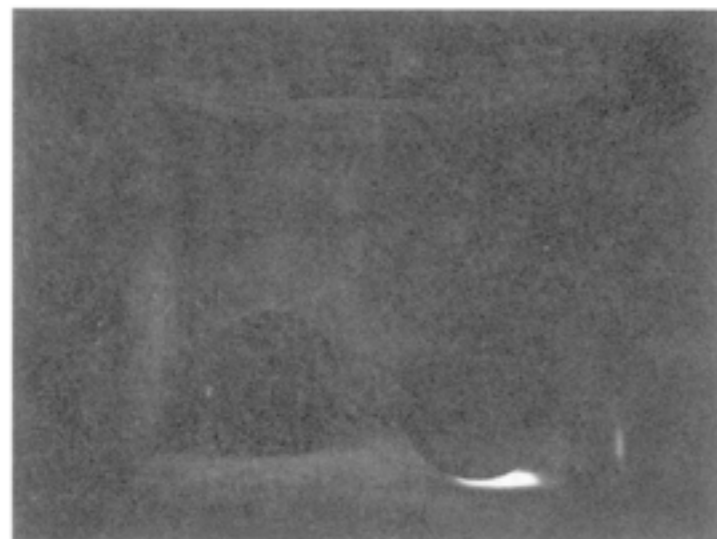
# Images of the four components



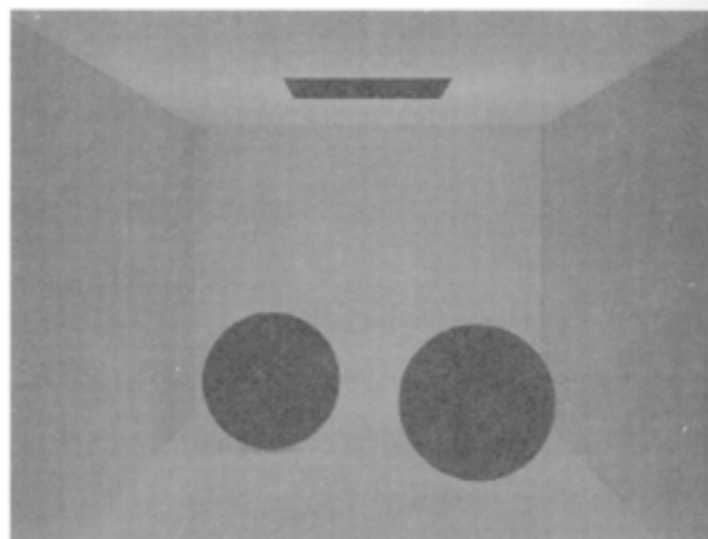
Direct illumination



Specular reflection

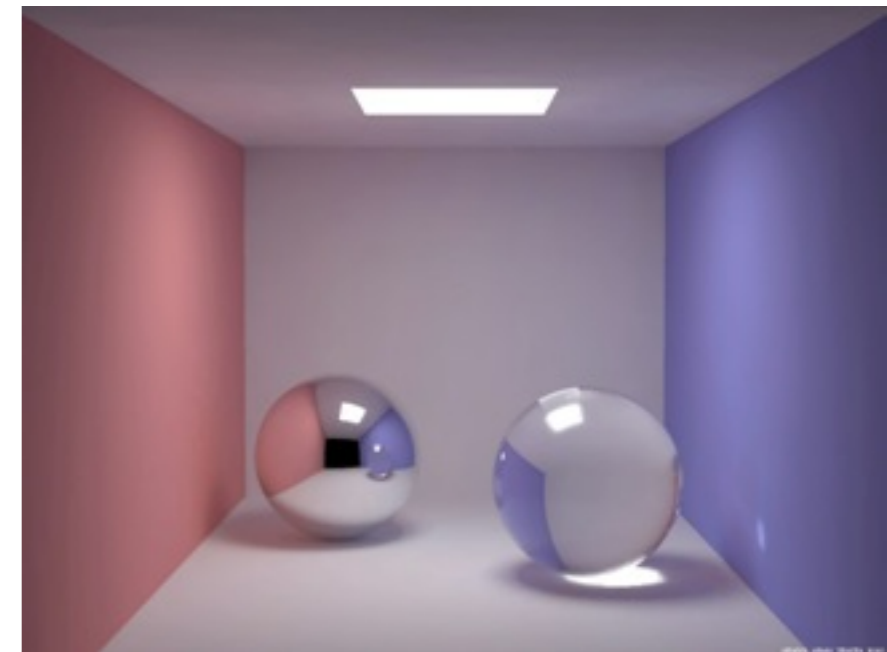


Caustics



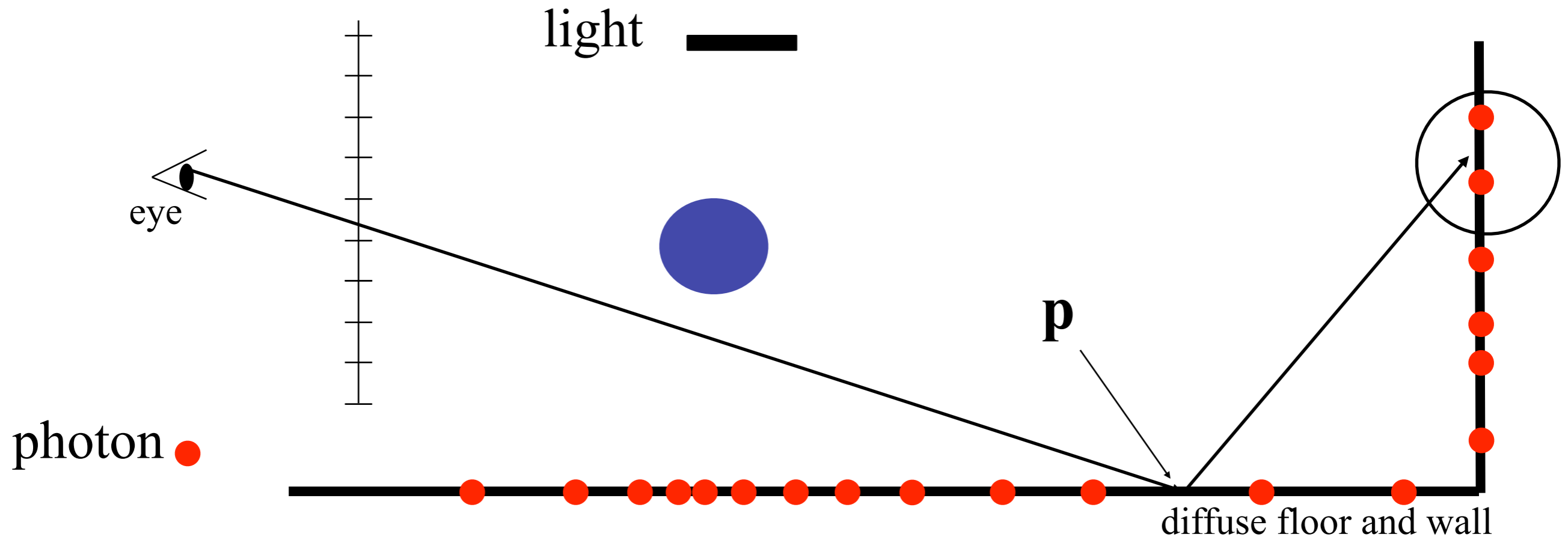
Indirect illumination

=



- These together solves the entire rendering equation!

# Indirect illumination: Use the photon map



- To evaluate indirect illumination at point  $p$ :
  - Send several random rays out from  $p$ , and grow spheres at contacts
  - May need several hundreds of rays to get good results.

# Locate $n$ nearest photons

given the photon map, a position  $x$  and a max search distance  $d^2$

this recursive function returns a heap  $h$  with the nearest photons.

Call with `locate_photons(1)` to initiate search at the root of the kd-tree

```
locate_photons( p ) {
  if ( 2p + 1 < number of photons ) {
    examine child nodes
    Compute distance to plane (just a subtract)
     $\delta$  = signed distance to splitting plane of node  $n$ 
    if (  $\delta < 0$  ) {
      We are left of the plane - search left subtree first
      locate_photons( 2p )
      if (  $\delta^2 < d^2$  )
        locate_photons( 2p + 1 )    check right subtree
    } else {
      We are right of the plane - search right subtree first
      locate_photons( 2p + 1 )
      if (  $\delta^2 < d^2$  )
        locate_photons( 2p )    check left subtree
    }
  }
  Compute true squared distance to photon
   $\delta^2$  = squared distance from photon  $p$  to  $x$ 
  if (  $\delta^2 < d^2$  ) {
    Check if the photon is close enough?
    insert photon into max heap  $h$ 
    Adjust maximum distance to prune the search
     $d^2$  = squared distance to photon in root node of  $h$ 
  }
}
```

from Fig4.10,  
photon mapping  
tutorial, "Advanced  
Global Illumination  
Using Photon  
Mapping",  
SIGGRAPH 2008

# More literature

- Photon Mapping Tutorial, “Advanced Global Illumination Using Photon Mapping”, SIGGRAPH 2008 course notes
- Great book on global illumination and photon mapping:
  - Henrik Wann Jensen, *Realistic Image Synthesis using Photon Mapping*, AK Peters, 2001.
- Check Henrik’s website:
  - <http://graphics.ucsd.edu/~henrik/>
  - ["Global Illumination using Photon Maps"](#)  
Henrik Wann Jensen  
In *"Rendering Techniques '96"*. Eds. X. Pueyo and P. Schröder. Springer-Verlag, pages 21-30, 1996



# Progressive Photon Mapping

LAB4

- Photon mapping limited by Photon Map
- Rearrange algorithm to remove limitation
- Progressively refine final image by tracing more photons
- image approaches correct solution

"Progressive Photon Mapping", T. Hachisuka, S. Ogaki and H.W. Jensen,  
ACM Transactions on Graphics (SIGGRAPH Asia 2008)

# Progressive Photon Mapping

LAB4

- 1st pass - find eye intersection positions
- 2nd pass - collect photons at intersection positions

## ■ View hit points

## • Photons

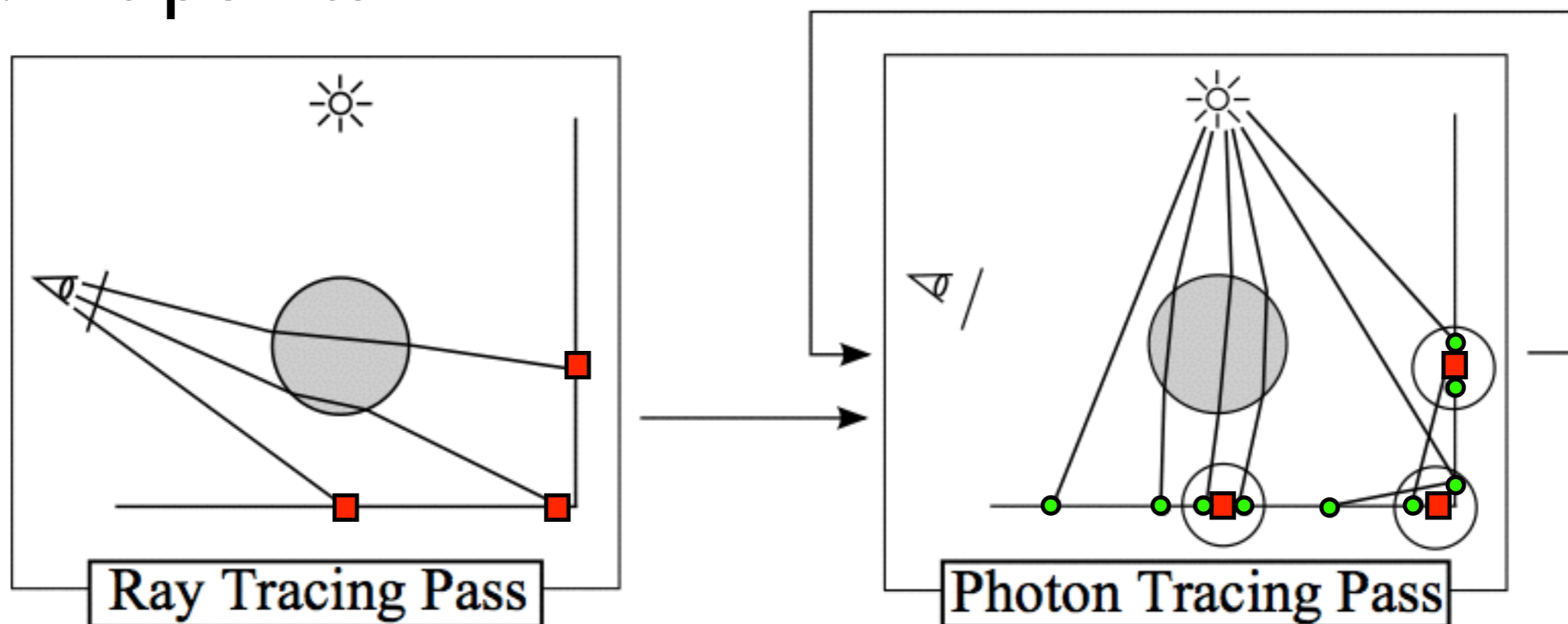
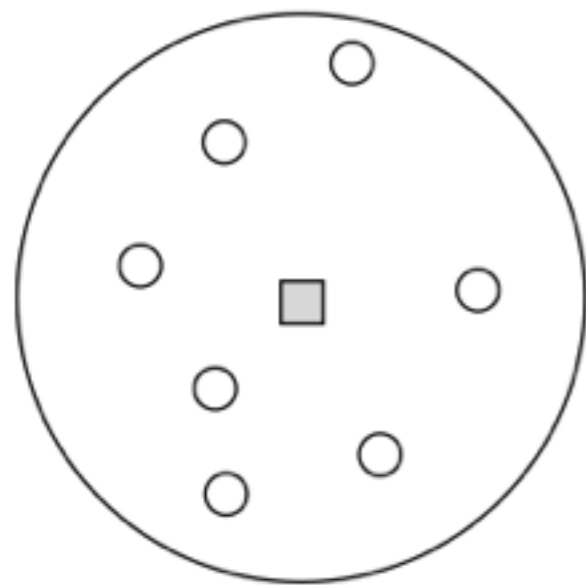


image from "Progressive Photon Mapping", T. Hachisuka, S. Ogaki and H.W. Jensen, ACM TOG 2008

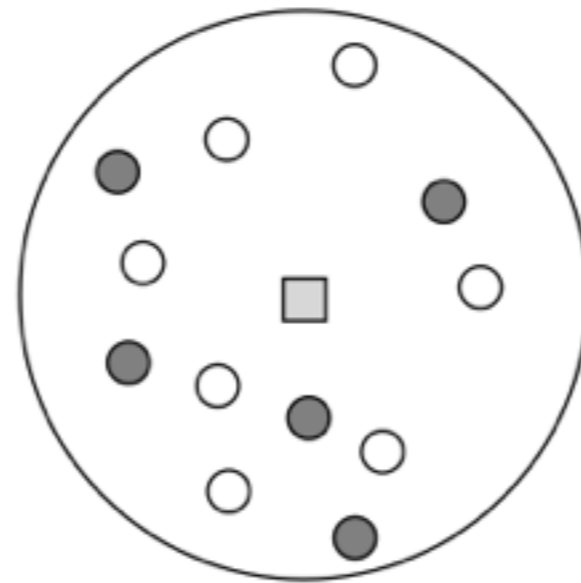
# Progressive Photon Mapping

LAB4

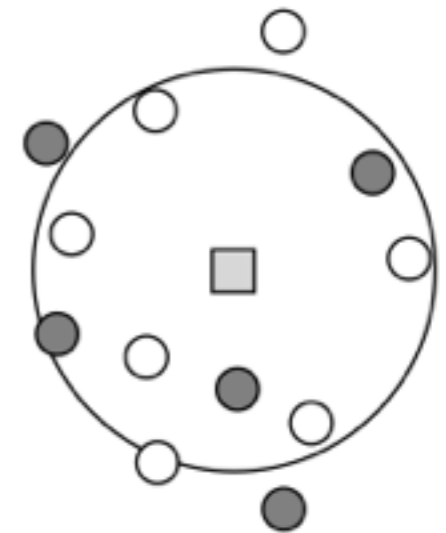
- 1st pass - find eye intersection positions
- 2nd pass - collect photons at intersection positions
  - Reduce radius of gathered photons as more photons are added



Radius:  $R(x)$   
Photons:  $N(x)$



Radius:  $R(x)$   
Photons:  $N(x) + M(x)$



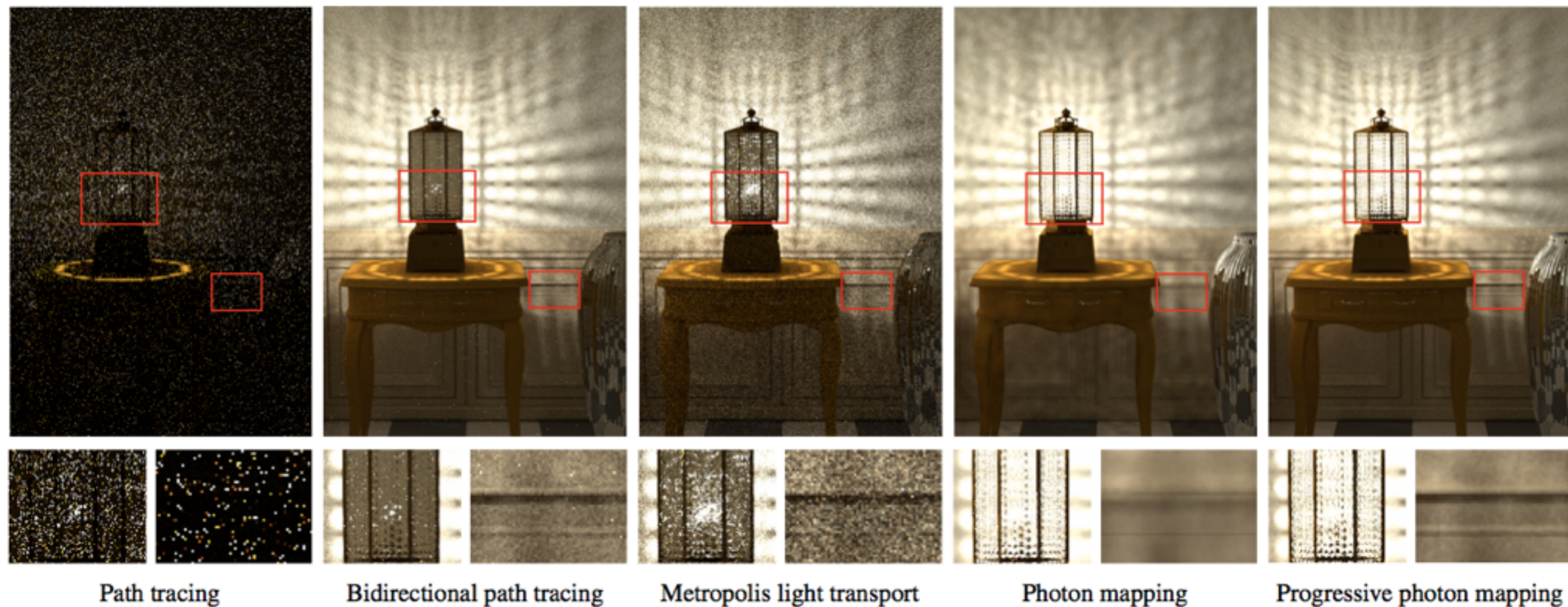
Radius:  $R(x) - dR(x)$   
Photons:  $N(x) + \alpha M(x)$

image from "Progressive Photon Mapping", T. Hachisuka, S. Ogaki and H.W. Jensen, ACM TOG 2008

# Progressive Photon Mapping

LAB4

- Equal time image : 22 hours
  - PM : 20 million photons, shorter runtime due to memory limit
  - PPM : 165 million photons



Path tracing

Bidirectional path tracing

Metropolis light transport

Photon mapping

Progressive photon mapping

image from "Progressive Photon Mapping", T. Hachisuka, S. Ogaki and H.W. Jensen, ACM TOG 2008

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# Stochastic Progressive Photon Mapping

- Add extra pass
- Randomly generate hit points

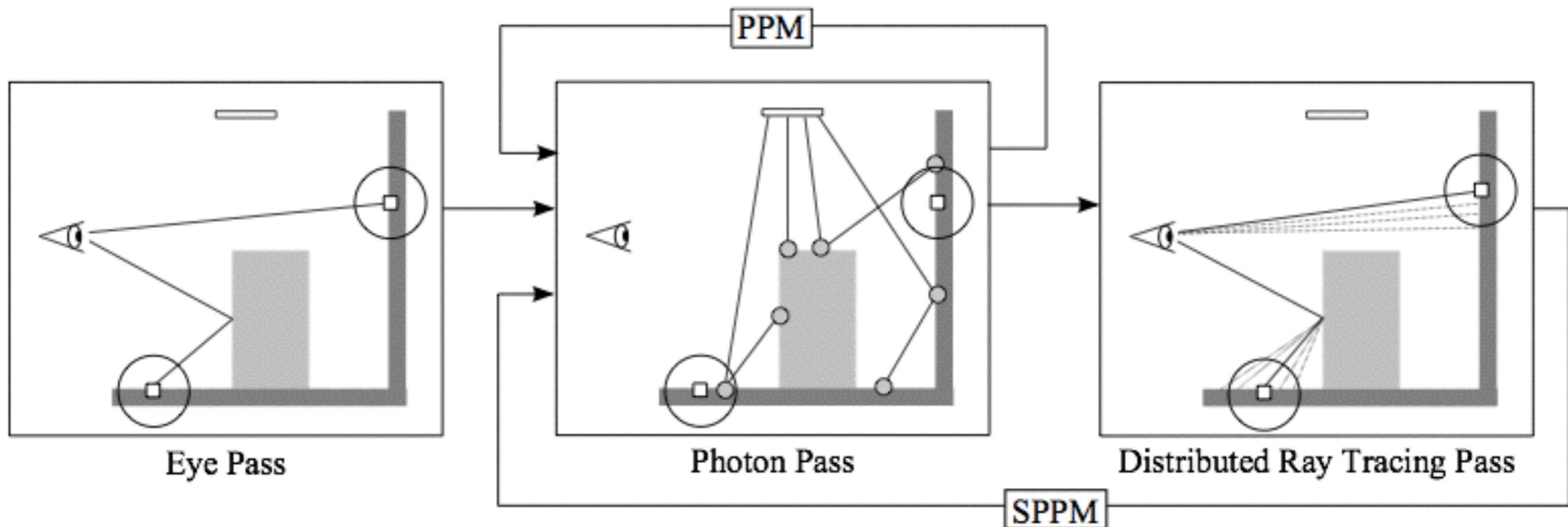
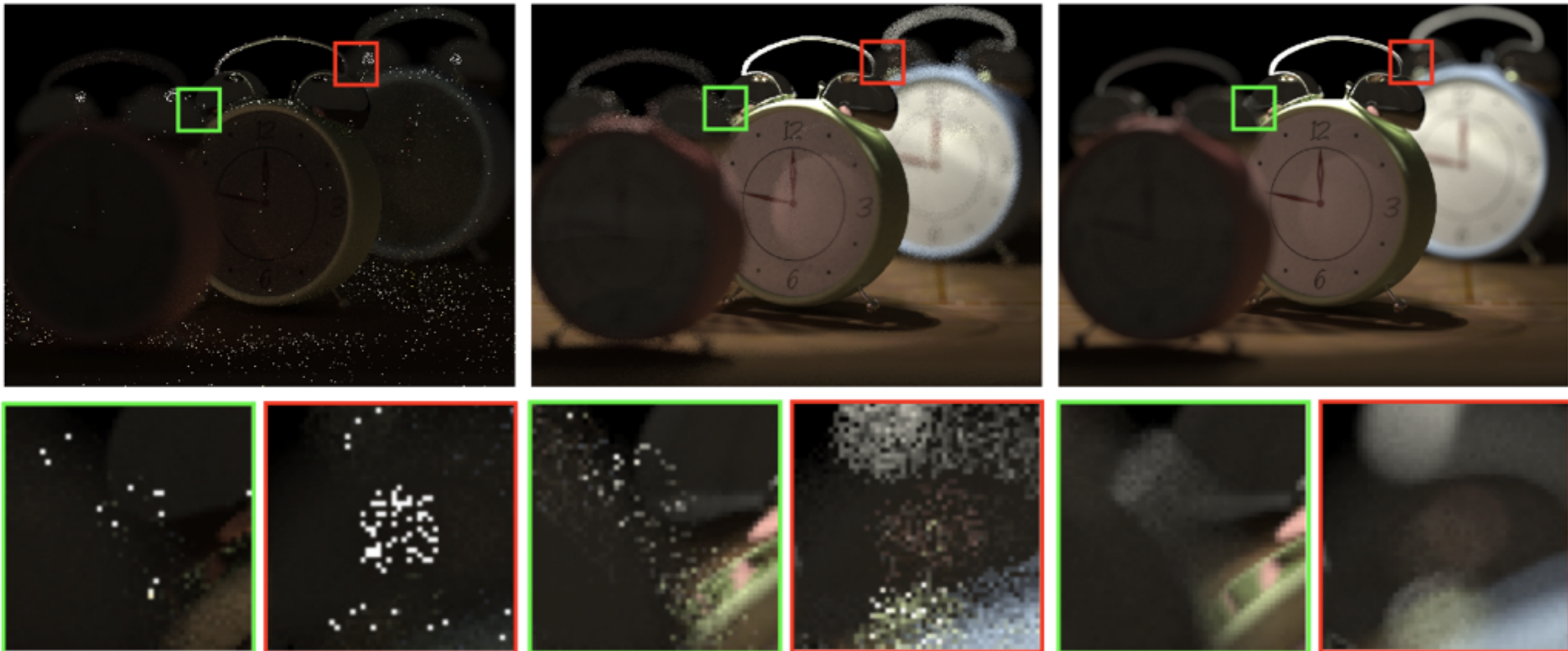


image from "Stochastic Progressive Photon Mapping", T. Hachisuka, and H.W. Jensen, ACM TOG 2009

# Stochastic Progressive Photon Mapping

- BDPT (left), PPM (middle), and SPPM (right)
- Same rendering time with Depth-of-field and caustics



# Stochastic Progressive Photon Mapping

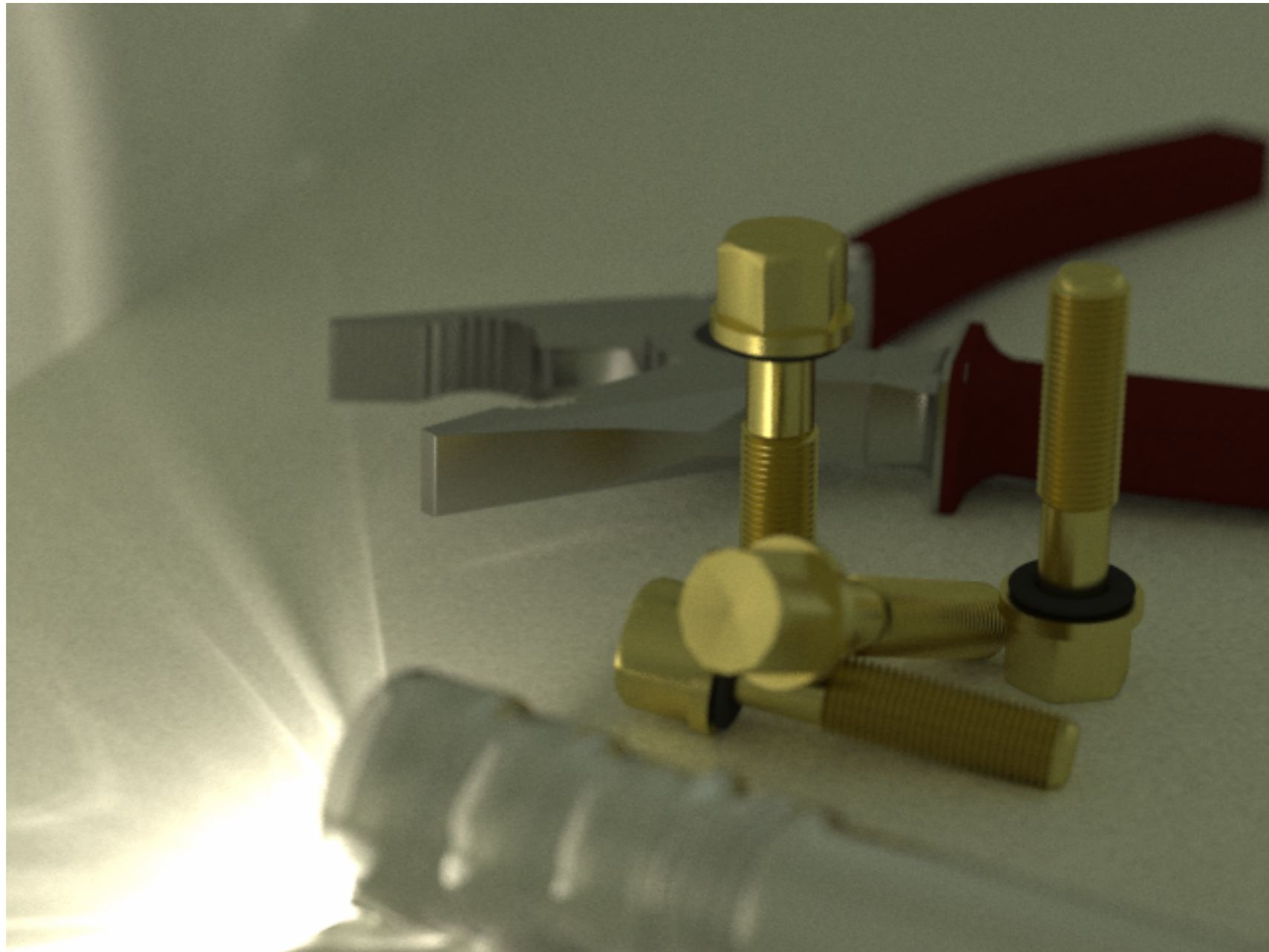


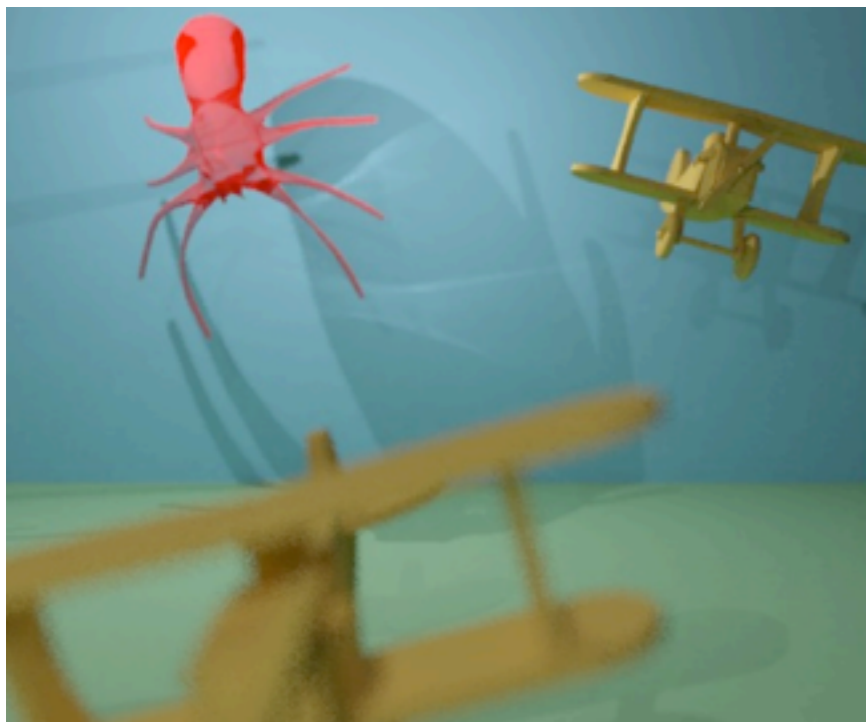
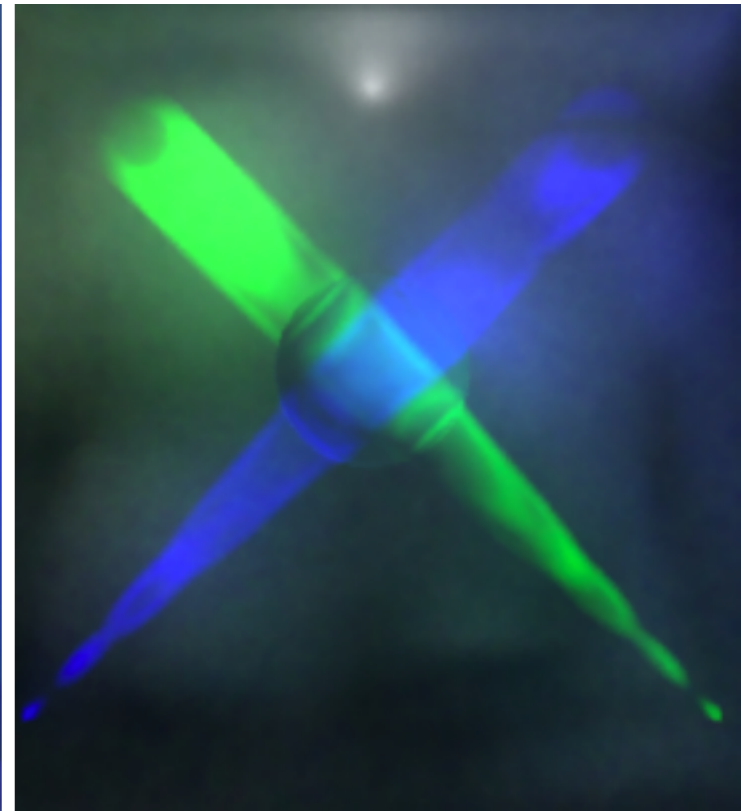
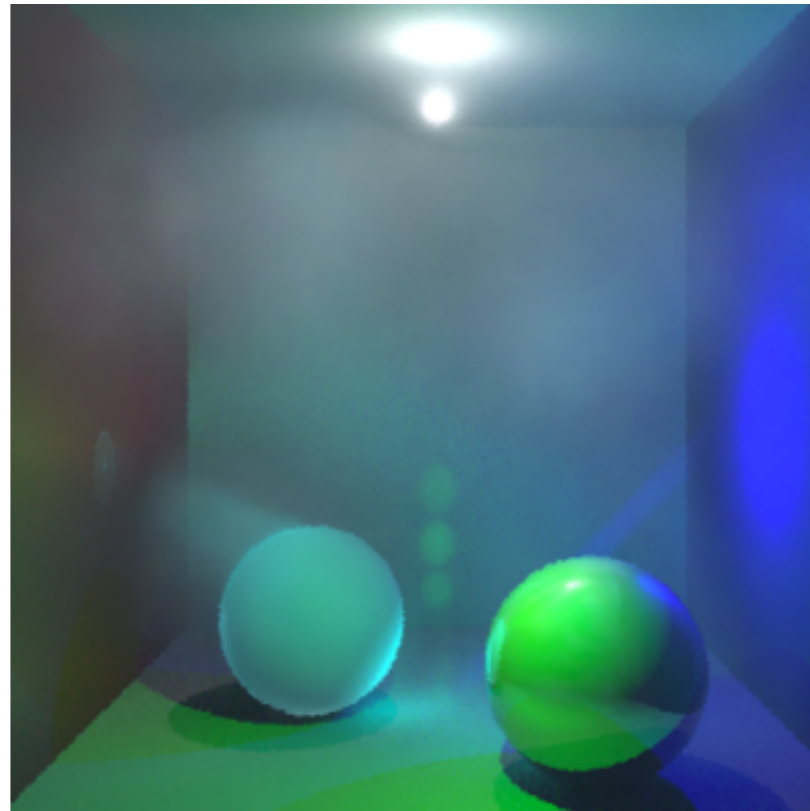
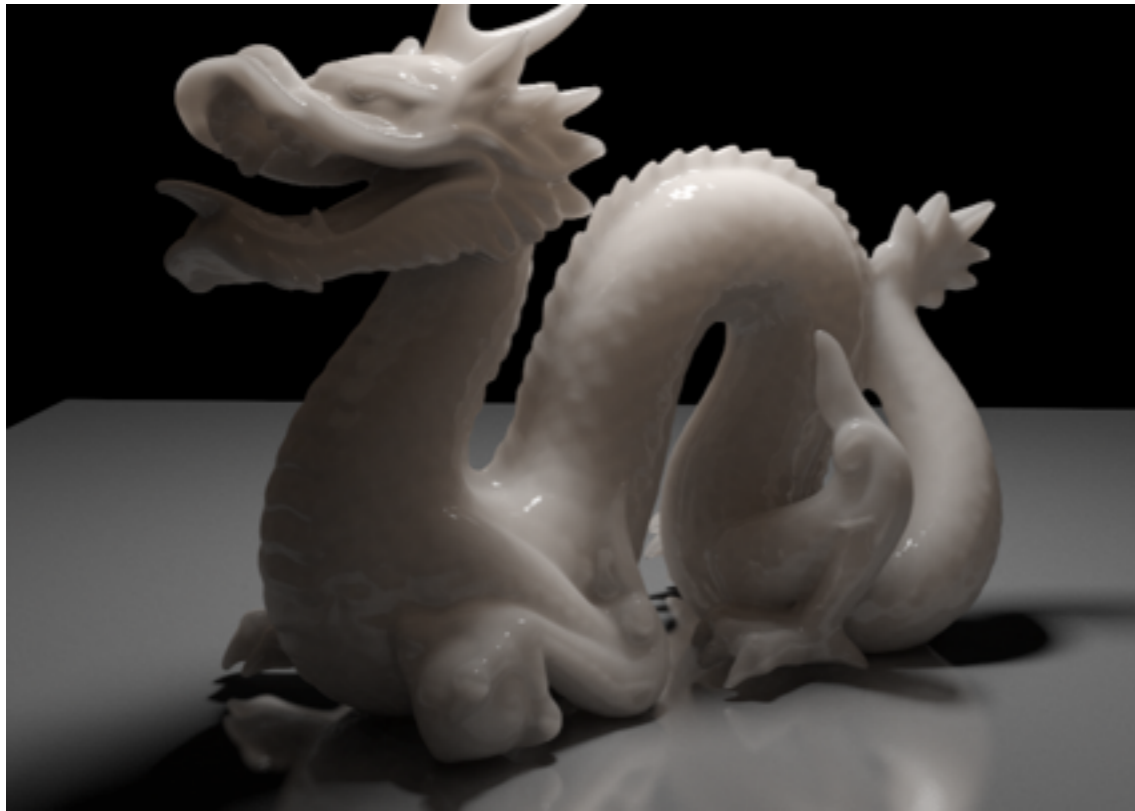
image courtesy Toshiya Hachisuka  
© 2011 Michael Doggett

# Elective

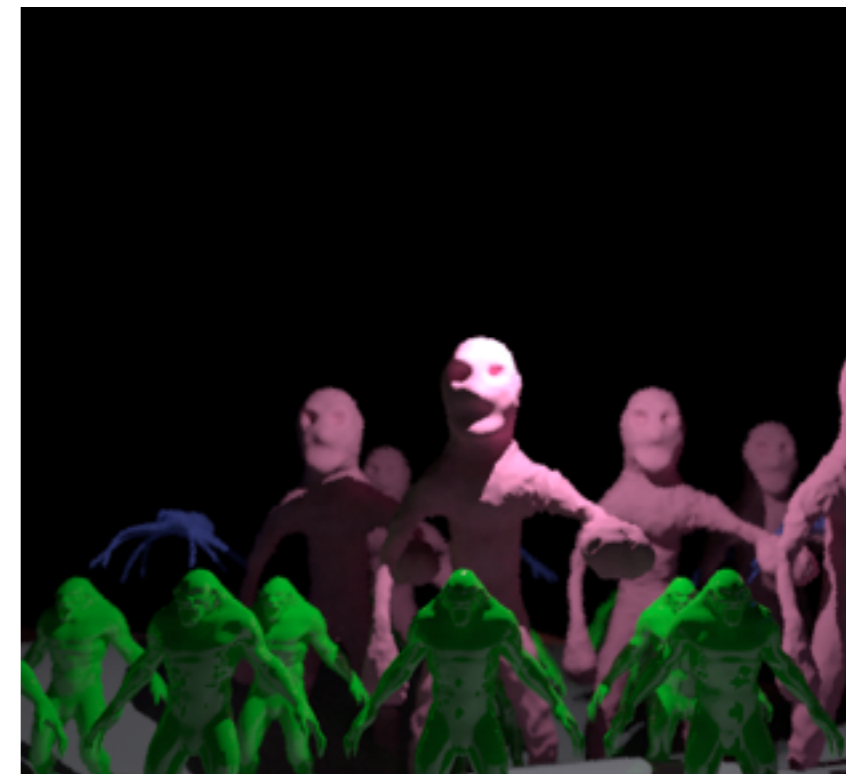
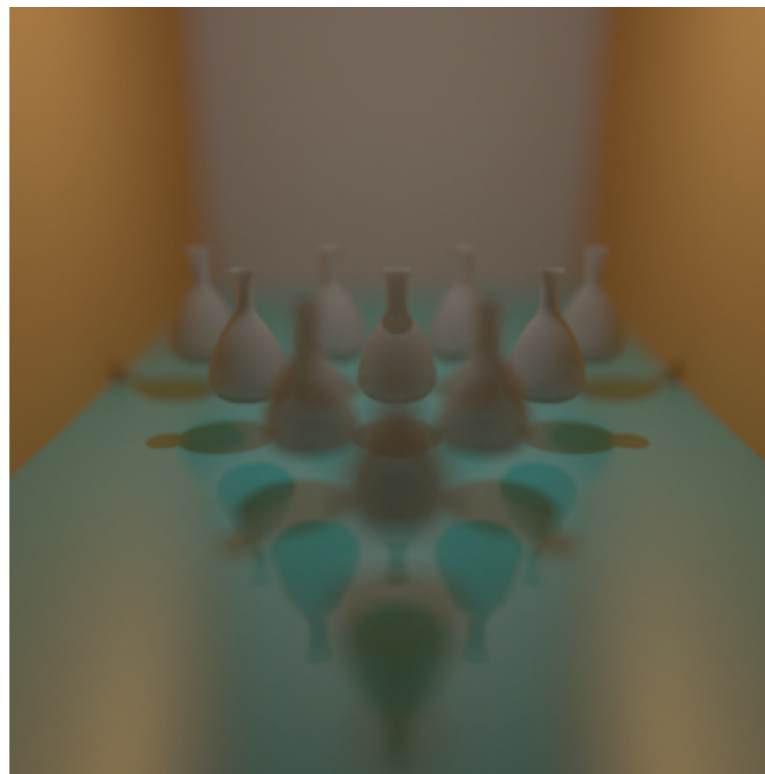
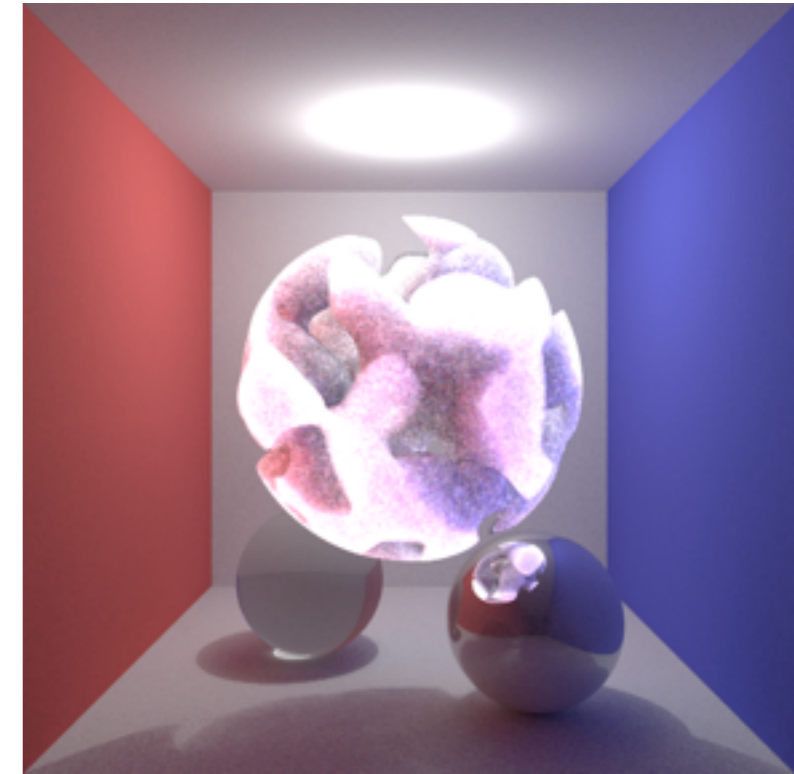
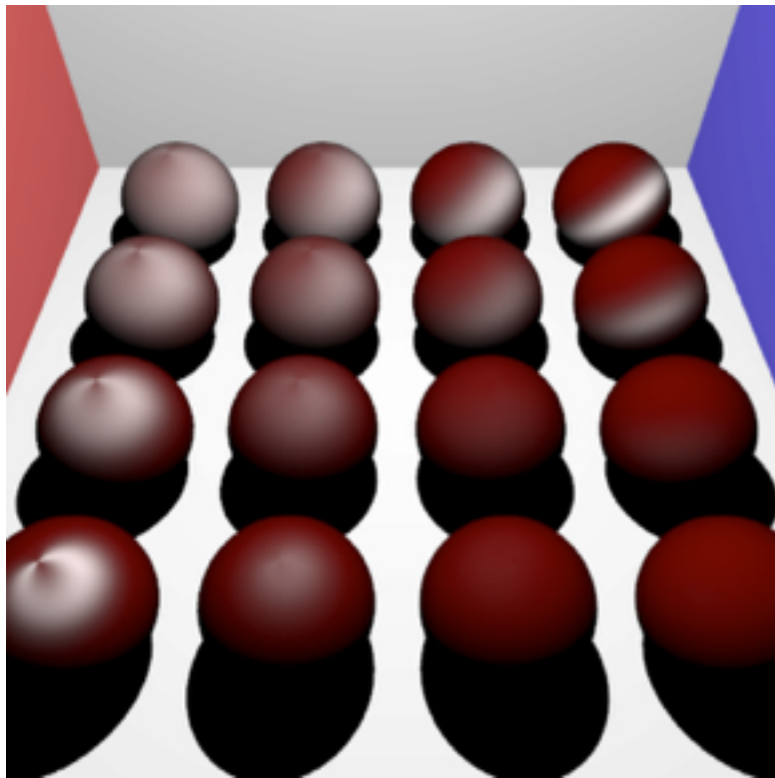
- Create a photorealistic image with an interesting effect
- AKA Assignment 5
- Choose your own topic
- Present an image at last lecture
  - 2 weeks
  - Describe what is interesting and how you did it



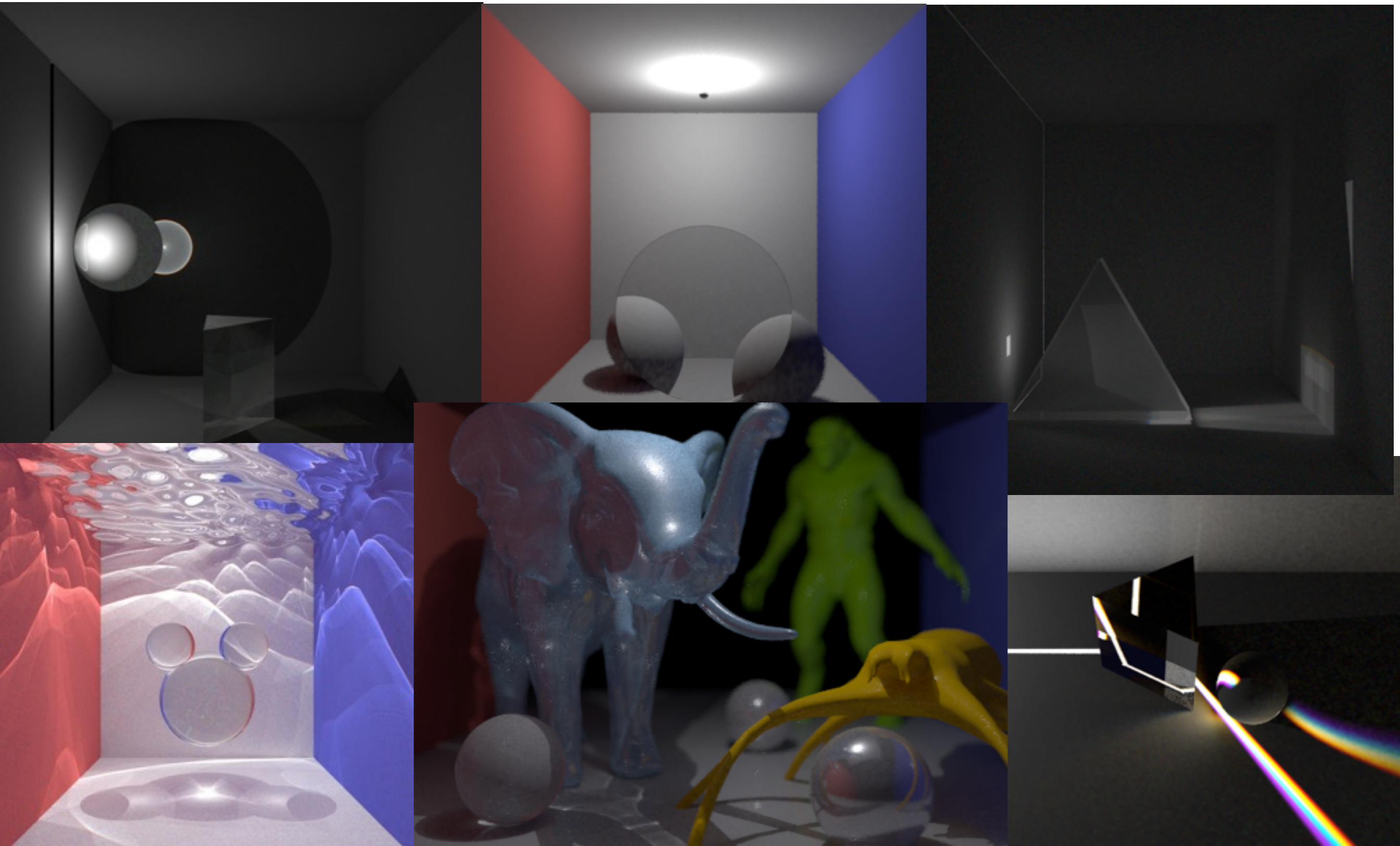
# Electives from 2011



# Elective from 2012

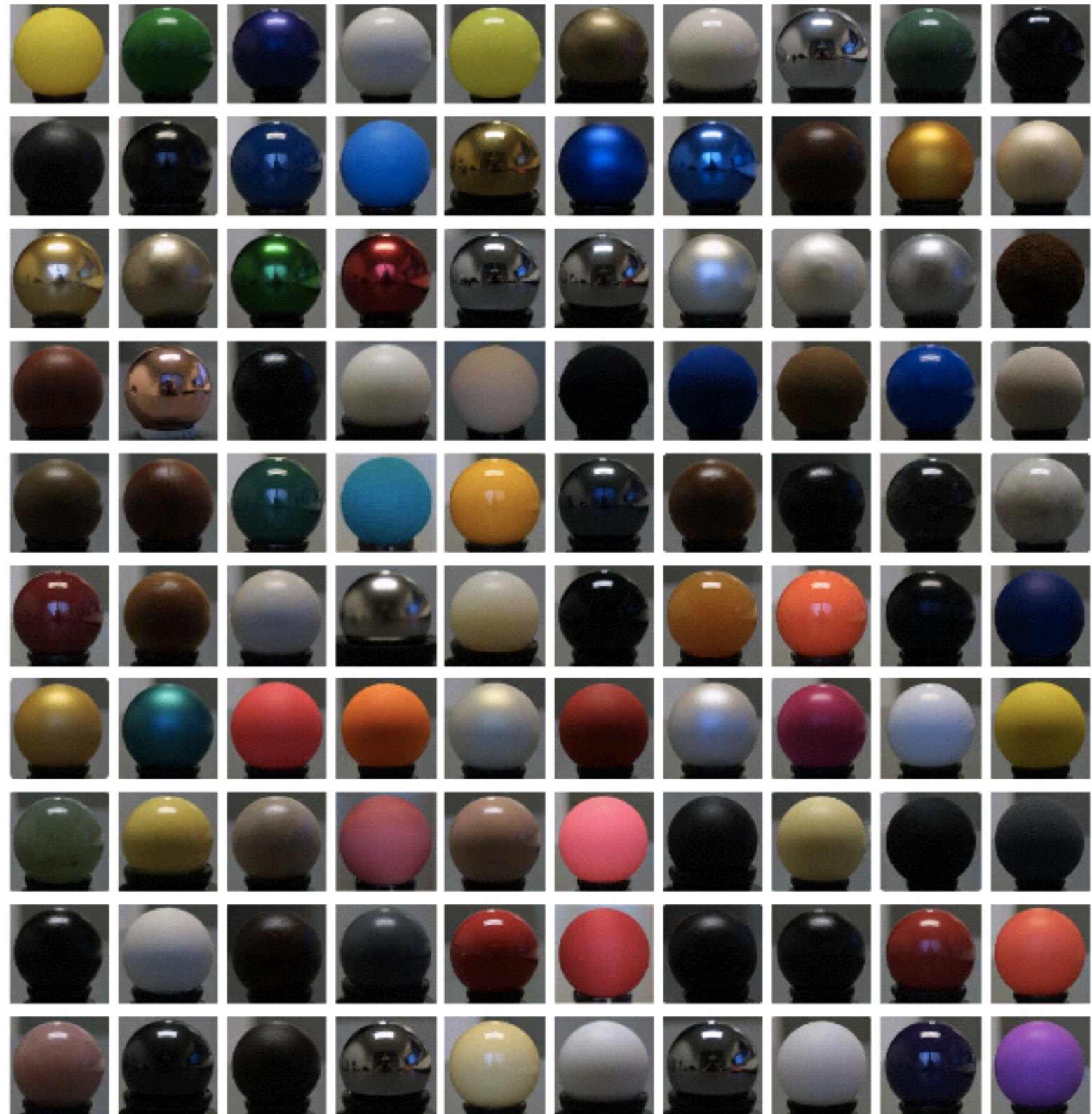


# Elective from 2013



# BRDFs

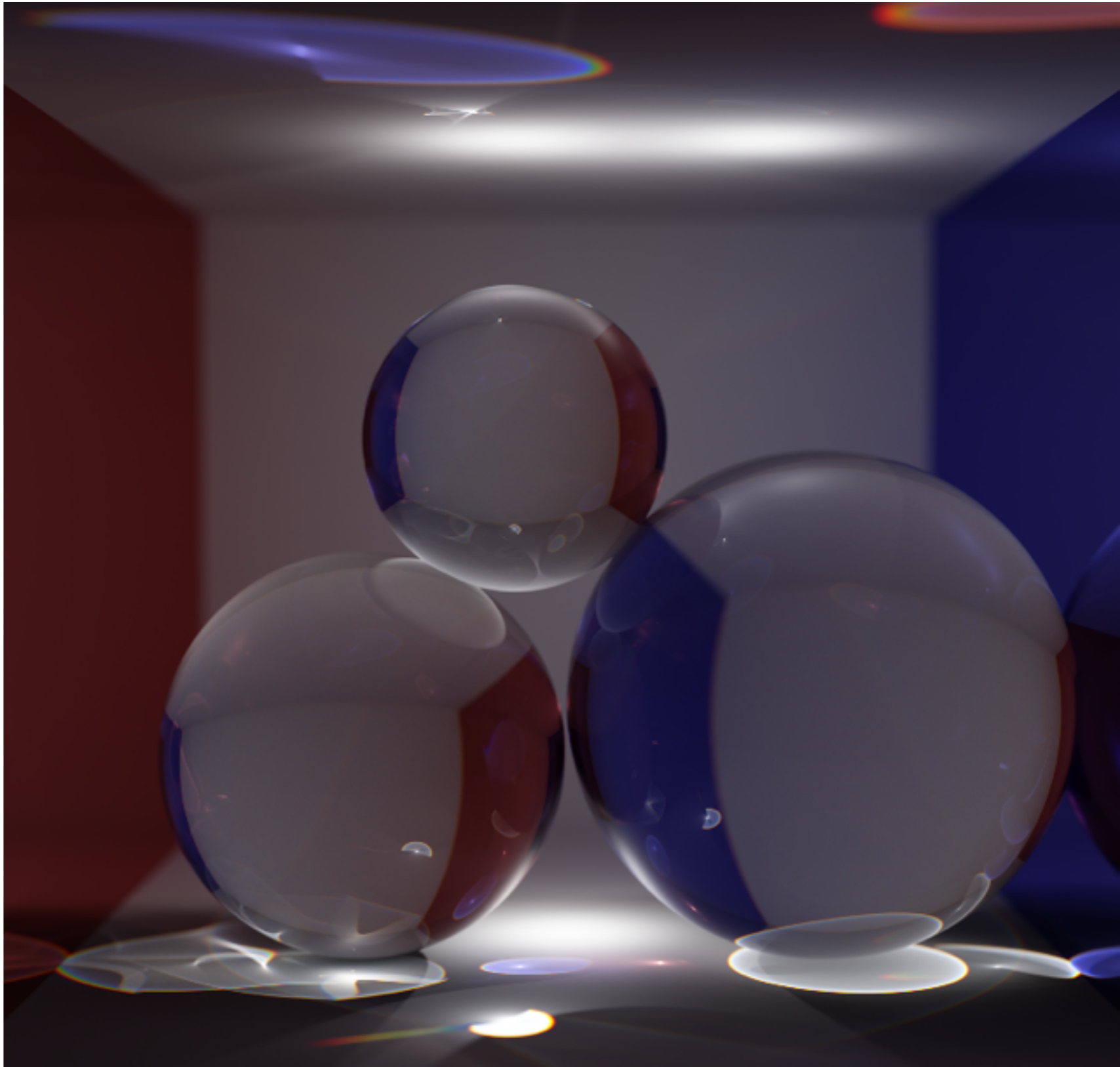
- Need more accurate physically correct model than Phong
- Measurement and analytical models
  - Schlick
  - Cook-Torrance '81
  - Ward '92
  - many others



from "A Data-Driven Reflectance Model",  
Wojciech Matusik, Hanspeter Pfister, Matt  
Brand and Leonard McMillan, ACM  
Transactions on Graphics 22, 3(2003)

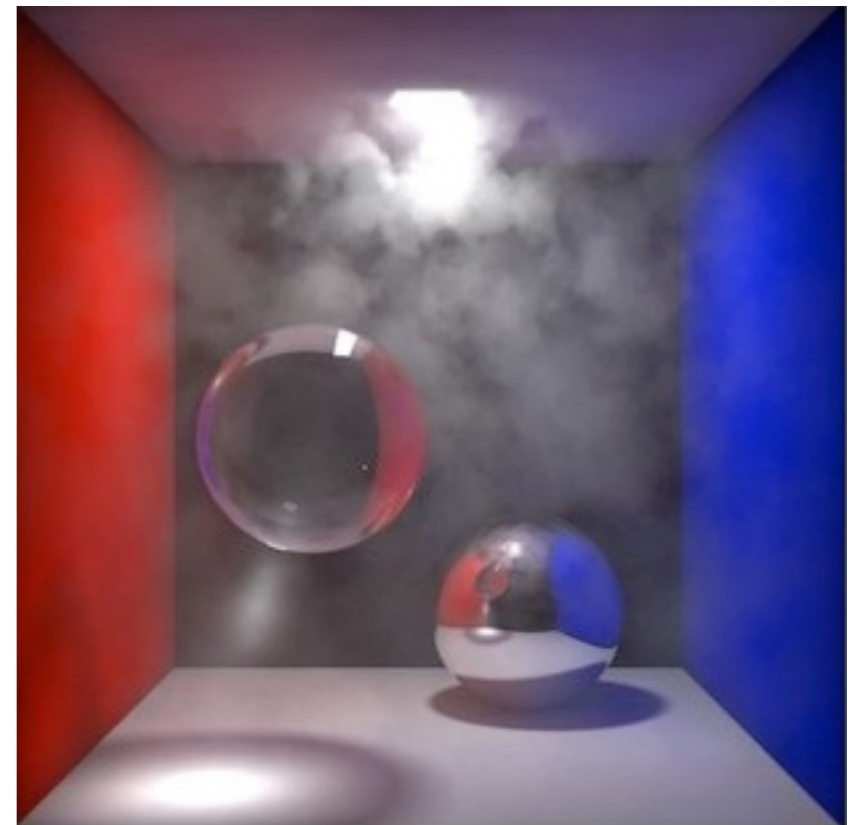
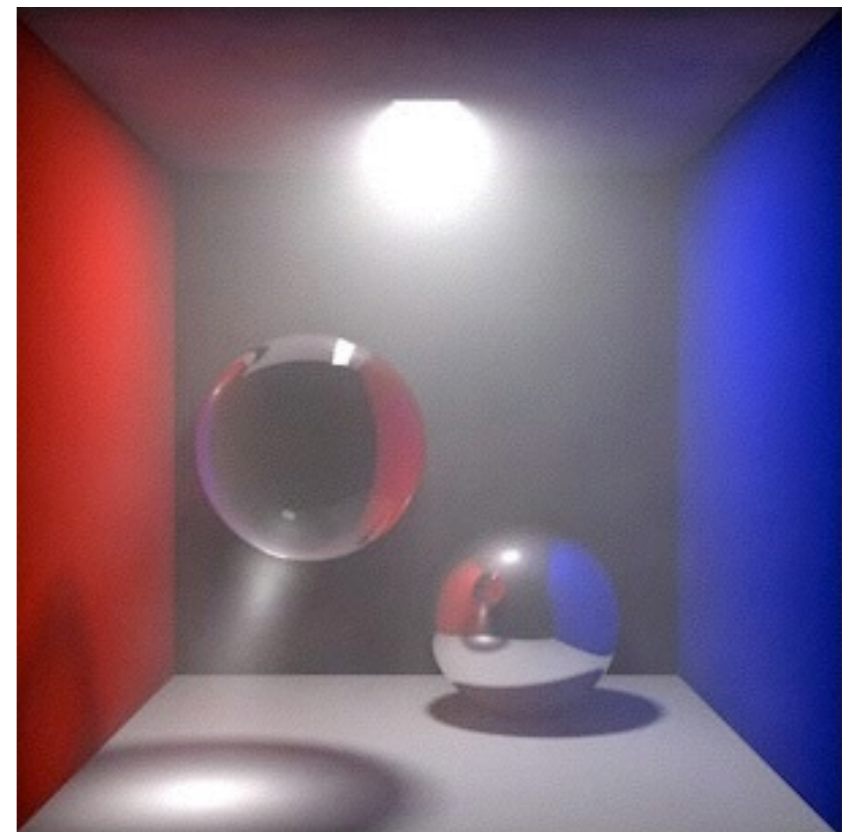
# Diffraction

- CDs, prisms
- Need to compute refraction for different wavelengths



# Inspiration...

- Subsurface scattering
- Participating media



Images courtesy of  
Henrik Wann Jensen

# Even more inspiration

- Have a look at Stanford University Rendering Competition for more ideas
- <http://www-graphics.stanford.edu/courses/cs348b-competition/cs348b-09/>



# Next

- Friday Lab 3: Path Tracing
- In 4 weeks
- Monday Seminar: Progressive Photon Mapping
- Wednesday Lecture: Advanced Topics