

# Attribute Grammars

## In practice using JastAdd

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(Examples from Donald Knuth)

**In this course:** Formalisms and algorithms useful in compiler construction

**Lexical analysis:** regular expressions, DFA, ..

**Syntactic analysis:** context-free grammars, parsing (LL, LR, ..)

**Semantic analysis:** abstract syntax trees, symbol tables, ..

# Short About Semantic Analysis

What is the **meaning** of my program?  
Does my program **do what I want**?

- Some things can be **checked by a compiler** via semantic analysis

*Are types used correctly in expressions? Are all exceptions caught? Segmentation faults?*

- Other things need to be **checked through testing**

*Does this function compute the right value for this input? ..*

# Formalisms for Semantic Analysis

denotational semantics, **attribute grammars**,  
operational semantics, natural semantics, term rewriting,  
algebraic semantics, axiomatic semantics, ...

# Brief History of Attribute Grammars (AGs)

Created in the 60s by Donald E. Knuth

*Semantic of Context-Free Languages*  
(Kunth, 1968)

An account of how AGs were developed is given in *The Genesis of Attribute Grammars* (Knuth, 1990)

## How do AGs work?

Extends a context-free grammar with **context-sensitive** semantic functions called **attributes**.

$$A = B C$$

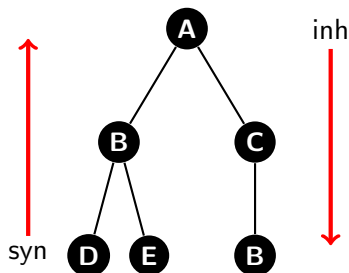
$$B = D E$$

$$C = B$$

We can add an attribute to D,  $D.v$ , and we can use this attribute in an equation for an attribute defined on B,  $B.v = D.v$ .

# The Basic Attributes

There are two kinds of attributes:  
**synthesized** and **inherited**.



synthesized attributes propagate information upwards

$$A.s = B.s + C.s$$

$$B.s = 1 + D.s$$

$$C.s = 2 + B.s$$

$$D.s = 3$$

inherited attributes propagate information downwards

$$B.i;$$

$$A.B.i = A.s;$$

$$A.C.i = 2;$$

The value of  $A.s$ ?

The value of  $B.i$ ?

## Binary Number Example (Knuth)

Computing the **decimal representation**  
of a **binary number**, for example,  $101_2 = 5_{10}$

$$\text{Version I: } 1 * 4 + 0 * 2 + 1 * 1 = 4 + 1 = 5$$

$$\text{Version II: } 1 * 2^2 + 0 * 2^1 + 1 * 2^0 = 4 + 1 = 5$$

# Binary Number Example (Knuth)

Given the following **grammar for binary numbers**:

$$\begin{array}{ll} \underline{N}um = \underline{L}ist & \underline{B}it = 0 \\ \underline{L}ist = \underline{B}it & \underline{B}it = 1 \\ \underline{L}ist = List \underline{B}it & \end{array}$$

**Which attributes are needed** for each of the below computation versions?

Version I:  $1 * 4 + 0 * 2 + 1 * 1 = 4 + 1 = 5$

Version II:  $1 * 2^2 + 0 * 2^1 + 1 * 2^0 = 4 + 1 = 5$

Discuss it with your neighbour

$$\text{Version I: } 1 * 4 + 0 * 2 + 1 * 1 = 4 + 1 = 5$$

### Grammar

$\underline{N}um = List$

$\underline{L}ist = Bit$

$\underline{L}ist_1 = List_2 \text{ Bit}$

$\underline{B}it = 0$

$\underline{B}it = 1$

### Semantic rules (syn)

$N.v = L.v$

$L.v = B.v$

$L_1.v = 2 * L_2.v + B.v$

$B.v = 0$

$B.v = 1$

**Version II:**  $1 * 2^2 + 0 * 2^1 + 1 * 2^0 = 4 + 1 = 5$

**Grammar**

$\underline{N}um = List$

$\underline{L}ist = Bit$

$\underline{L}ist_1 = \underline{L}ist_2 Bit$

$\underline{B}it = 0$

$\underline{B}it = 1$

**Semantic rules (syn)**

$N.v = L.v$

$L.v = B.v$

$L_1.v = L_2.v + B.v$

$B.v = 0$

$B.v = 2^{B.s}$

**Semantic rules (inh)**

$N : L.s = 0$

$L : B.s = L.s$

$L_1 : L_2.s = L_1.s + 1$

$L_1 : B.s = L_1.s$

# Evaluation of Attributes

Attributes may be **evaluated in any order**.

Attributes equations should have **no side-effects**.

**Circular dependencies?** Not allowed in Knuth-style AGs

**Inherited attribute on the root?** Not allowed in any AG, there is nothing to inherit.

# Some Attribute Grammar Extensions

## **Circular dependencies** (Farrow, 1986)

*Fix-point iteration*

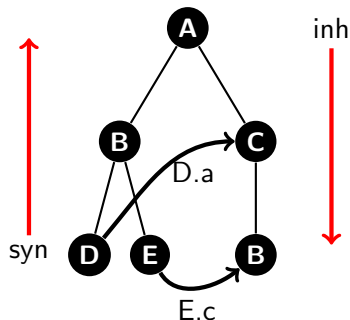
## **Reference attributes** (Hedin, 1994)

*References to distant nodes as values*

*This is supported by the JastAdd system*

# Reference Attributes Grammars

Attributes can have **references**  
to distant nodes **as values**



syn C D.a = D.b;

inh C D.b;

A.B.b = C;

syn B E.c = E.d;

inh B E.d;

B.E.d = D.a.B;

Use nodes can point to  
the node of their declaration.

```
abstract Stmt;  
Block : Stmt ::= Stmt*;  
Use : Stmt ::= <ID:String>;  
Decl : Stmt ::= <ID:String>;  
  
syn Decl Use.decl = lookup(getID());  
inh Decl Use.lookup(String ID);
```

## Equations for lookup?

Discuss with your neighbour

## Name Analysis using RAGs

```
abstract Stmt;
Block : Stmt ::= Stmt*;
Use : Stmt ::= <ID:String>;
Decl : Stmt ::= <ID:String>;

syn Decl Use.decl = lookup(getID());
inh Decl Use.lookup(String ID);

inh Decl Block.lookup(String ID);
eq Block.getStmt(int i).lookup(String ID) {
  for (int k = 0; k < getNumStmt(); k++) {
    Stmt s = getStmt(k);
    if (s instanceof Decl) &&
        ((Decl)s).getID().equals(ID))
      return (Decl)s;
  }
  return super.lookup(ID);
}
```

### **S E A L**

Small Example of an Attributed Language grammar

## SEAL example

```
int f = 0;

void main ( int p ) {
    int a = 0;
    while ( a < 10 ) {
        int c = f;
        while ( c < 5 ) {
            c = d + 2;
        }
        a = a + f(c);
    }
}

int f ( int q ) {
    return 2 * q;
}
```

## Abbreviated SEAL grammar

```
Program ::= Element*;  
abstract Element;  
Field : Element ::= Decl [Expr];  
Function : Element ::= FuncDecl Block;  
  
Decl ::= Type <Name:String>;  
FuncDecl : Decl ::= Parameter:Decl*;  
  
Use ::= <Name:String>;  
FuncUse : Use ::= Arg:Expr*;  
  
abstract Stmt;  
Block : Stmt ::= Stmt*;  
DeclStmt : Stmt ::= Decl [Expr];  
AssignStmt : Stmt ::= Use Expr;
```

## Name analysis

```
aspect NameAnalysis {  
  
    syn Decl Use.decl() = lookup(this);  
    inh Decl Use.lookup(Use u);  
  
    void Use.nameAnalysis() {  
        if (decl() == null) {  
            error("Use of unknown variable");  
        }  
    }  
    ...  
}
```

## More Information

<http://jastadd.org>