

Haskell problems

You are advised to solve these problems with Hugs or ghc. Solutions will be provided.

The last part of the Prelude contains all the predefined functions. Consult it for lots of examples, <http://www.haskell.org/onlinereport/standard-prelude.html>. When you are asked to define a function from the Prelude its name has been changed by adding an apostrophe.

1. Define a function that swaps the elements of a pair, `swap(1,True) => (True,1)`. Check the type!
2. Define a function that returns the last element of a nonempty list, `last' [1,2,3] => 3`. Hint: Use pattern matching with

```
last' [x]      =
last' (x:xs) =
```

3. Define a function that “zips” two lists, `zip' [1,2] [3,4] => [(1,3), (2,4)]`. You may assume that the lists have the same length. Hint: There are two cases: both lists are empty and both list are nonempty. Use pattern matching.
4. Define a function `filter' :: (a -> Bool) -> [a] -> [a]` such that `filter' even [1,2,4,5] => [2,4]` with list comprehension. The functions `filter` and `even` are defined in the Prelude. You may test them.
5. Do the same thing without list comprehension.
6. The function `map` is defined in Hudak using recursion. Use list comprehension to define it.
7. What is the type of `map map`? Try to infer the type before asking hugs. Hugs will give the answer from `:t map map`. Apply it to some arguments!
8. Define a data type to represent arithmetic expressions with `+`, `-`, `*` and `/` and `Double` constants.
9. Define a function that evaluates such expressions.
10. Define a function `toString :: Expr -> String` that returns a string representation of such expressions. Use parentheses around all composite subexpressions.
11. An integer list is either empty or has a head that is an `Integer` and a tail that is an integer list. Define a data type to represent such lists (without using `[]` lists).
12. Solve the same problem for lists that may have elements of any type. All elements of a single list are assumed to be of the same type.
13. The following is a data type for representing a binary tree with values at nodes and leaves.

```
data Tree a = Leaf a | Node (Tree a) a (Tree a)
```


Define a function that returns a “mirror image” of such a tree. `mirror (Node (Leaf 1) 2 (Node (Leaf 3) 4 (Leaf 5))) => Node (Node (Leaf 5) 4 (Leaf 3)) 2 (Leaf 1)`.

14. Define a function `map'` that takes a function and such a tree as arguments and returns a tree where the function has been applied to all the values.

```
map' (+1) (Node (Leaf 1) 2 (Node (Leaf 3) 4 (Leaf 5))) =>
(Node (Leaf 2) 3 (Node (Leaf 4) 5 (Leaf 6))).
```

`(+1)` is a function that adds 1 to its argument.

For any binary operator, `#`, `(a #) = (\ x -> a # x)`, `(# a) = (\ x -> x # a)`, and `(#) = (\ x -> (\y -> x # y))`.