

Problems

These problems will be discussed on seminar 1. Programs in Haskell are not required to compile.

- 1 Let $A = \{a, b, c\}$ and $B = \{0, 1\}$ be languages. Describe the following languages: $A \cdot B$, $A \cup B$, B^3 , A^* , $A(A \cup B)^*$, \emptyset^2 , \emptyset^* .
- 2 Find all languages L such that L^* has a finite number of strings.
- 3 Find all languages L such that $L = \{\epsilon\} \cup (\{a\} \cdot L)$.
- 4 Find a regular expression denoting the language $\{\epsilon\}$ without using ϵ .
- 5 Define an abstract representation for regular expressions using Haskell or Java.
- 6 Sometimes the language of regular expressions is extended with $[\alpha]$ meaning that the string correspondingly to α occurs or is missing and $\alpha+$ meaning that one or more strings corresponding to α is present. Define \mathcal{L} for the extended language.
- 7 Define a concrete grammar for concrete grammars, i.e. the grammar should show how to write productions and a complete grammar. You may assume that *terminal* and *nonterminal* are nonterminal symbols defined elsewhere and that there are no alternatives and repetitions in the right hand parts.
- 8 Define an abstract representation for concrete grammars using Haskell or Java.