

# Planning

Based on slides prepared by Tom Lenaerts  
SWITCH, Vlaams Interuniversitair Instituut voor Biotechnologie

Modifications by Jacek.Malec@cs.lth.se  
Original slides can be found at <http://aima.cs.berkeley.edu>



# Planning

The Planning problem  
Planning with State-space search  
Partial-order planning  
Planning graphs  
Planning with propositional logic  
Analysis of planning approaches

## What is Planning

Generate sequences of actions to perform tasks and achieve objectives.

- States, actions and goals

Search for solution over abstract space of plans.

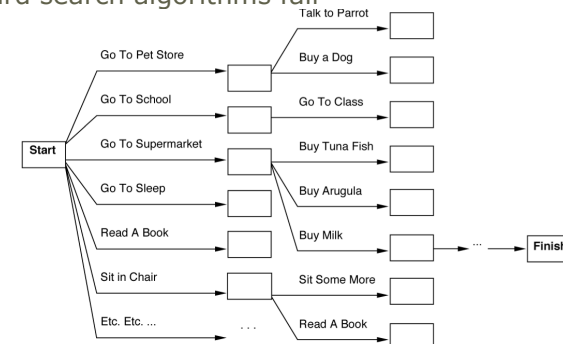
Classical planning environment: fully observable, deterministic, finite, static and discrete.

Assists humans in practical applications

- design and manufacturing
- military operations
- games
- space exploration
- transport and logistics

## Why not standard search?

Consider the task **get milk, bananas and a cordless drill**  
Standard search algorithms fail



## Difficulty of real world problems

### Assume a problem-solving agent using some search method ...

- Which actions are relevant?
  - Exhaustive search vs. backward search
- What is a good heuristic functions?
  - Good estimate of the cost of the state?
  - Problem-dependent vs, -independent
- How to decompose the problem?
  - Most real-world problems are *nearly* decomposable.

## Planning language

### What is a good language?

- Expressive enough to describe a wide variety of problems.
- Restrictive enough to allow efficient algorithms to operate on it.
- Planning algorithm should be able to take advantage of the logical structure of the problem.

### STRIPS and PDDL

## General language features

### Representation of states

- Decompose the world in logical conditions and represent a state as a *conjunction of positive literals*.
  - Propositional literals:  $Safe \wedge HasGold$
  - FO-literals (grounded and function-free):  $At(Plane1, Copenhagen) \wedge At(Plane2, Stockholm)$
- Closed world assumption

### Representation of goals

- Partially specified state and represented as a *conjunction of positive ground literals*
- A goal is *satisfied* if the state contains all literals in goal.

## General language features

### Representations of actions

- Action = PRECOND + EFFECT
  - $Action(Fly(p, from, to),$ 
    - $PRECOND: At(p, from) \wedge Plane(p) \wedge Airport(from) \wedge Airport(to)$
    - $EFFECT: \neg AT(p, from) \wedge At(p, to)$
- = action schema (p, from, to need to be instantiated)
  - Action name and parameter list
  - Precondition (conj. of function-free literals)
  - Effect (conjunction of function-free literals and P is True and not P is false)
- Add-list vs delete-list in Effect

# Language semantics?

## How do actions affect states?

- An action is applicable in any state that satisfies the precondition.
- For FO action schema applicability involves a substitution  $\theta$  for the variables in the PRECOND.

$At(P1, ARN) \wedge At(P2, CPH) \wedge Plane(P1) \wedge Plane(P2) \wedge$   
 $Airport(ARN) \wedge Airport(CPH)$

Satisfies :  $At(p, from) \wedge Plane(p) \wedge Airport(from) \wedge Airport(to)$

With  $\theta = \{p/P1, from/ARN, to/CPH\}$

Thus the action is applicable.

# Language semantics?

## The result of executing action $a$ in state $s$ is the state $s'$

- $s'$  is same as  $s$  except
  - Any positive literal  $P$  in the effect of  $a$  is added to  $s'$
  - Any negative literal  $\neg P$  is removed from  $s'$

EFFECT:  $\neg At(p, from) \wedge At(p, to)$ :

$At(P1, CPH) \wedge At(P2, CPH) \wedge Plane(P1) \wedge Plane(P2) \wedge Airport(ARN) \wedge$   
 $Airport(CPH)$

- STRIPS assumption: (avoids representational frame problem)  
*every literal NOT in the effect remains unchanged*

# Expressiveness and extensions

## STRIPS is simplified

- Important limit: function-free literals
  - Allows for propositional representation
  - Function symbols lead to infinitely many states and actions

## Expressiveness extension: Planning Domain Description Language (PDDL)

$Action(Fly(p: Plane, from: Airport, to: Airport),$

$PRECOND: At(p, from) \wedge (from \neq to)$

$EFFECT: \neg At(p, from) \wedge At(p, to)$ )

Standardization : now (since 2008) in its 3.1 version

# Example: air cargo transport

$Init(At(C1, CPH) \wedge At(C2, ARN) \wedge At(P1, CPH) \wedge At(P2, ARN) \wedge Cargo(C1) \wedge$   
 $Cargo(C2) \wedge Plane(P1) \wedge Plane(P2) \wedge Airport(ARN) \wedge Airport(CPH))$

$Goal(At(C1, ARN) \wedge At(C2, CPH))$

$Action(Load(c, p, a)$

$PRECOND: At(c, a) \wedge At(p, a) \wedge Cargo(c) \wedge Plane(p) \wedge Airport(a)$

$EFFECT: \neg At(c, a) \wedge In(c, p)$ )

$Action(Unload(c, p, a)$

$PRECOND: In(c, p) \wedge At(p, a) \wedge Cargo(c) \wedge Plane(p) \wedge Airport(a)$

$EFFECT: At(c, a) \wedge \neg In(c, p)$ )

$Action(Fly(p, from, to)$

$PRECOND: At(p, from) \wedge Plane(p) \wedge Airport(from) \wedge Airport(to)$

$EFFECT: \neg At(p, from) \wedge At(p, to)$ )

$[Load(C1, P1, CPH), Fly(P1, CPH, ARN), Load(C2, P2, ARN), Fly(P2, ARN, CPH)]$

# Example: Spare tire problem

```

Init(At(Flat, Axle) ∧ At(Spare, trunk))
Goal(At(Spare, Axle))
Action(Remove(Spare, Trunk))
  PRECOND: At(Spare, Trunk)
  EFFECT: ¬At(Spare, Trunk) ∧ At(Spare, Ground))
Action(Remove(Flat, Axle))
  PRECOND: At(Flat, Axle)
  EFFECT: ¬At(Flat, Axle) ∧ At(Flat, Ground))
Action(PutOn(Spare, Axle))
  PRECOND: At(Spare, Ground) ∧ ¬At(Flat, Axle)
  EFFECT: At(Spare, Axle) ∧ ¬At(Spare, Ground))
Action(LeaveOvernight)
  PRECOND:
  EFFECT: ¬At(Spare, Ground) ∧ ¬At(Spare, Axle) ∧ ¬At(Spare, trunk) ∧ ¬At(Flat, Ground) ∧
  ¬At(Flat, Axle)
  
```

This example goes beyond STRIPS: negative literal in pre-condition (PDDL description)

# Example: Blocks world

```

Init(On(A, Table) ∧ On(B, Table) ∧ On(C, Table) ∧ Block(A) ∧ Block(B)
  ∧ Block(C) ∧ Clear(A) ∧ Clear(B) ∧ Clear(C))
  
```

```
Goal(On(A, B) ∧ On(B, C))
```

```

Action(Move(b, x, y))
  PRECOND: On(b, x) ∧ Clear(b) ∧ Clear(y) ∧ Block(b) ∧ (b ≠ x) ∧ (b
  ≠ y) ∧ (x ≠ y)
  EFFECT: On(b, y) ∧ Clear(x) ∧ ¬On(b, x) ∧ ¬Clear(y))
Action(MoveToTable(b, x))
  PRECOND: On(b, x) ∧ Clear(b) ∧ Block(b) ∧ (b ≠ x)
  EFFECT: On(b, Table) ∧ Clear(x) ∧ ¬On(b, x)
  
```

# Planning with state-space search

Both forward and backward search possible

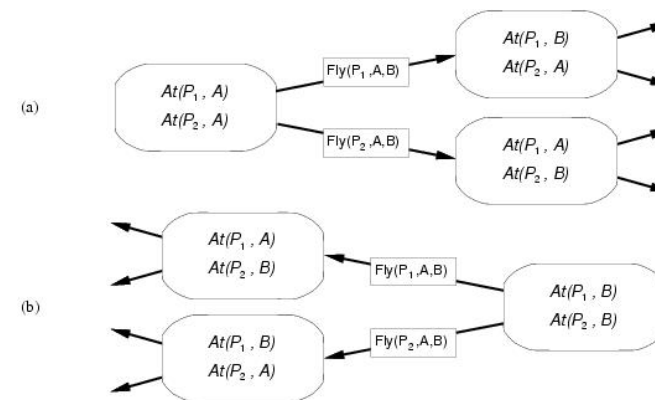
## Progression planners

- forward state-space search
- Consider the effect of all possible actions in a given state

## Regression planners

- backward state-space search
- To achieve a goal, what must have been true in the previous state.

# Progression and regression



# Progression algorithm

## Formulation as state-space search problem:

- Initial state = initial state of the planning problem
  - Literals not appearing are false
- Actions = those whose preconditions are satisfied
  - Add positive effects, delete negative
- Goal test = does the state satisfy the goal
- Step cost = each action costs 1

No functions ... any graph search that is complete is a complete planning algorithm.

- E.g. A\*

## Inefficient:

- (1) irrelevant action problem
- (2) good heuristic required for efficient search

# Regression algorithm

## How to determine predecessors?

- What are the states from which applying a given action leads to the goal?

Goal state =  $At(C1, B) \wedge At(C2, B) \wedge \dots \wedge At(C20, B)$

Relevant action for first conjunct:  $Unload(C1, p, B)$

Works only if pre-conditions are satisfied.

Previous state =  $In(C1, p) \wedge At(p, B) \wedge At(C2, B) \wedge \dots \wedge At(C20, B)$

Subgoal  $At(C1, B)$  should not be present in this state.

## Actions must not undo desired literals (consistent)

Main advantage: only relevant actions are considered.

- Often much lower branching factor than forward search.

# Regression algorithm

## General process for predecessor construction

- Give a goal description G
- Let A be an action that is relevant and consistent
- The predecessors are as follows:
  - Any positive effects of A that appear in G are deleted.
  - Each precondition literal of A is added, unless it already appears.

Any standard search algorithm can be added to perform the search.

Termination when predecessor is satisfied by initial state.

- In FO case, satisfaction might require a substitution.

# Heuristics for state-space search

Neither progression or regression are very efficient without a good heuristic.

- How many actions are needed to achieve the goal?
- Exact solution is NP hard, find a good estimate

## Two approaches to find admissible heuristic:

- The optimal solution to the relaxed problem.
  - Remove all preconditions from actions
- The subgoal independence assumption:
  - The cost of solving a conjunction of subgoals is approximated by the sum of the costs of solving the subproblems independently.

# Partial-order planning

Progression and regression planning are *totally ordered plan search forms*.

- They cannot take advantage of problem decomposition.
  - Decisions must be made on how to sequence actions on all the subproblems

## Least commitment strategy:

- Delay choice during search

# Shoe example

Goal(RightShoeOn  $\wedge$  LeftShoeOn)

Init()

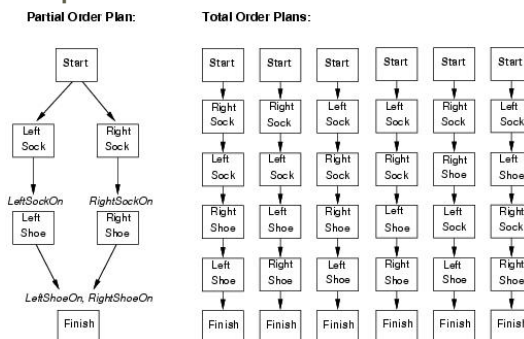
Action(RightShoe,	PRECOND: RightSockOn	EFFECT: RightShoeOn)
Action(RightSock,	PRECOND:	EFFECT: RightSockOn)
Action(LeftShoe,	PRECOND: LeftSockOn	EFFECT: LeftShoeOn)
Action(LeftSock,	PRECOND:	EFFECT: LeftSockOn)

Planner: combine two action sequences

- (1) leftsock, leftshoe
- (2) rightsock, rightshoe

# Partial-order planning(POP)

Any planning algorithm that can place two actions into a plan without stating which comes first is a PO plan.



# POP as a search problem

States are (mostly unfinished) plans.

- The empty plan contains only start and finish actions.

Each plan has 4 components:

- A set of actions (steps of the plan)
- A set of ordering constraints:  $A < B$  (A before B)
  - Cycles represent contradictions.
- A set of causal links  $A \xrightarrow{p} B$ 
  - The plan may not be extended by adding a new action C that conflicts with the causal link. (if the effect of C is  $\neg p$  and if C could come after A and before B)
- A set of open preconditions.
  - If precondition is not achieved by action in the plan.

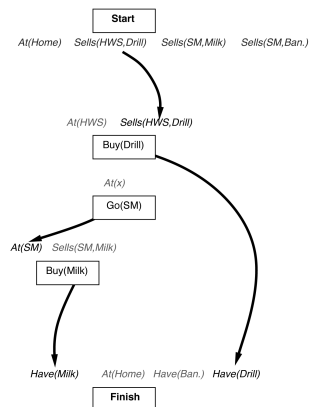
# Example of final plan

Actions={Rightsock, Rightshoe, Leftsock,  
 Leftshoe, Start, Finish}  
 Orderings={Rightsock < Rightshoe; Leftsock  
 < Leftshoe}  
 Links={Rightsock->Rightsockon ->  
 Rightshoe, Leftsock->Leftsockon-> Leftshoe,  
 Rightshoe->Rightshoeon->Finish, ...}  
 Open preconditions={ }

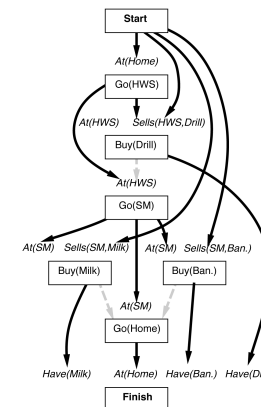
# Shopping list example



# Shopping list example



# Shopping list example



## POP as a search problem

A plan is *consistent* iff there are no cycles in the ordering constraints and no conflicts with the causal links.

A consistent plan with no open preconditions is a *solution*.

A partial order plan is executed by repeatedly choosing *any* of the possible next actions.

- This flexibility is a benefit in non-cooperative environments;
- Gives rise to emergent behaviours.

## Solving POP

Assume propositional planning problems:

- The initial plan contains *Start* and *Finish*, the ordering constraint  $Start < Finish$ , no causal links, all the preconditions in *Finish* are open.
- Successor function :
  - picks one open precondition  $p$  on an action  $B$  and
  - generates a successor plan for every possible consistent way of choosing action  $A$  that achieves  $p$ .
- Test goal

## Enforcing consistency

When generating successor plan:

- The causal link  $A \rightarrow p \rightarrow B$  and the ordering constraint  $A < B$  is added to the plan.
  - If  $A$  is new also add  $start < A$  and  $A < B$  to the plan
- Resolve conflicts between new causal link and all existing actions
- Resolve conflicts between action  $A$  (if new) and all existing causal links.

## Process summary

Operators on partial plans

- Add link from existing plan to open precondition.
- Add a step to fulfill an open condition.
- Order one step w.r.t another to remove possible conflicts

Gradually move from incomplete/vague plans to complete/correct plans

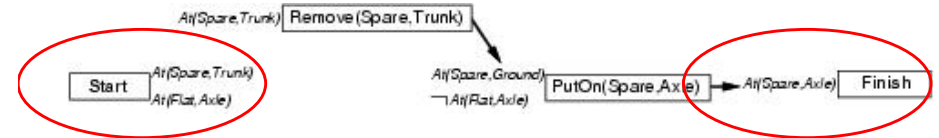
Backtrack if an open condition is unachievable or if a conflict is irresolvable.



# Example: Spare tire problem

*Init*( $At(Flat, Axle) \wedge At(Spare, trunk)$ )  
*Goal*( $At(Spare, Axle)$ )  
*Action*(*Remove*(*Spare, Trunk*))  
 PRECOND:  $At(Spare, Trunk)$   
 EFFECT:  $\neg At(Spare, Trunk) \wedge At(Spare, Ground)$   
*Action*(*Remove*(*Flat, Axle*))  
 PRECOND:  $At(Flat, Axle)$   
 EFFECT:  $\neg At(Flat, Axle) \wedge At(Flat, Ground)$   
*Action*(*PutOn*(*Spare, Axle*))  
 PRECOND:  $At(Spare, Ground) \wedge \neg At(Flat, Axle)$   
 EFFECT:  $At(Spare, Axle) \wedge \neg At(Spare, Ground)$   
*Action*(*LeaveOvernight*)  
 PRECOND:  
 EFFECT:  $\neg At(Spare, Ground) \wedge \neg At(Spare, Axle) \wedge \neg At(Spare, trunk) \wedge \neg At(Flat, Ground) \wedge \neg At(Flat, Axle)$

# Solving the problem



Initial plan: Start with EFFECTS and Finish with PRECOND.

# Solving the problem



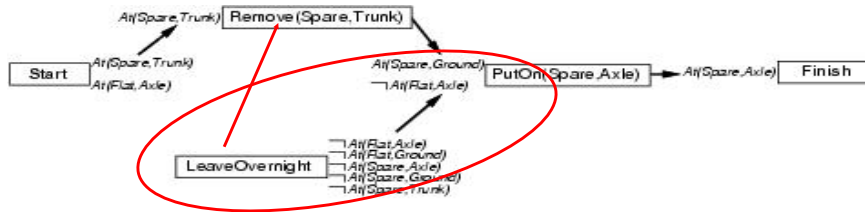
Initial plan: Start with EFFECTS and Finish with PRECOND.  
 Pick an open precondition:  $At(Spare, Axle)$   
 Only *PutOn*(*Spare, Axle*) is applicable  
 Add causal link:  $PutOn(Spare, Axle) \xrightarrow{At(Spare, Axle)} Finish$   
 Add constraint :  $PutOn(Spare, Axle) < Finish$

# Solving the problem



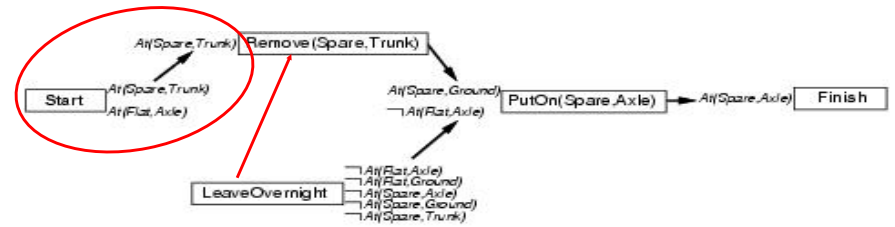
Pick an open precondition:  $At(Spare, Ground)$   
 Only *Remove*(*Spare, Trunk*) is applicable  
 Add causal link:  $Remove(Spare, Trunk) \xrightarrow{At(Spare, Ground)} PutOn(Spare, Axle)$   
 Add constraint :  $Remove(Spare, Trunk) < PutOn(Spare, Axle)$

# Solving the problem



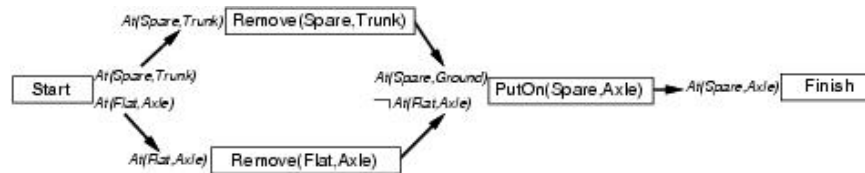
Pick an open precondition:  $\neg At(Flat, Axle)$   
 LeaveOverNight is applicable  
 conflict: LeaveOverNight also has the effect  $\neg At(Spare, Ground)$   
 $Remove(Spare, Trunk) \xrightarrow{At(Spare, Ground)} PutOn(Spare, Axle)$   
 To resolve, add constraint : LeaveOverNight < Remove(Spare, Trunk)

# Solving the problem



Pick an open precondition:  $At(Spare, Trunk)$   
 Only Start is applicable  
 Add causal link:  $Start \xrightarrow{At(Spare, Trunk)} Remove(Spare, Trunk)$   
 Conflict: of causal link with effect  $\neg At(Spare, Trunk)$  in LeaveOverNight  
 - No re-ordering solution possible.  
 backtrack

# Solving the problem



Remove LeaveOverNight, Remove(Spare, Trunk)  
 and causal links  
 Repeat step with Remove(Spare,Trunk)  
 Add also RemoveFlatAxle and finish

# Some details ...

What happens when a first-order representation that includes variables is used?

- Complicates the process of detecting and resolving conflicts.
- Can be resolved by introducing inequality constraint.

CSP's most-constrained-variable heuristic can be used for planning algorithms to select a PRECOND.

# Planning graphs

Used to achieve better heuristic estimates.

- A solution can also be directly extracted using GRAPHPLAN.

Consists of a sequence of levels that correspond to time steps in the plan.

- Level 0 is the initial state.
- Each level consists of a set of literals and a set of actions.
  - *Literals* = all those that *could* be true at that time step, depending upon the actions executed at the preceding time step.
  - *Actions* = all those actions that *could* have their preconditions satisfied at that time step, depending on which of the literals actually hold.

# Planning graphs

“Could”?

- Records only a restricted subset of possible negative interactions among actions.

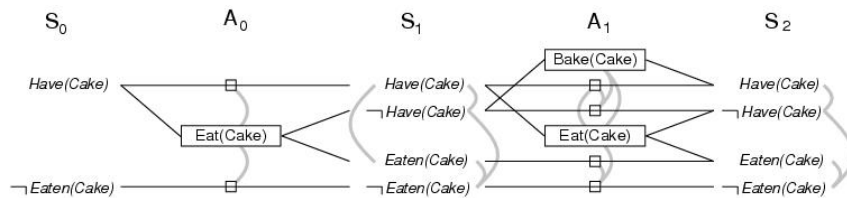
They work only for propositional problems.

Example:

```

Init(Have(Cake))
Goal(Have(Cake) ^ Eaten(Cake))
Action(Eat(Cake), PRECOND: Have(Cake)
      EFFECT: ¬Have(Cake) ^ Eaten(Cake))
Action(Bake(Cake), PRECOND: ¬Have(Cake)
      EFFECT: Have(Cake))
    
```

# Cake example



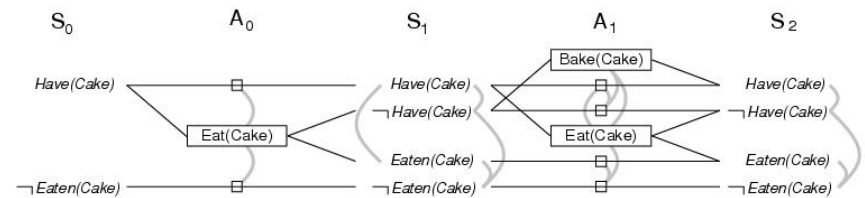
Start at level  $S_0$  and determine action level  $A_0$  and next level  $S_1$ .

- $A_0 \gg$  all actions whose preconditions are satisfied in the previous level.
- Connect precondition and effect of actions  $S_0 \rightarrow S_1$
- Inaction is represented by *persistence actions*.

Level  $A_0$  contains the actions that could occur

- Conflicts between actions are represented by *mutex* links

# Cake example



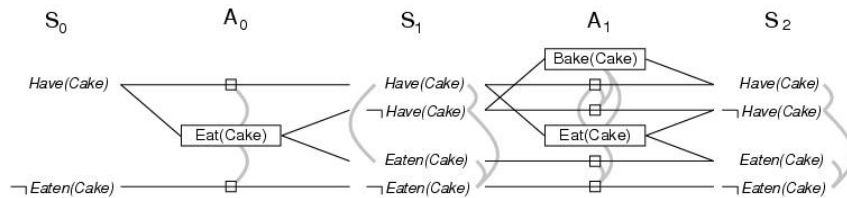
Level  $S_1$  contains all literals that could result from picking any subset of actions in  $A_0$

- Conflicts between literals that can not occur together (as a consequence of the selection action) are represented by mutex links.
- $S_1$  defines multiple states and the mutex links are the constraints that define this set of states.

Continue until two consecutive levels are identical: *leveled off*

- Or contain the same amount of literals

# Cake example



A mutex relation holds between **two actions** when:

- *Inconsistent effects*: one action negates the effect of another.
- *Interference*: one of the effects of one action is the negation of a precondition of the other.
- *Competing needs*: one of the preconditions of one action is mutually exclusive with the precondition of the other.

A mutex relation holds between **two literals** when (*inconsistent support*):

- If one is the negation of the other OR
- if each possible action pair that could achieve the literals is mutex.

# PG and heuristic estimation

PG's provide information about the problem

- A literal that does not appear in the final level of the graph cannot be achieved by any plan.
  - Useful for backward search (cost = inf).
- Level of appearance can be used as cost estimate of achieving any goal literals = *level cost*.
- Small problem: several actions can occur
  - Restrict to one action using serial PG (add mutex links between every pair of actions, except persistence actions).
- Cost of a conjunction of goals? Max-level, sum-level and set-level heuristics.

PG is a relaxed problem.

# The GRAPHPLAN Algorithm

How to extract a solution directly from the PG

```

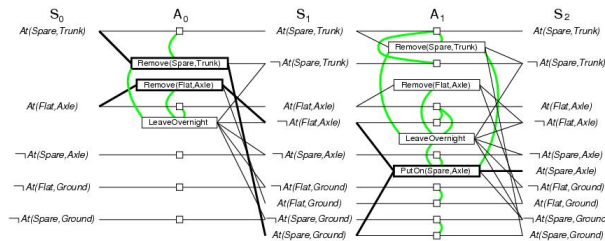
function GRAPHPLAN(problem) return solution or failure
  graph ← INITIAL-PLANNING-GRAPH(problem)
  goals ← GOALS[problem]
  loop do
    if goals all non-mutex in last level of graph then do
      solution ← EXTRACT-SOLUTION(graph, goals, LENGTH(graph))
    if solution ≠ failure then return solution
    else if NO-SOLUTION-POSSIBLE(graph) then return failure
    graph ← EXPAND-GRAPH(graph, problem)
    
```

# Example: Spare tire problem

```

Init(At(Flat, Axle) ∧ At(Spare, trunk))
Goal(At(Spare, Axle))
Action(Remove(Spare, Trunk))
  PRECOND: At(Spare, Trunk)
  EFFECT: ¬At(Spare, Trunk) ∧ At(Spare, Ground))
Action(Remove(Flat, Axle))
  PRECOND: At(Flat, Axle)
  EFFECT: ¬At(Flat, Axle) ∧ At(Flat, Ground))
Action(PutOn(Spare, Axle))
  PRECOND: At(Spare, Ground) ∧ ¬At(Flat, Axle)
  EFFECT: At(Spare, Axle) ∧ ¬At(Spare, Ground))
Action(LeaveOvernight)
  PRECOND:
  EFFECT: ¬At(Spare, Ground) ∧ ¬At(Spare, Axle) ∧ ¬At(Spare, trunk) ∧ ¬At(Flat, Ground) ∧
    ¬At(Flat, Axle) )
    
```

# GRAPHPLAN example



Initially the plan consist of 5 literals from the initial state and the CWA literals ( $S_0$ ).

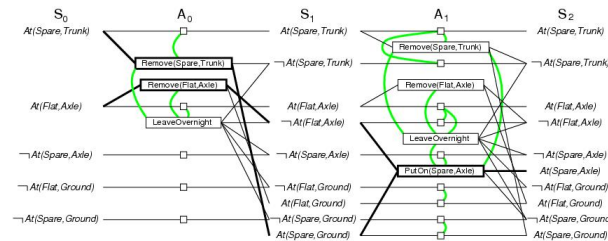
Add actions whose preconditions are satisfied by EXPAND-GRAPH ( $A_0$ )

Also add persistence actions and mutex relations.

Add the effects at level  $S_1$

Repeat until goal is in level  $S_i$

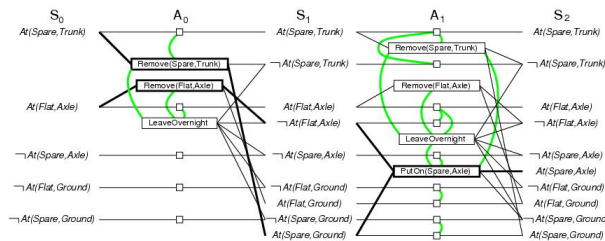
# GRAPHPLAN example



EXPAND-GRAPH also looks for mutex relations

- Inconsistent effects
  - E.g. Remove(Spare, Trunk) and LeaveOverNight due to At(Spare, Ground) and **not** At(Spare, Ground)
- Interference
  - E.g. Remove(Flat, Axle) and LeaveOverNight At(Flat, Axle) as PRECOND and **not** At(Flat, Axle) as EFFECT
- Competing needs
  - E.g. PutOn(Spare, Axle) and Remove(Flat, Axle) due to At(Flat, Axle) and **not** At(Flat, Axle)
- Inconsistent support
  - E.g. in  $S_2$ , At(Spare, Axle) and At(Flat, Axle)

# GRAPHPLAN example



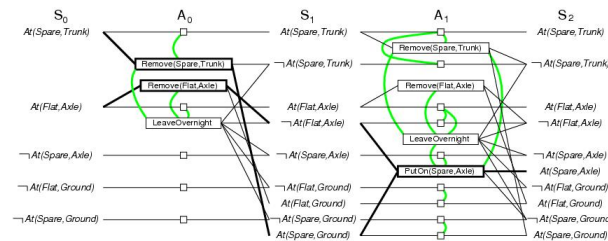
In  $S_{2r}$  the goal literals exist and are not mutex with any other

- Solution might exist and EXTRACT-SOLUTION will try to find it

EXTRACT-SOLUTION can use Boolean CSP to solve the problem or a search process:

- Initial state = last level of PG and goal goals of planning problem
- Actions = select any set of non-conflicting actions that cover the goals in the state
- Goal = reach level  $S_0$  such that all goals are satisfied
- Cost = 1 for each action.

# GRAPHPLAN example



Termination? YES

PG are monotonically increasing or decreasing:

- Literals increase monotonically
- Actions increase monotonically
- Mutexes decrease monotonically

Because of these properties and because there is a finite number of actions and literals, every PG will eventually level off !

## Planning with propositional logic

Planning can be done by proving theorem in situation calculus.  
Here: test the *satisfiability* of a logical sentence:

*initial state*  $\wedge$  *all possible action descriptions*  $\wedge$  *goal*

Sentence contains propositions for every action occurrence.

- A model will assign true to the actions that are part of the correct plan and false to the others
- An assignment that corresponds to an incorrect plan will not be a model because of inconsistency with the assertion that the goal is true.
- If the planning is unsolvable the sentence will be unsatisfiable.

## Analysis of planning approach

Planning is an area of great interest within AI

- Search for solution
- Constructively prove a existence of solution

Biggest problem is the combinatorial explosion in states.

Efficient methods are under research

- E.g. divide-and-conquer

## Planning vs. scheduling

Classical planning:

What to do? In what order?

But not:

How long? When? Using what resources?

Normally:

Plan first, schedule later.

## Representation

Job-shop scheduling problem:

- ◆ A set of jobs
- ◆ Each job is a collection of ACTIONS with some ORDERING CONSTRAINTS
- ◆ Each action has a DURATION and a set of RESOURCE CONSTRAINTS  
resources may be CONSUMABLE or REUSABLE

Solution:

Start times for all actions, obeying all constraints