

Planning 1

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Original slides can be found at <http://aima.cs.berkeley.edu>



Vrije Universiteit Brussel

Planning

The Planning problem
Planning with State-space search
Partial-order planning
Planning graphs
Planning with propositional logic
Analysis of planning approaches

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What is Planning

Generate sequences of actions to perform tasks and achieve objectives.

- States, actions and goals

Search for solution over abstract space of plans.

Classical planning environment: fully observable, deterministic, finite, static and discrete.

Assists humans in practical applications

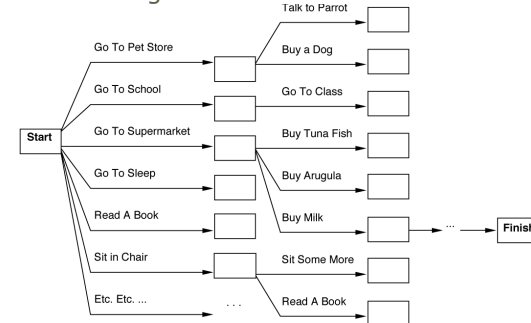
- design and manufacturing
- military operations
- games
- space exploration

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Why not standard search?

Consider the task **get milk, bananas and a cordless drill**

Standard search algorithms fail



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Difficulty of real world problems

Assume a problem-solving agent using some search method ...

- Which actions are relevant?
 - Exhaustive search vs. backward search
- What is a good heuristic functions?
 - Good estimate of the cost of the state?
 - Problem-dependent vs, -independent
- How to decompose the problem?
 - Most real-world problems are *nearly* decomposable.

Planning language

What is a good language?

- Expressive enough to describe a wide variety of problems.
- Restrictive enough to allow efficient algorithms to operate on it.
- Planning algorithm should be able to take advantage of the logical structure of the problem.

STRIPS and PDDL

General language features

Representation of states

- Decompose the world in logical conditions and represent a state as a *conjunction of positive literals*.
 - Propositional literals: *Poor* \wedge *Unknown*
 - FO-literals (grounded and function-free): *At(Plane1, Copenhagen)* \wedge *At(Plane2, Oslo)*
- Closed world assumption

Representation of goals

- Partially specified state and represented as a *conjunction of positive ground literals*
- A goal is *satisfied* if the state contains all literals in goal.

General language features

Representations of actions

- Action = PRECOND + EFFECT
 - Action(Fly(p,from, to),*
 - PRECOND: At(p,from) \wedge Plane(p) \wedge Airport(from) \wedge Airport(to)*
 - EFFECT: \neg AT(p,from) \wedge At(p,to)*
- = action schema (p, from, to need to be instantiated)
 - Action name and parameter list
 - Precondition (conj. of function-free literals)
 - Effect (conj of function-free literals and P is True and not P is false)
- Add-list vs delete-list in Effect

Language semantics?

How do actions affect states?

- An action is applicable in any state that satisfies the precondition.
- For FO action schema applicability involves a substitution θ for the variables in the PRECOND.

$At(P1,JFK) \wedge At(P2,SFO) \wedge Plane(P1) \wedge Plane(P2) \wedge Airport(JFK) \wedge Airport(SFO)$

Satisfies : $At(p,from) \wedge Plane(p) \wedge Airport(from) \wedge Airport(to)$

With $\theta = \{p/P1, from/JFK, to/SFO\}$

Thus the action is applicable.

Language semantics?

The result of executing action a in state s is the state s'

- s' is same as s except
 - Any positive literal P in the effect of a is added to s'
 - Any negative literal $\neg P$ is removed from s'

EFFECT: $\neg At(p,from) \wedge At(p,to)$:

$At(P1,SFO) \wedge At(P2,SFO) \wedge Plane(P1) \wedge Plane(P2) \wedge Airport(JFK) \wedge Airport(SFO)$

- STRIPS assumption: (avoids representational frame problem)
every literal NOT in the effect remains unchanged

Expressiveness and extensions

STRIPS is simplified

- Important limit: function-free literals
 - Allows for propositional representation
 - Function symbols lead to infinitely many states and actions

Expressiveness extension: Planning Domain Description language (PDDL)

Action($Fly(p:Plane, from: Airport, to: Airport)$,

PRECOND: $At(p,from) \wedge (from \neq to)$

EFFECT: $\neg At(p,from) \wedge At(p,to)$)

Standardization : now (2008) in its 3.1 version

Example: air cargo transport

Init($At(C1, SFO) \wedge At(C2,JFK) \wedge At(P1,SFO) \wedge At(P2,JFK) \wedge Cargo(C1) \wedge Cargo(C2) \wedge Plane(P1) \wedge Plane(P2) \wedge Airport(JFK) \wedge Airport(SFO)$)

Goal($At(C1,JFK) \wedge At(C2,SFO)$)

Action($Load(c,p,a)$

PRECOND: $At(c,a) \wedge At(p,a) \wedge Cargo(c) \wedge Plane(p) \wedge Airport(a)$

EFFECT: $\neg At(c,a) \wedge In(c,p)$)

Action($Unload(c,p,a)$

PRECOND: $In(c,p) \wedge At(p,a) \wedge Cargo(c) \wedge Plane(p) \wedge Airport(a)$

EFFECT: $At(c,a) \wedge \neg In(c,p)$)

Action($Fly(p,from,to)$

PRECOND: $At(p,from) \wedge Plane(p) \wedge Airport(from) \wedge Airport(to)$

EFFECT: $\neg At(p,from) \wedge At(p,to)$)

[$Load(C1,P1,SFO), Fly(P1,SFO,JFK), Load(C2,P2,JFK), Fly(P2,JFK,SFO)$]

Example: Spare tire problem

```

Init(At(Flat, Axle)  $\wedge$  At(Spare, trunk))
Goal(At(Spare, Axle))
Action(Remove(Spare, Trunk))
  PRECOND: At(Spare, Trunk)
  EFFECT:  $\neg$ At(Spare, Trunk)  $\wedge$  At(Spare, Ground))
Action(Remove(Flat, Axle))
  PRECOND: At(Flat, Axle)
  EFFECT:  $\neg$ At(Flat, Axle)  $\wedge$  At(Flat, Ground))
Action(PutOn(Spare, Axle))
  PRECOND: At(Spare, Ground)  $\wedge$   $\neg$ At(Flat, Axle)
  EFFECT: At(Spare, Axle)  $\wedge$   $\neg$ At(Spare, Ground))
Action(LeaveOvernight)
  PRECOND:
  EFFECT:  $\neg$  At(Spare, Ground)  $\wedge$   $\neg$  At(Spare, Axle)  $\wedge$   $\neg$  At(Spare, trunk)  $\wedge$   $\neg$  At(Flat, Ground)  $\wedge$   $\neg$  At(Flat, Axle) )
    
```

This example goes beyond STRIPS: negative literal in pre-condition (PDDL description)

Example: Blocks world

```

Init(On(A, Table)  $\wedge$  On(B, Table)  $\wedge$  On(C, Table)  $\wedge$  Block(A)  $\wedge$  Block(B)
 $\wedge$  Block(C)  $\wedge$  Clear(A)  $\wedge$  Clear(B)  $\wedge$  Clear(C))
Goal(On(A, B)  $\wedge$  On(B, C))
Action(Move(b, x, y))
  PRECOND: On(b, x)  $\wedge$  Clear(b)  $\wedge$  Clear(y)  $\wedge$  Block(b)  $\wedge$  (b  $\neq$  x)  $\wedge$  (b  $\neq$  y)  $\wedge$  (x  $\neq$  y)
  EFFECT: On(b, y)  $\wedge$  Clear(x)  $\wedge$   $\neg$  On(b, x)  $\wedge$   $\neg$  Clear(y))
Action(MoveToTable(b, x))
  PRECOND: On(b, x)  $\wedge$  Clear(b)  $\wedge$  Block(b)  $\wedge$  (b  $\neq$  x)
  EFFECT: On(b, Table)  $\wedge$  Clear(x)  $\wedge$   $\neg$  On(b, x))
    
```

Spurious actions are possible: Move(B,C,C)

Planning with state-space search

Both forward and backward search possible

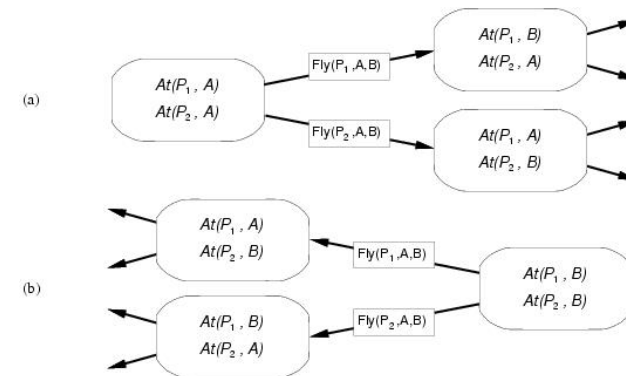
Progression planners

- forward state-space search
- Consider the effect of all possible actions in a given state

Regression planners

- backward state-space search
- To achieve a goal, what must have been true in the previous state.

Progression and regression



Progression algorithm

Formulation as state-space search problem:

- Initial state = initial state of the planning problem
 - Literals not appearing are false
- Actions = those whose preconditions are satisfied
 - Add positive effects, delete negative
- Goal test = does the state satisfy the goal
- Step cost = each action costs 1

No functions ... any graph search that is complete is a complete planning algorithm.

- E.g. A*

Inefficient:

- (1) irrelevant action problem
- (2) good heuristic required for efficient search

Regression algorithm

How to determine predecessors?

- What are the states from which applying a given action leads to the goal?

Goal state = $At(C1, B) \wedge At(C2, B) \wedge \dots \wedge At(C20, B)$

Relevant action for first conjunct: $Unload(C1, p, B)$

Works only if pre-conditions are satisfied.

Previous state = $In(C1, p) \wedge At(p, B) \wedge At(C2, B) \wedge \dots \wedge At(C20, B)$

Subgoal $At(C1, B)$ should not be present in this state.

Actions must not undo desired literals (consistent)

Main advantage: only relevant actions are considered.

- Often much lower branching factor than forward search.

Regression algorithm

General process for predecessor construction

- Give a goal description G
- Let A be an action that is relevant and consistent
- The predecessors is as follows:
 - Any positive effects of A that appear in G are deleted.
 - Each precondition literal of A is added, unless it already appears.

Any standard search algorithm can be added to perform the search.

Termination when predecessor satisfied by initial state.

- In FO case, satisfaction might require a substitution.

Heuristics for state-space search

Neither progression or regression are very efficient without a good heuristic.

- How many actions are needed to achieve the goal?
- Exact solution is NP hard, find a good estimate

Two approaches to find admissible heuristic:

- The optimal solution to the relaxed problem.
 - Remove all preconditions from actions
- The subgoal independence assumption:
 - The cost of solving a conjunction of subgoals is approximated by the sum of the costs of solving the subproblems independently.

Partial-order planning

Progression and regression planning are *totally ordered plan search forms*.

- They cannot take advantage of problem decomposition.
 - Decisions must be made on how to sequence actions on all the subproblems

Least commitment strategy:

- Delay choice during search

Shoe example

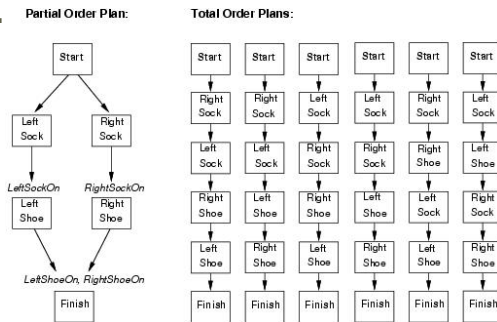
```

Goal(RightShoeOn ^ LeftShoeOn)
Init()
Action(RightShoe,    PRECOND: RightSockOn
      EFFECT: RightShoeOn)
Action(RightSock,    PRECOND:
      EFFECT: RightSockOn)
Action(LeftShoe,     PRECOND: LeftSockOn
      EFFECT: LeftShoeOn)
Action(LeftSock,     PRECOND:
      EFFECT: LeftSockOn)
    
```

Planner: combine two action sequences (1)leftsock, leftshoe (2)rightsock, rightshoe

Partial-order planning(POP)

Any planning algorithm that can place two actions into a plan without which comes first is a PO plan.



POP as a search problem

States are (mostly unfinished) plans.

- The empty plan contains only start and finish actions.

Each plan has 4 components:

- A set of actions (steps of the plan)
- A set of ordering constraints: $A < B$ (A before B)
 - Cycles represent contradictions.
- A set of causal links $A \xrightarrow{p} B$
 - The plan may not be extended by adding a new action C that conflicts with the causal link. (if the effect of C is $\neg p$ and if C could come after A and before B)
- A set of open preconditions.
 - If precondition is not achieved by action in the plan.

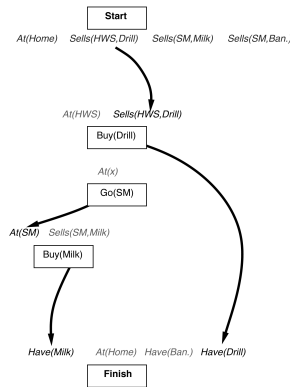
Example of final plan

Actions={Rightsock, Rightshoe, Leftsock, Leftshoe, Start, Finish}
 Orderings={Rightsock < Rightshoe; Leftsock < Leftshoe}
 Links={Rightsock->Rightsockon -> Rightshoe, Leftsock->Leftsockon-> Leftshoe, Rightshoe->Rightshoeon->Finish, ...}
 Open preconditions={ }

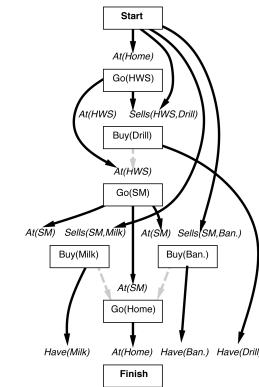
Shopping list example



Shopping list example



Shopping list example



POP as a search problem

A plan is *consistent* iff there are no cycles in the ordering constraints and no conflicts with the causal links.

A consistent plan with no open preconditions is a *solution*.

A partial order plan is executed by repeatedly choosing *any* of the possible next actions.

- This flexibility is a benefit in non-cooperative environments.

Solving POP

Assume propositional planning problems:

- The initial plan contains *Start* and *Finish*, the ordering constraint $Start < Finish$, no causal links, all the preconditions in *Finish* are open.
- Successor function :
 - picks one open precondition p on an action B and
 - generates a successor plan for every possible consistent way of choosing action A that achieves p .
- Test goal

Enforcing consistency

When generating successor plan:

- The causal link $A \rightarrow p \rightarrow B$ and the ordering constraint $A < B$ is added to the plan.
 - If A is new also add $start < A$ and $A < B$ to the plan
- Resolve conflicts between new causal link and all existing actions
- Resolve conflicts between action A (if new) and all existing causal links.

Process summary

Operators on partial plans

- Add link from existing plan to open precondition.
- Add a step to fulfill an open condition.
- Order one step w.r.t another to remove possible conflicts

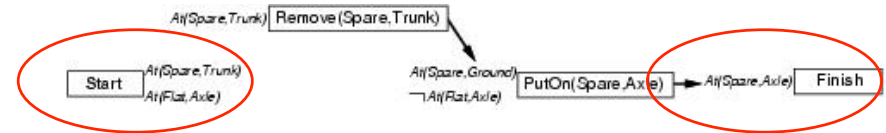
Gradually move from incomplete/vague plans to complete/correct plans

Backtrack if an open condition is unachievable or if a conflict is irresolvable.

Example: Spare tire problem

Init($At(Flat, Axle) \wedge At(Spare, trunk)$)
Goal($At(Spare, Axle)$)
Action(*Remove*(*Spare*, *Trunk*))
 PRECOND: $At(Spare, Trunk)$
 EFFECT: $\neg At(Spare, Trunk) \wedge At(Spare, Ground)$
Action(*Remove*(*Flat*, *Axle*))
 PRECOND: $At(Flat, Axle)$
 EFFECT: $\neg At(Flat, Axle) \wedge At(Flat, Ground)$
Action(*PutOn*(*Spare*, *Axle*))
 PRECOND: $At(Spare, Ground) \wedge \neg At(Flat, Axle)$
 EFFECT: $At(Spare, Axle) \wedge \neg At(Spare, Ground)$
Action(*LeaveOvernight*)
 PRECOND:
 EFFECT: $\neg At(Spare, Ground) \wedge \neg At(Spare, Axle) \wedge \neg At(Spare, trunk) \wedge \neg At(Flat, Ground) \wedge \neg At(Flat, Axle)$

Solving the problem



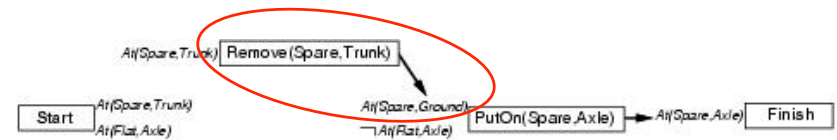
Initial plan: Start with EFFECTS and Finish with PRECOND.

Solving the problem



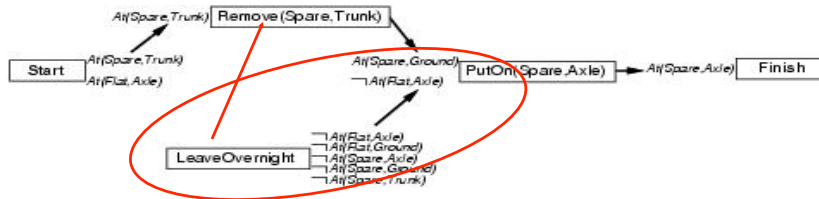
Initial plan: Start with EFFECTS and Finish with PRECOND.
 Pick an open precondition: $At(Spare, Axle)$
 Only *PutOn*(*Spare*, *Axle*) is applicable
 Add causal link: $PutOn(Spare, Axle) \xrightarrow{At(Spare, Axle)} Finish$
 Add constraint : $PutOn(Spare, Axle) < Finish$

Solving the problem



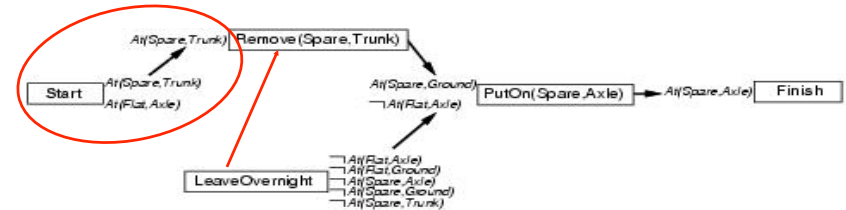
Pick an open precondition: $At(Spare, Ground)$
 Only *Remove*(*Spare*, *Trunk*) is applicable
 Add causal link: $Remove(Spare, Trunk) \xrightarrow{At(Spare, Ground)} PutOn(Spare, Axle)$
 Add constraint : $Remove(Spare, Trunk) < PutOn(Spare, Axle)$

Solving the problem



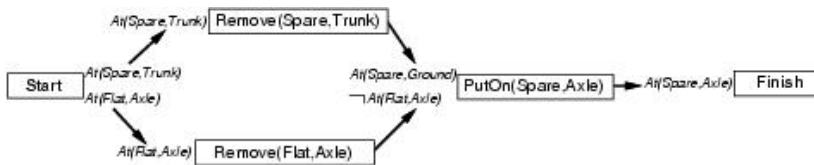
Pick an open precondition: $\neg At(Flat, Axle)$
 LeaveOverNight is applicable
 conflict: LeaveOverNight also has the effect $\neg At(Spare, Ground)$
 $Remove(Spare, Trunk) \xrightarrow{At(Spare, Ground)} PutOn(Spare, Axle)$
 To resolve, add constraint : $LeaveOverNight < Remove(Spare, Trunk)$

Solving the problem



Pick an open precondition: $At(Spare, Trunk)$
 Only Start is applicable
 Add causal link: $Start \xrightarrow{At(Spare, Trunk)} Remove(Spare, Trunk)$
 Conflict: of causal link with effect $At(Spare, Trunk)$ in LeaveOverNight
 - No re-ordering solution possible.
 backtrack

Solving the problem



Remove LeaveOverNight, $Remove(Spare, Trunk)$ and causal links
 Repeat step with $Remove(Spare, Trunk)$
 Add also RemoveFlatAxle and finish

Some details ...

What happens when a first-order representation that includes variables is used?

- Complicates the process of detecting and resolving conflicts.
- Can be resolved by introducing inequality constraint.

CSP's most-constrained-variable constraint can be used for planning algorithms to select a PRECOND.

Planning graphs

Used to achieve better heuristic estimates.

- A solution can also directly extracted using GRAPHPLAN.

Consists of a sequence of levels that correspond to time steps in the plan.

- Level 0 is the initial state.
- Each level consists of a set of literals and a set of actions.
 - *Literals* = all those that *could* be true at that time step, depending upon the actions executed at the preceding time step.
 - *Actions* = all those actions that *could* have their preconditions satisfied at that time step, depending on which of the literals actually hold.

Planning graphs

"Could"?

- Records only a restricted subset of possible negative interactions among actions.

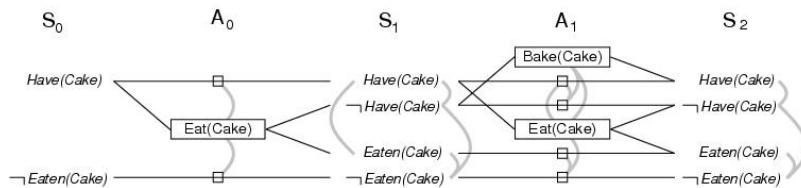
They work only for propositional problems.

Example:

```

Init(Have(Cake))
Goal(Have(Cake) ^ Eaten(Cake))
Action(Eat(Cake), PRECOND: Have(Cake)
      EFFECT: ~Have(Cake) ^ Eaten(Cake))
Action(Bake(Cake), PRECOND: ~Have(Cake)
      EFFECT: Have(Cake))
    
```

Cake example



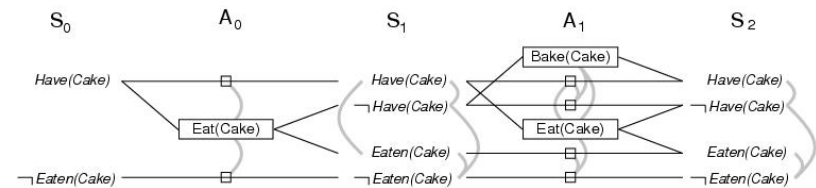
Start at level S0 and determine action level A0 and next level S1.

- A0 >> all actions whose preconditions are satisfied in the previous level.
- Connect precond and effect of actions S0 --> S1
- Inaction is represented by *persistence actions*.

Level A0 contains the actions that could occur

- Conflicts between actions are represented by *mutex links*

Cake example



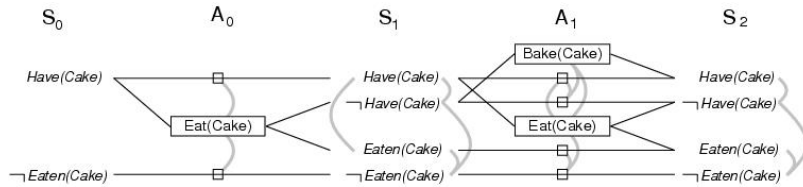
Level S1 contains all literals that could result from picking any subset of actions in A0

- Conflicts between literals that can not occur together (as a consequence of the selection action) are represented by mutex links.
- S1 defines multiple states and the mutex links are the constraints that define this set of states.

Continue until two consecutive levels are identical: *leveled off*

- Or contain the same amount of literals (explanation follows later)

Cake example



A mutex relation holds between **two actions** when:

- *Inconsistent effects*: one action negates the effect of another.
- *Interference*: one of the effects of one action is the negation of a precondition of the other.
- *Competing needs*: one of the preconditions of one action is mutually exclusive with the precondition of the other.

A mutex relation holds between **two literals** when (*inconsistent support*):

- If one is the negation of the other OR
- if each possible action pair that could achieve the literals is mutex.

PG and heuristic estimation

PG's provide information about the problem

- A literal that does not appear in the final level of the graph cannot be achieved by any plan.
 - Useful for backward search (cost = inf).
- Level of appearance can be used as cost estimate of achieving any goal literals = *level cost*.
- Small problem: several actions can occur
 - Restrict to one action using serial PG (add mutex links between every pair of actions, except persistence actions).
- Cost of a conjunction of goals? Max-level, sum-level and set-level heuristics.

PG is a relaxed problem.

The GRAPHPLAN Algorithm

How to extract a solution directly from the PG

```

function GRAPHPLAN(problem) return solution or failure
  graph ← INITIAL-PLANNING-GRAPH(problem)
  goals ← GOALS[problem]
  loop do
    if goals all non-mutex in last level of graph then do
      solution ← EXTRACT-SOLUTION(graph, goals, LENGTH(graph))
      if solution ≠ failure then return solution
      else if NO-SOLUTION-POSSIBLE(graph) then return failure
      graph ← EXPAND-GRAPH(graph, problem)
    
```

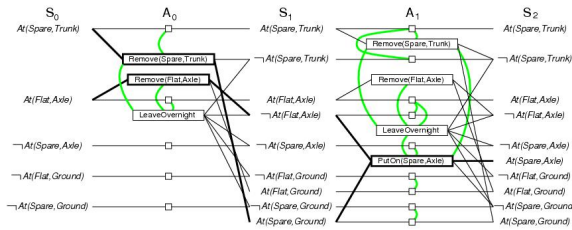
Example: Spare tire problem

```

Init(At(Flat, Axle) ∧ At(Spare, trunk))
Goal(At(Spare, Axle))
Action(Remove(Spare, Trunk))
  PRECOND: At(Spare, Trunk)
  EFFECT: ¬At(Spare, Trunk) ∧ At(Spare, Ground))
Action(Remove(Flat, Axle))
  PRECOND: At(Flat, Axle)
  EFFECT: ¬At(Flat, Axle) ∧ At(Flat, Ground))
Action(PutOn(Spare, Axle))
  PRECOND: At(Spare, Ground) ∧ ¬At(Flat, Axle)
  EFFECT: At(Spare, Axle) ∧ ¬At(Spare, Ground))
Action(LeaveOvernight)
  PRECOND:
  EFFECT: ¬At(Spare, Ground) ∧ At(Spare, Axle) ∧ ¬At(Spare, trunk) ∧ At(Flat, Ground) ∧ At(Flat, Axle) )
    
```

This example goes beyond STRIPS: negative literal in pre-condition (ADL description)

GRAPHPLAN example



Initially the plan consist of 5 literals from the initial state and the CWA literals (S0).

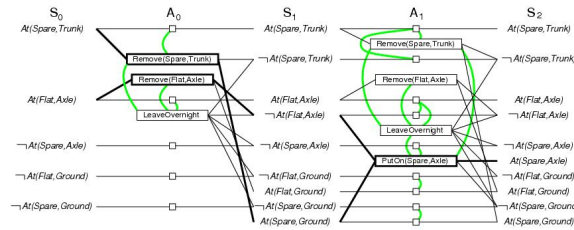
Add actions whose preconditions are satisfied by EXPAND-GRAPH (A0)

Also add persistence actions and mutex relations.

Add the effects at level S1

Repeat until goal is in level Si

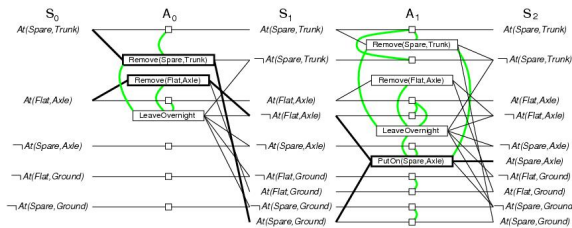
GRAPHPLAN example



EXPAND-GRAPH also looks for mutex relations

- Inconsistent effects
 - E.g. Remove(Spare, Trunk) and LeaveOverNight due to At(Spare,Ground) and **not** At(Spare, Ground)
- Interference
 - E.g. Remove(Flat, Axle) and LeaveOverNight At(Flat, Axle) as PRECOND and **not** At(Flat,Axle) as EFFECT
- Competing needs
 - E.g. PutOn(Spare,Axle) and Remove(Flat, Axle) due to At(Flat,Axle) and **not** At(Flat, Axle)
- Inconsistent support
 - E.g. in S2, At(Spare,Axle) and At(Flat,Axle)

GRAPHPLAN example



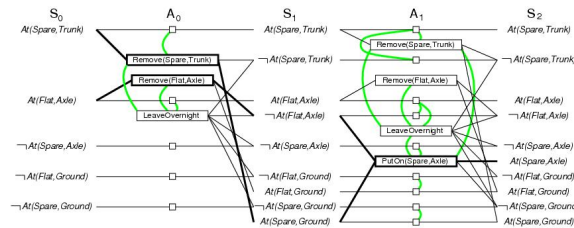
In S2, the goal literals exist and are not mutex with any other

- Solution might exist and EXTRACT-SOLUTION will try to find it

EXTRACT-SOLUTION can use Boolean CSP to solve the problem or a search process:

- Initial state = last level of PG and goal goals of planning problem
- Actions = select any set of non-conflicting actions that cover the goals in the state
- Goal = reach level S0 such that all goals are satisfied
- Cost = 1 for each action.

GRAPHPLAN example



Termination? YES

PG are monotonically increasing or decreasing:

- Literals increase monotonically
- Actions increase monotonically
- Mutexes decrease monotonically

Because of these properties and because there is a finite number of actions and literals, every PG will eventually level off !

Planning with propositional logic

Planning can be done by proving theorem in situation calculus.
Here: test the *satisfiability* of a logical sentence:

$initial\ state \wedge all\ possible\ action\ descriptions \wedge goal$

Sentence contains propositions for every action occurrence.

- A model will assign true to the actions that are part of the correct plan and false to the others
- An assignment that corresponds to an incorrect plan will not be a model because of inconsistency with the assertion that the goal is true.
- If the planning is unsolvable the sentence will be unsatisfiable.

SATPLAN algorithm

```
function SATPLAN(problem,  $T_{max}$ ) return solution or failure
inputs: problem, a planning problem
        $T_{max}$ , an upper limit to the plan length
for  $T = 0$  to  $T_{max}$  do
    cnf, mapping  $\leftarrow$  TRANSLATE-TO_SAT(problem,  $T$ )
    assignment  $\leftarrow$  SAT-SOLVER(cnf)
    if assignment is not null then
        return EXTRACT-SOLUTION(assignment, mapping)
return failure
```

$cnf, mapping \leftarrow TRANSLATE-TO_SAT$
 $(problem, T)$

Distinct propositions for assertions about each time step.

- Superscripts denote the time step
 $At(P1, SFO)^0 \wedge At(P2, JFK)^0$
- No CWA thus specify which propositions are not true
 $\neg At(P1, SFO)^0 \wedge \neg At(P2, JFK)^0$
- Unknown propositions are left unspecified.

The goal is associated with a particular time-step

- But which one?

$cnf, mapping \leftarrow TRANSLATE-TO_SAT$
 $(problem, T)$

How to determine the time step where the goal will be reached?

- Start at $T=0$
 - Assert $At(P1, SFO)^0 \wedge At(P2, JFK)^0$
- Failure .. Try $T=1$
 - Assert $At(P1, SFO)^1 \wedge At(P2, JFK)^1$
- ...
- Repeat this until some minimal path length is reached.
- Termination is ensured by T_{max}

$cnf, mapping \leftarrow \text{TRANSLATE-TO_SAT}(problem, T)$

How to encode actions into PL?

- Propositional versions of successor-state axioms
 $At(P1, JFK)^1 \Leftrightarrow (At(P1, JFK)^0 \wedge \neg(Fly(P1, JFK, SFO)^0 \wedge At(P1, JFK)^0)) \vee (Fly(P1, SFO, JFK)^0 \wedge At(P1, SFO)^0)$
- Such an axiom is required for each plane, airport and time step
- If more airports add another way to travel than additional disjuncts are required

Once all these axioms are in place, the satisfiability algorithm can start to find a plan.

$assignment \leftarrow \text{SAT-SOLVER}(cnf)$

Multiple models can be found

They are NOT satisfactory: (for $T=1$)

$$Fly(P1, SFO, JFK)^0 \wedge Fly(P1, JFK, SFO)^0 \wedge Fly(P2, JFK, SFO)^0$$

The second action is infeasible

Yet the plan IS a model of the sentence

$initial\ state \wedge all\ possible\ action\ descriptions \wedge goal^1$

Avoiding illegal actions: pre-condition axioms

$$Fly(P1, SFO, JFK)^0 \Rightarrow At(P1, JFK)$$

Exactly one model now satisfies all the axioms where the goal is achieved at $T=1$.

$assignment \leftarrow \text{SAT-SOLVER}(cnf)$

A plane can fly to two destinations at once

They are NOT satisfactory: (for $T=1$)

$$Fly(P1, SFO, JFK)^0 \wedge Fly(P2, JFK, SFO)^0 \wedge Fly(P2, JFK, LAX)^0$$

The second action is infeasible

Yet the plan allows spurious relations

Avoid spurious solutions: action-exclusion axioms

$$\neg(Fly(P2, JFK, SFO)^0 \wedge Fly(P2, JFK, LAX)^0)$$

Prevents simultaneous actions

Lost of flexibility since plan becomes totally ordered : no actions are allowed to occur at the same time.

- Restrict exclusion to preconditions

Analysis of planning approach

Planning is an area of great interest within AI

- Search for solution
- Constructively prove a existence of solution

Biggest problem is the combinatorial explosion in states.

Efficient methods are under research

- E.g. divide-and-conquer